



# NMR-lecture April 6th, 2009, FMP Berlin

**Christian Freund**

## Outline:

- **Basic understandings:**
  - Relaxation
  - Chemical exchange
- **Mapping interactions:**
  - .Chemical shift mapping (fast exchange)
  - Linewidth analysis (slow exchange)
  - .Cross saturation transfer
  - .Transfer NOE/STD NMR
  - .Half filter experiments/isotope labeling

# Monitoring protein:protein interactions: Capitalizing on chemical shift and relaxation rate changes

In the absence of an applied rf field, the Bloch equations are defined as:

$$\frac{dM_x(t)}{dt} = -\Omega M_y(t) - R_2 M_x(t)$$

In the case of chemical exchange it is :

$$\frac{dM_y(t)}{dt} = -\Omega M_x(t) - R_2 M_y(t)$$

$$\frac{dM_{xy}(t)}{dt} = -(\Omega - R_2 + K)M_{xy}(t)$$

$$\frac{dM_z(t)}{dt} = -\Omega\{M_z(t) - M_0\}$$

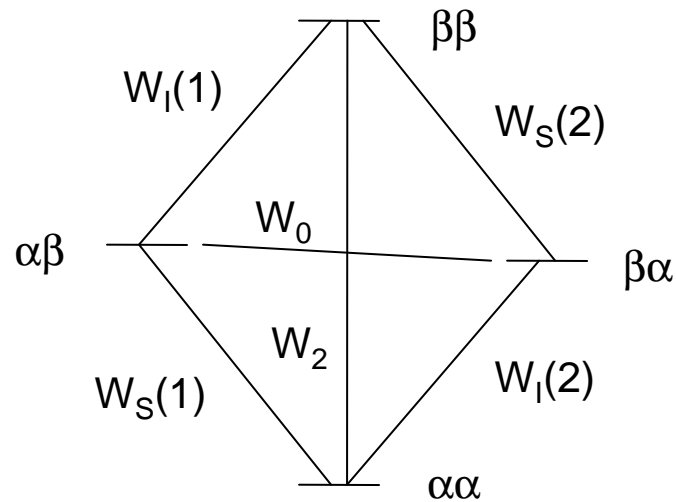
↓

$$\frac{dM_z(t)}{dt} = -(\Omega + K)\Delta M_z(t)$$

Formal solution :  $\Delta M_z(t) = e^{-Rt}\Delta M_z(0)$

$$R = \begin{bmatrix} \rho_I & \sigma_{IS} \\ \sigma_{IS} & \rho_S \end{bmatrix}$$

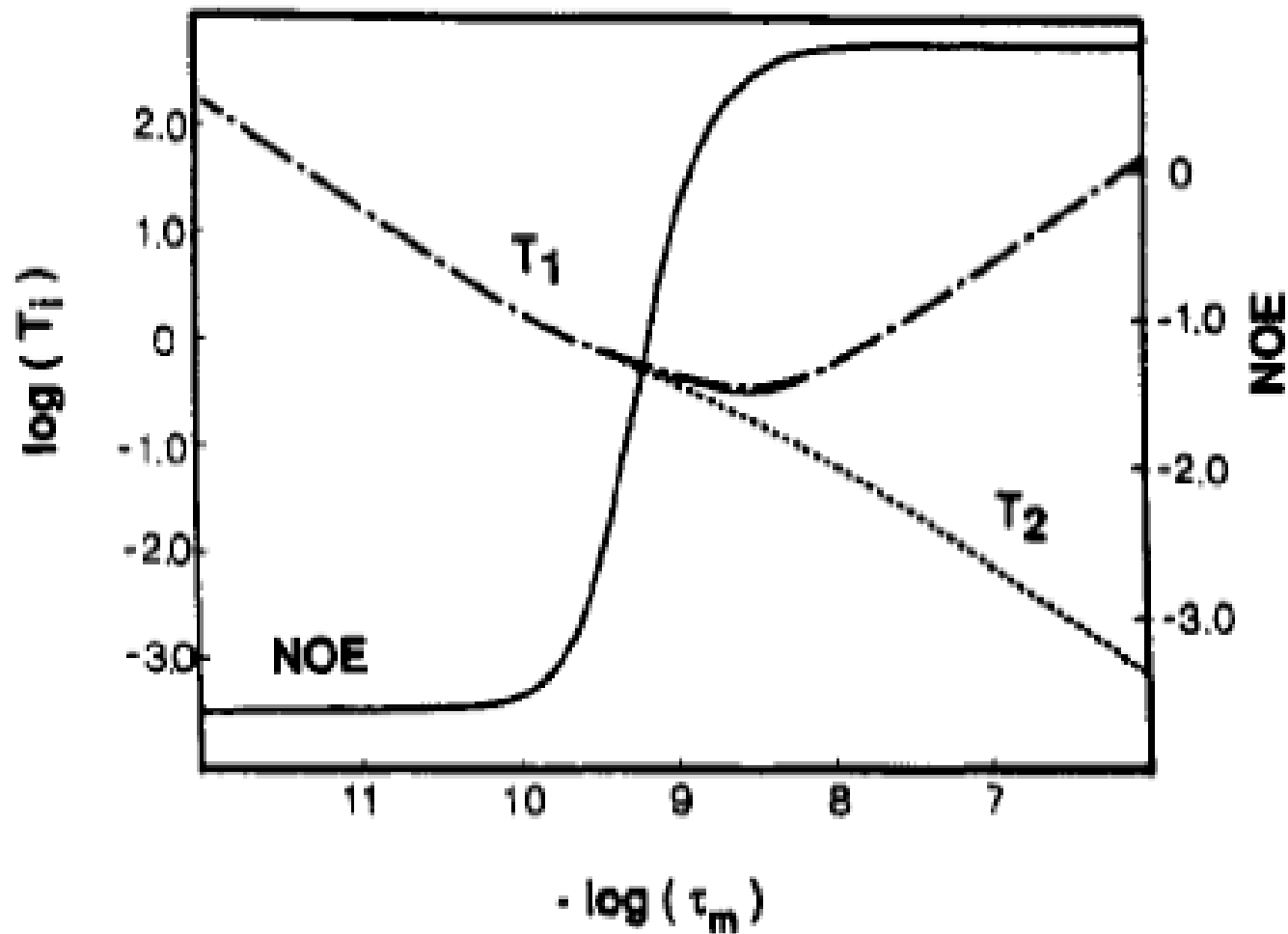
## Transitions between states in a two-spin system



$$\sigma = W_2 - W_0$$

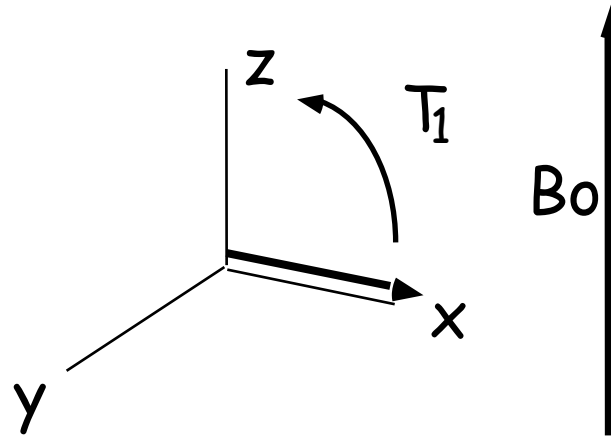
$$\sigma_{ij} \sim 1/r_{ij}^6 * [6J(2\omega_0) - J(0)]$$

Relaxation times depend on the overall tumbling time of molecules which is proportional to molecular weight

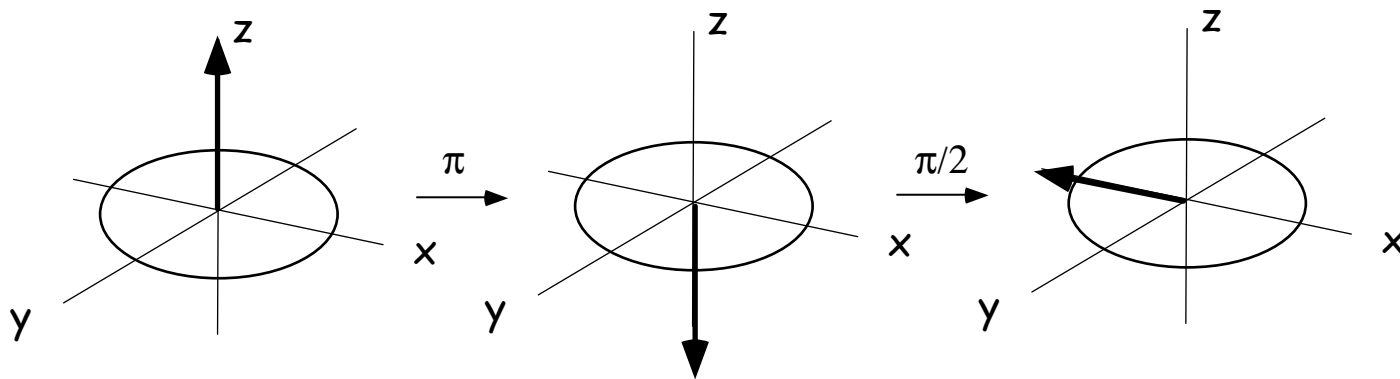


$$\tau_c = \frac{4\pi\eta r^3}{3kT}$$

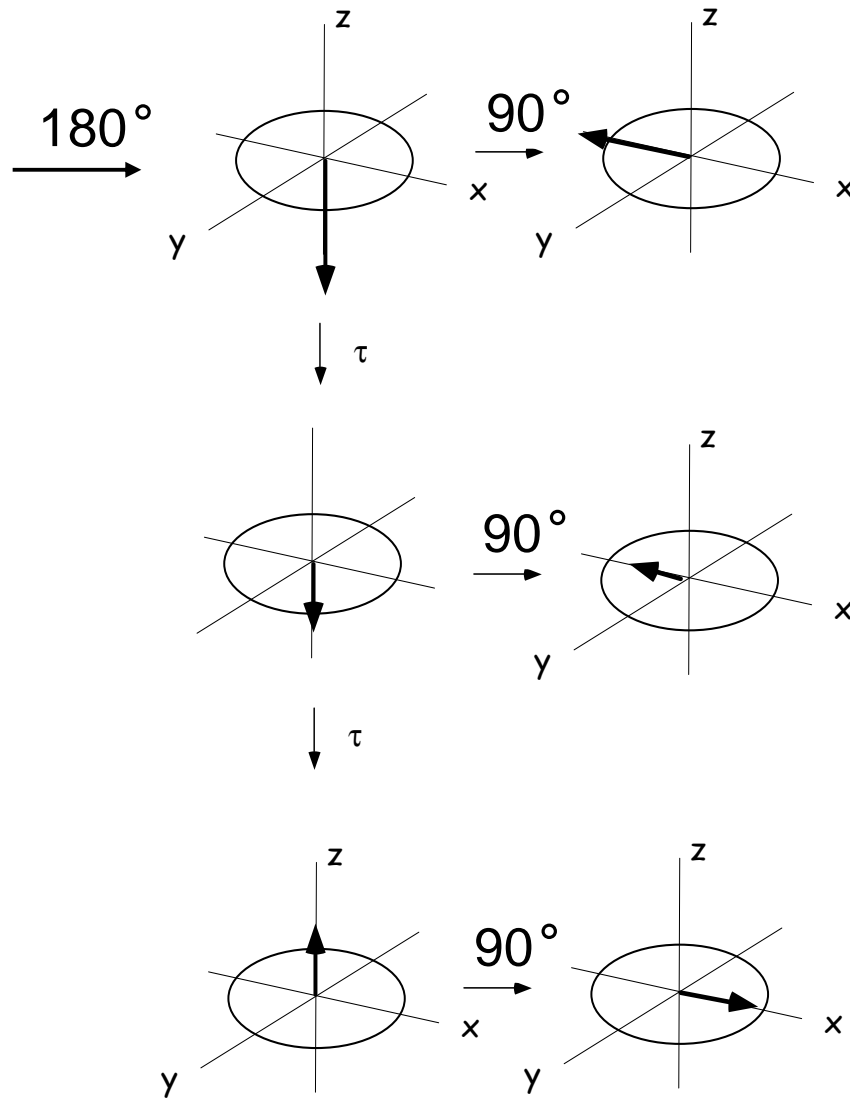
## $T_1$ relaxation



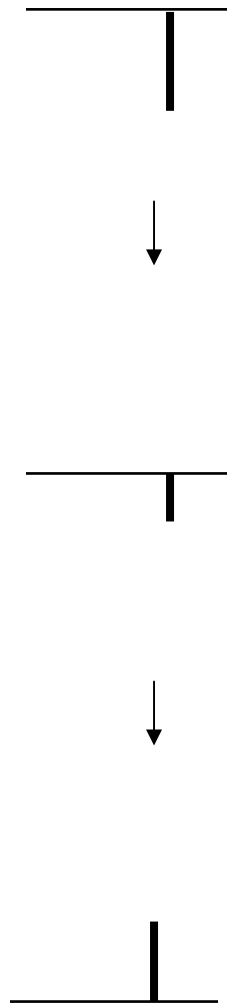
Measuring  $T_1$  from inversion recovery pulse sequence



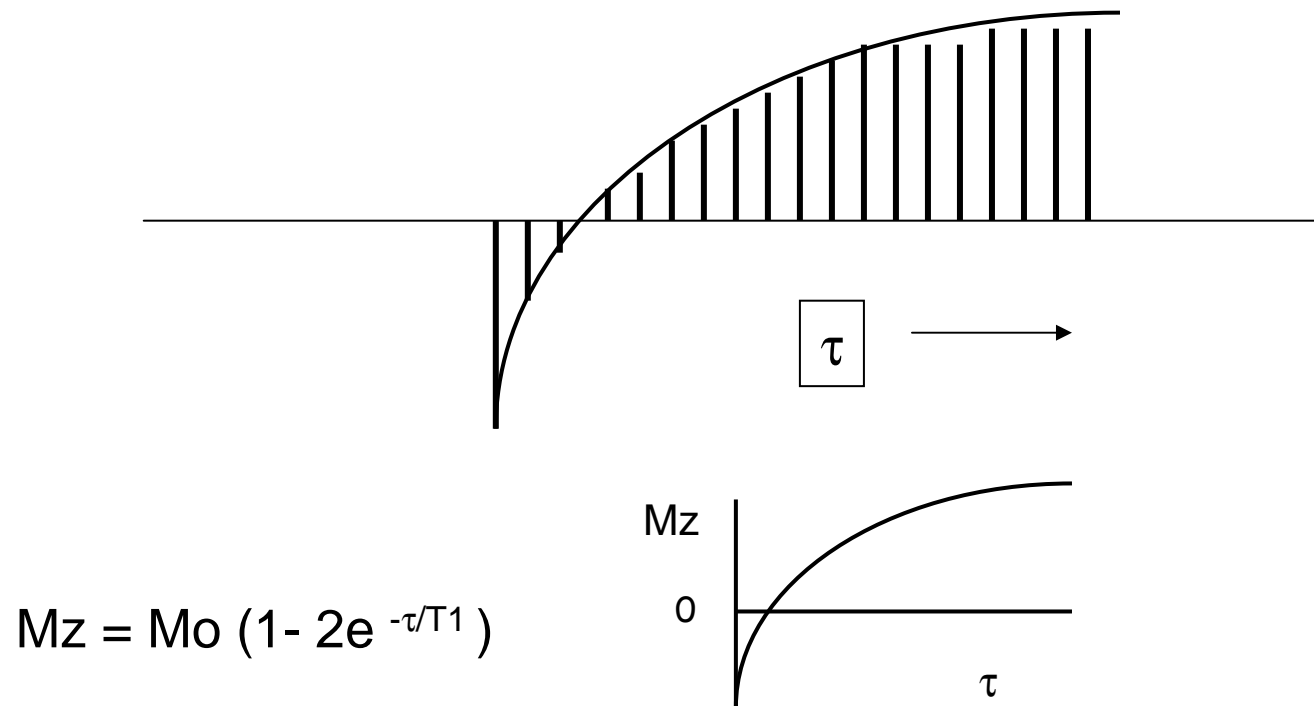
# Measuring T1 relaxation times



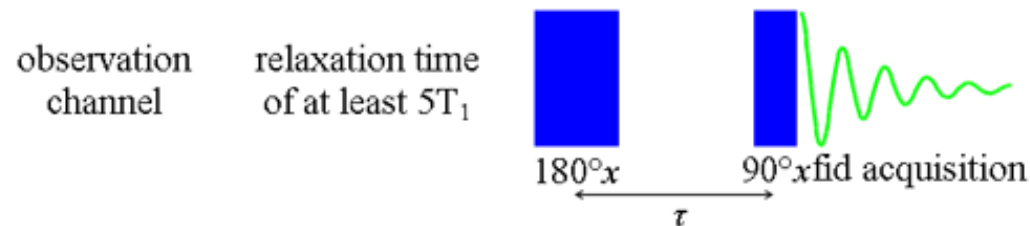
## Inversion Recovery



# Inversion Recovery - Measure NMR Intensity as a function of the delay time $\tau$ and fit to an exponential function

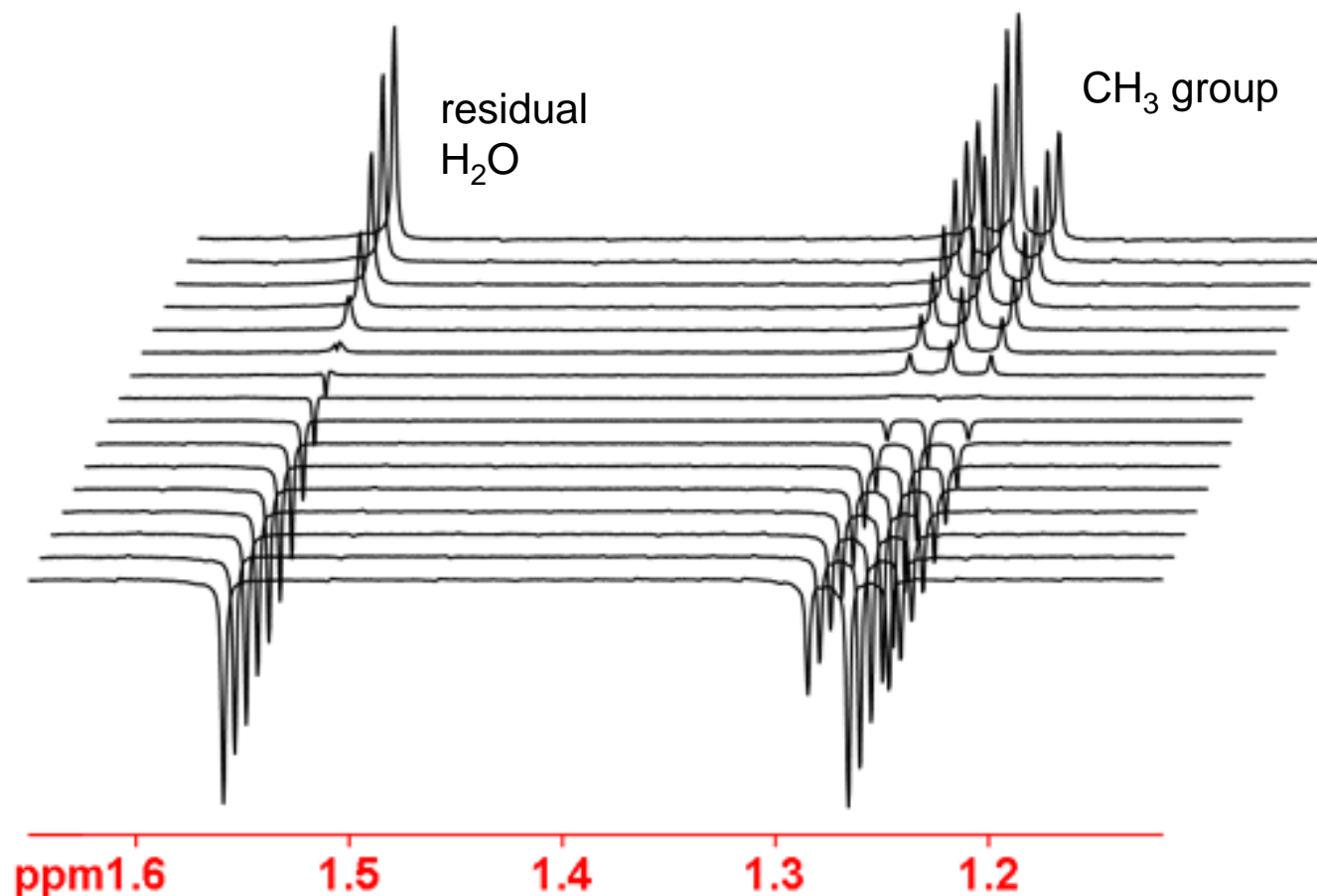


## Inversion recovery pulse sequence for measuring $T_1$



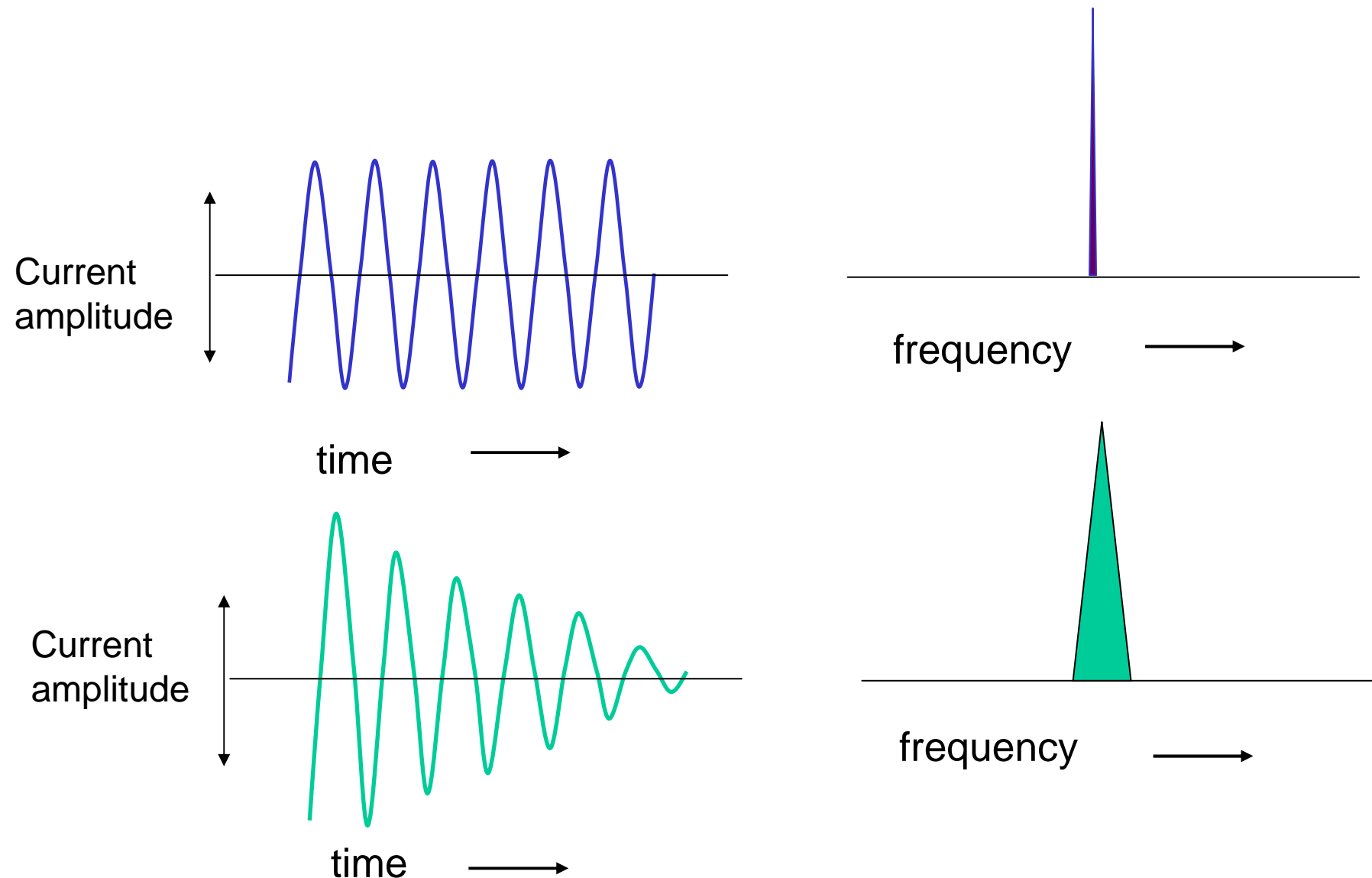
Adopted from Roy Hofmann,  
Hebrew University

The inversion recovery experiment yields T1 values for different signals that may have different relaxation times

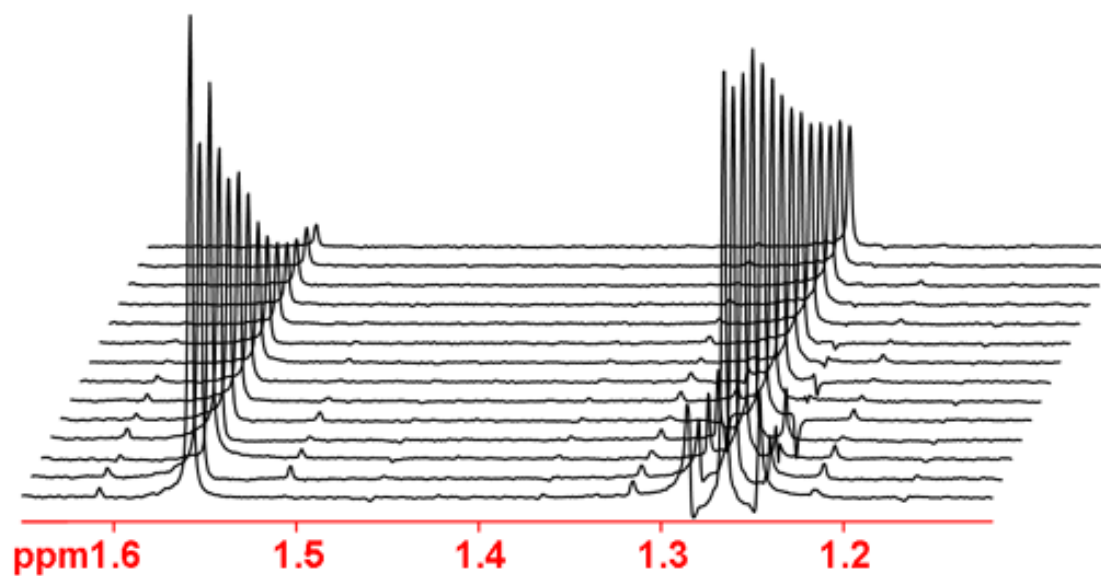
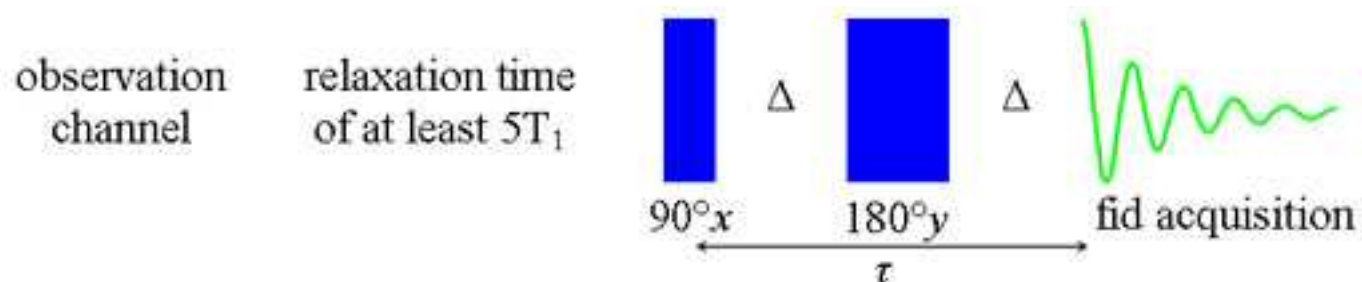


Example: Ethylbenzene in CDCl<sub>3</sub>

## $T_2$ relaxation leads to line-width broadening



## Spin-echo pulse sequence for measuring $T_2$



Example: Ethylbenzene in  $\text{CDCl}_3$

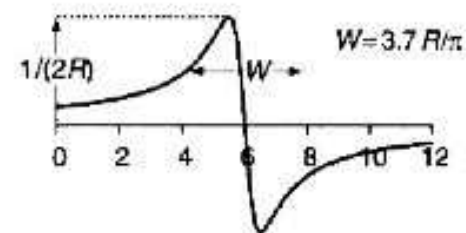
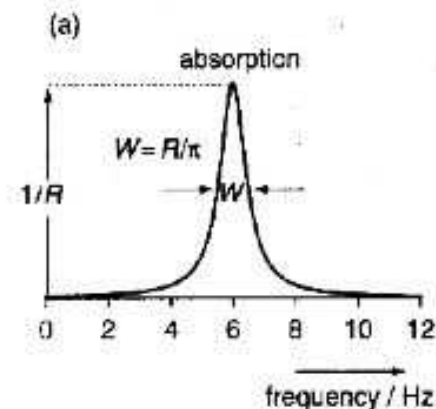
## Linewidth depends on transverse relaxation

$$S(\omega) = \text{Re} \int_0^{\infty} s^+(t) \exp(-i\omega t) dt$$

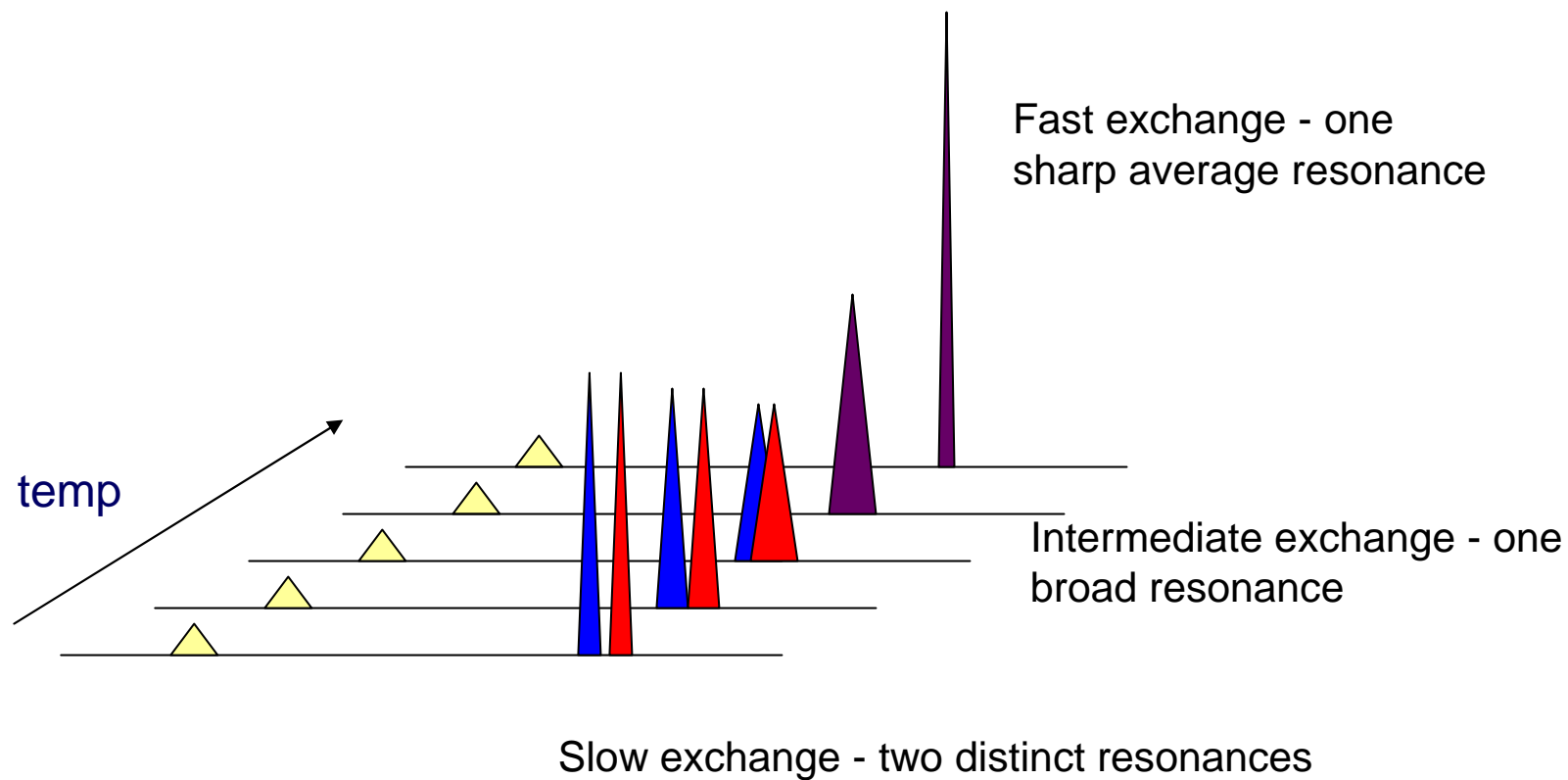
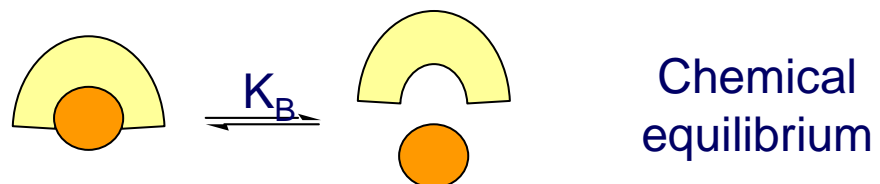
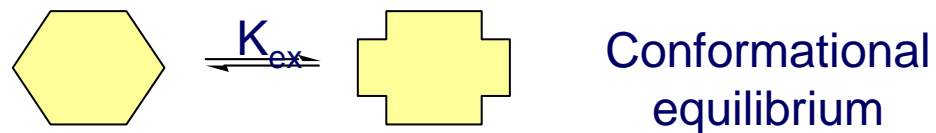
$$= \nu(\omega) + i\upsilon(\omega)$$

$$\nu(\omega) = \lambda M_0 \frac{R_2}{R_2^2 + (\Omega - \omega)^2}$$

$$\upsilon(\omega) = \lambda M_0 \frac{\Omega - \omega}{R_2^2 + (\Omega - \omega)^2}$$



# Chemical exchange complicates matters



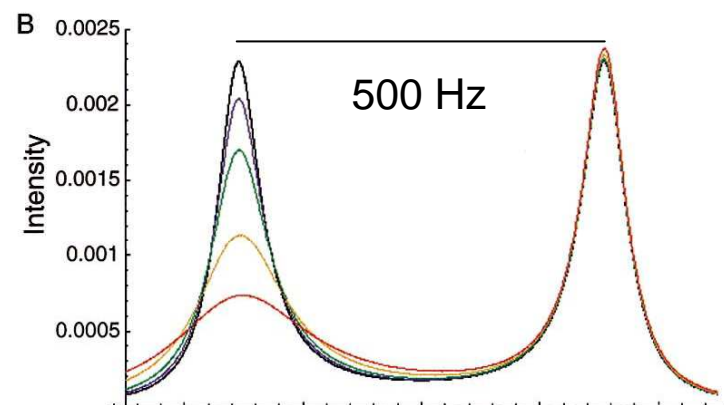
# Linewidth simulations for slow exchange interactions



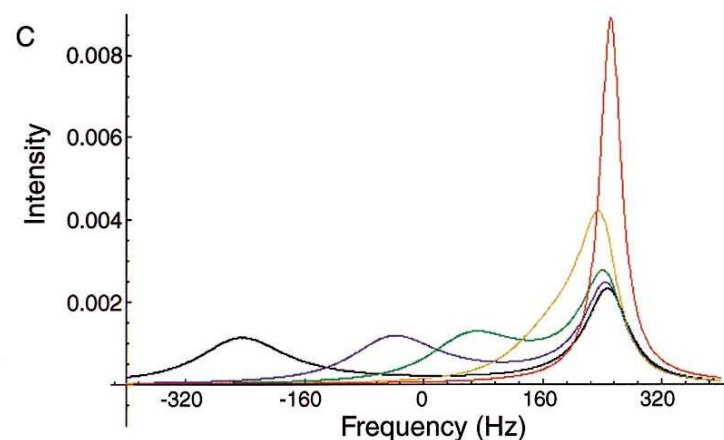
$$I(\omega) \sim \text{Re} \{W * A^{-1} * 1\}$$

$$A = i(\Omega - \omega E) + K + R$$

Changing  $R_2$  of the bound state: 500, 250, 100, 50 and 23  $\text{s}^{-1}$ . No chemical shift difference of free and bound state



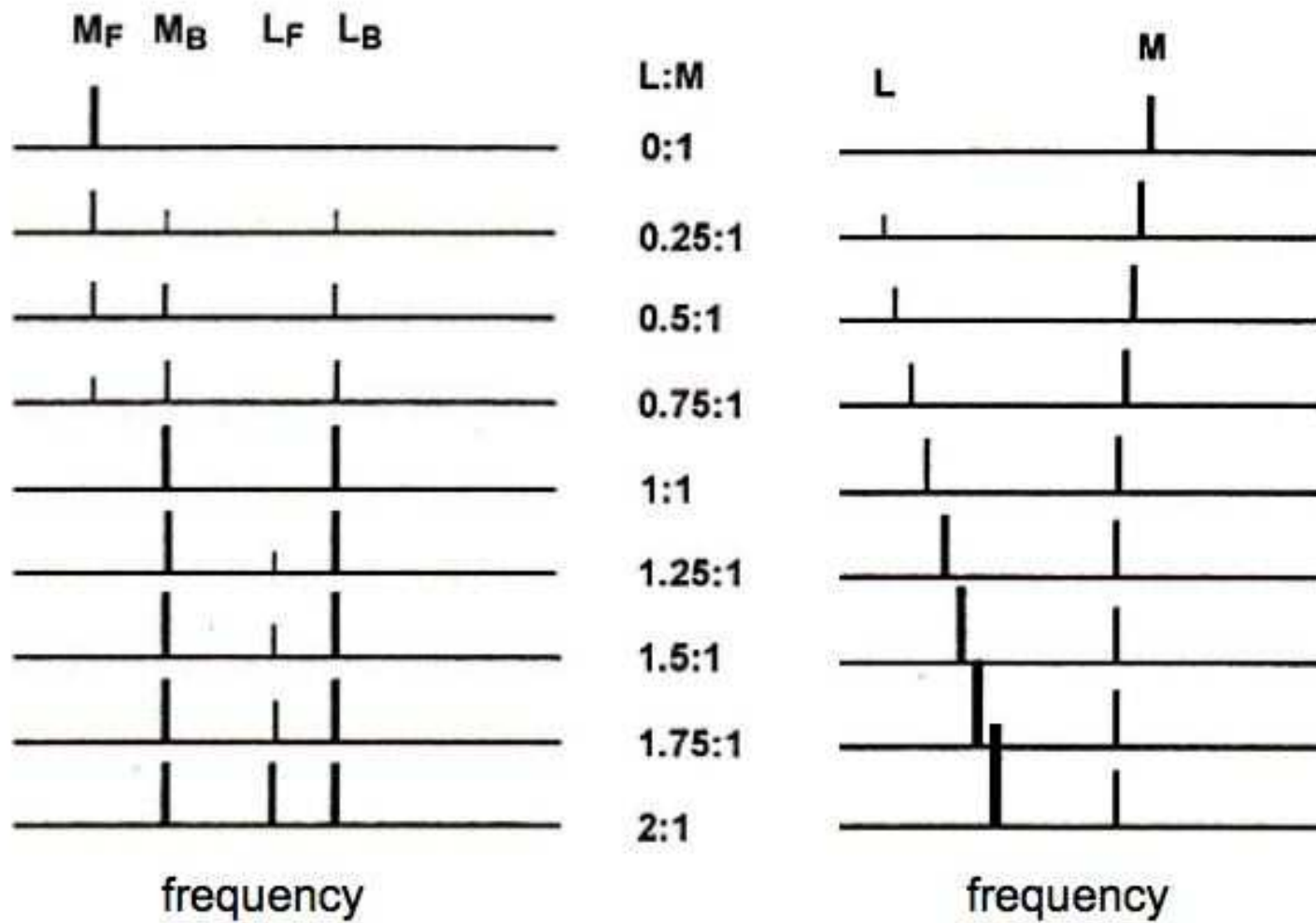
Same parameters used as above.  $R_2$  (free) is 23  $\text{s}^{-1}$  and  $k_{\text{off}} = 200 \text{ s}^{-1}$ . The fraction of free protein is 0.5.



$R_2$  (bound) is set to 250  $\text{s}^{-1}$  and chemical shifts are varied : 500, 250, 100, 50 and 23 Hz

Published in: Hiroshi Matsuo; Kylie J. Walters; Kenta Teruya; Takeyuki Tanaka; George T. Gassner; Stephen J. Lippard; Yoshimasa Kyogoku; Gerhard Wagner; *J. Am. Chem. Soc.* **1999**, 121, 9903-9904.

What type of exchange ?

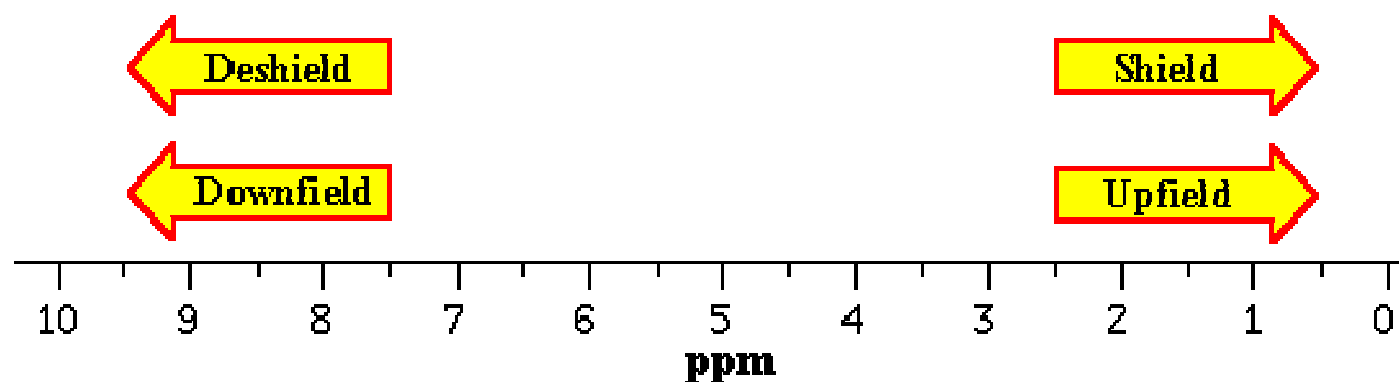




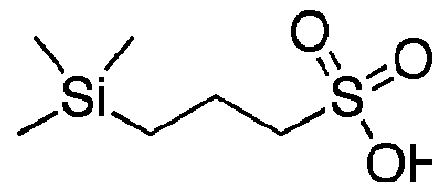
Mapping protein interactions:

Chemical shift as a measure of chemical environment :

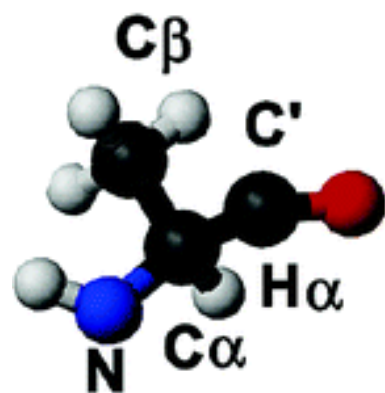
$$\delta = \frac{\text{difference in precession frequency between two nuclei}}{\text{operating frequency of the magnet}}$$



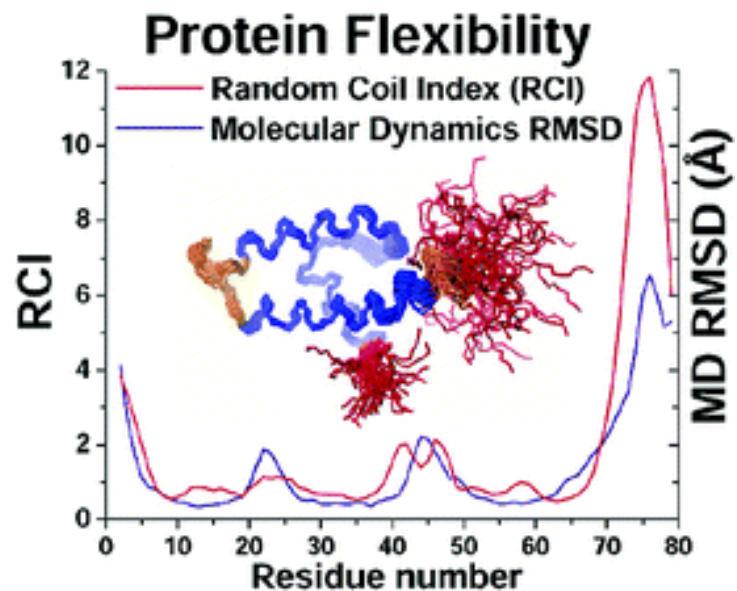
Reference against: 2,2-dimethyl-2-silapentane-5-sulfonic acid (DSS)



## Predicting protein chemical shifts via CSI

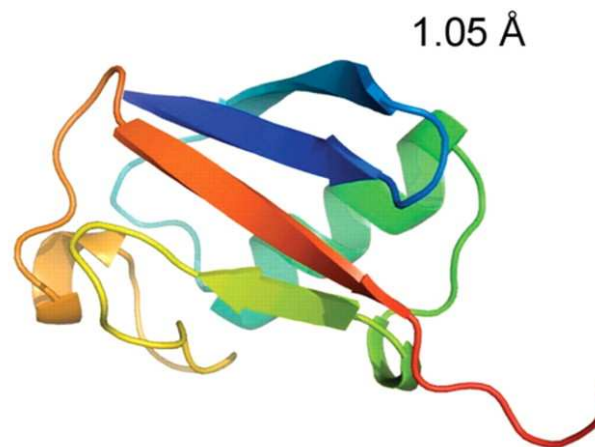
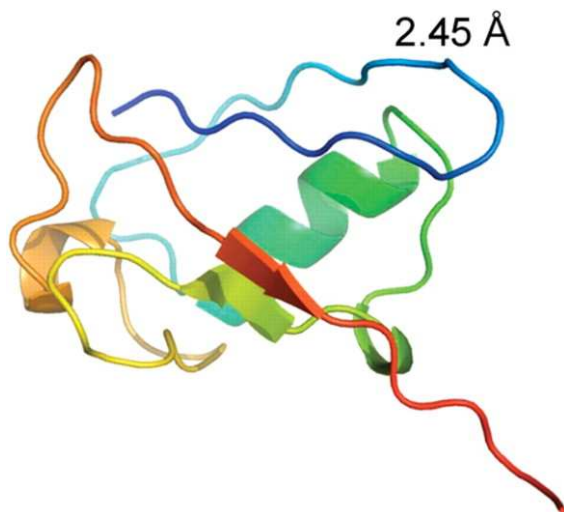


→  
**NMR**



Berjanskii & Wishart,  
Nature Protocols 1, - 683 - 688 (2006)

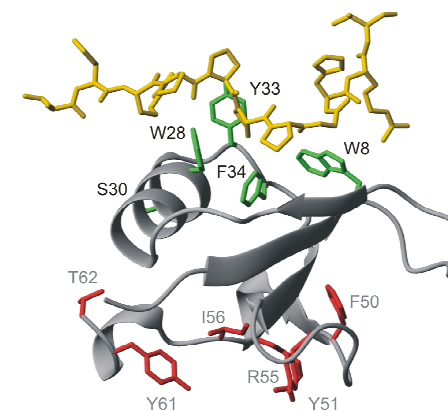
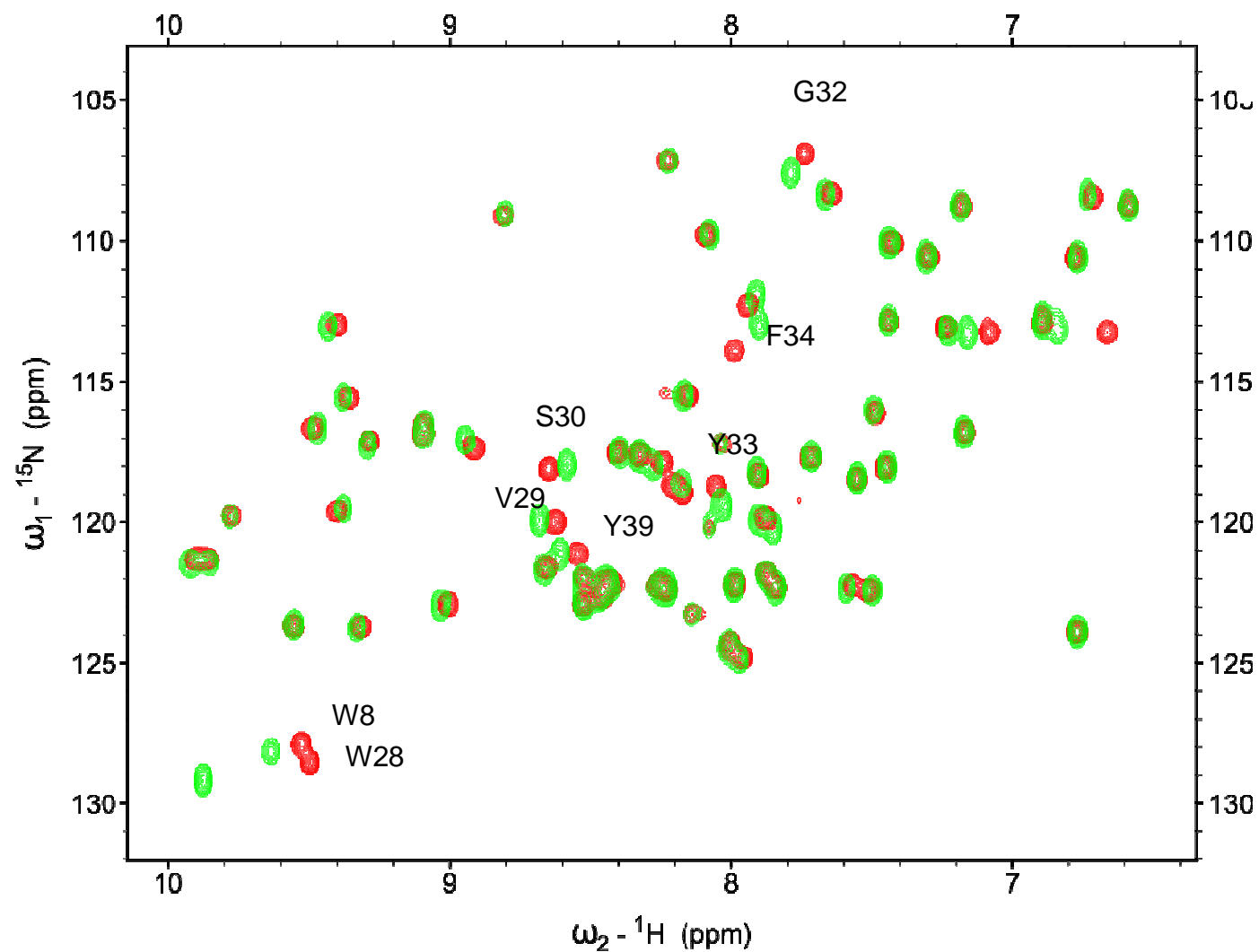
## Structure refinement via CSI



<http://www.cs23d.ca/>

# Chemical shift changes : a single non-disruptive mutation

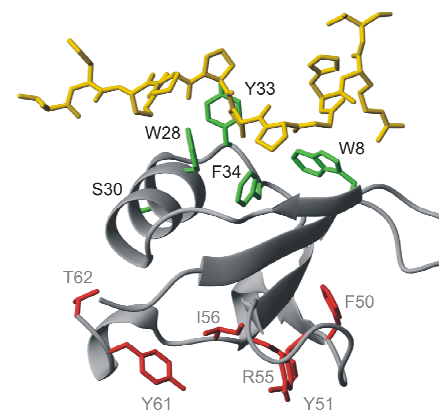
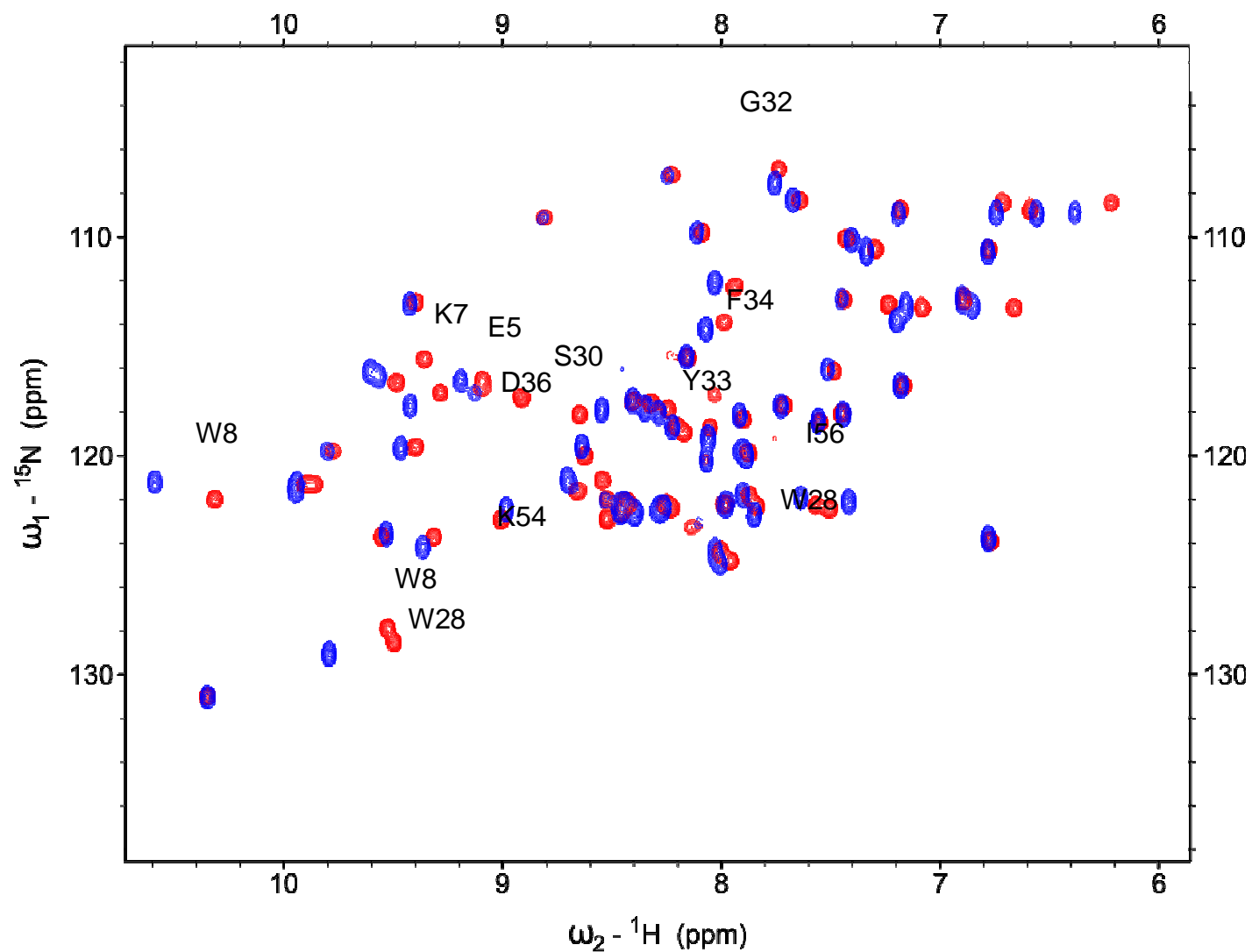
Wt(rot)/Y33A(grün)



GYF domain

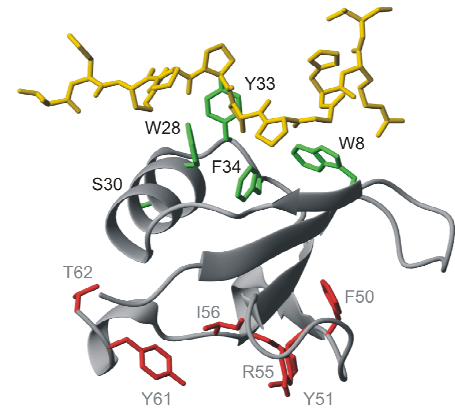
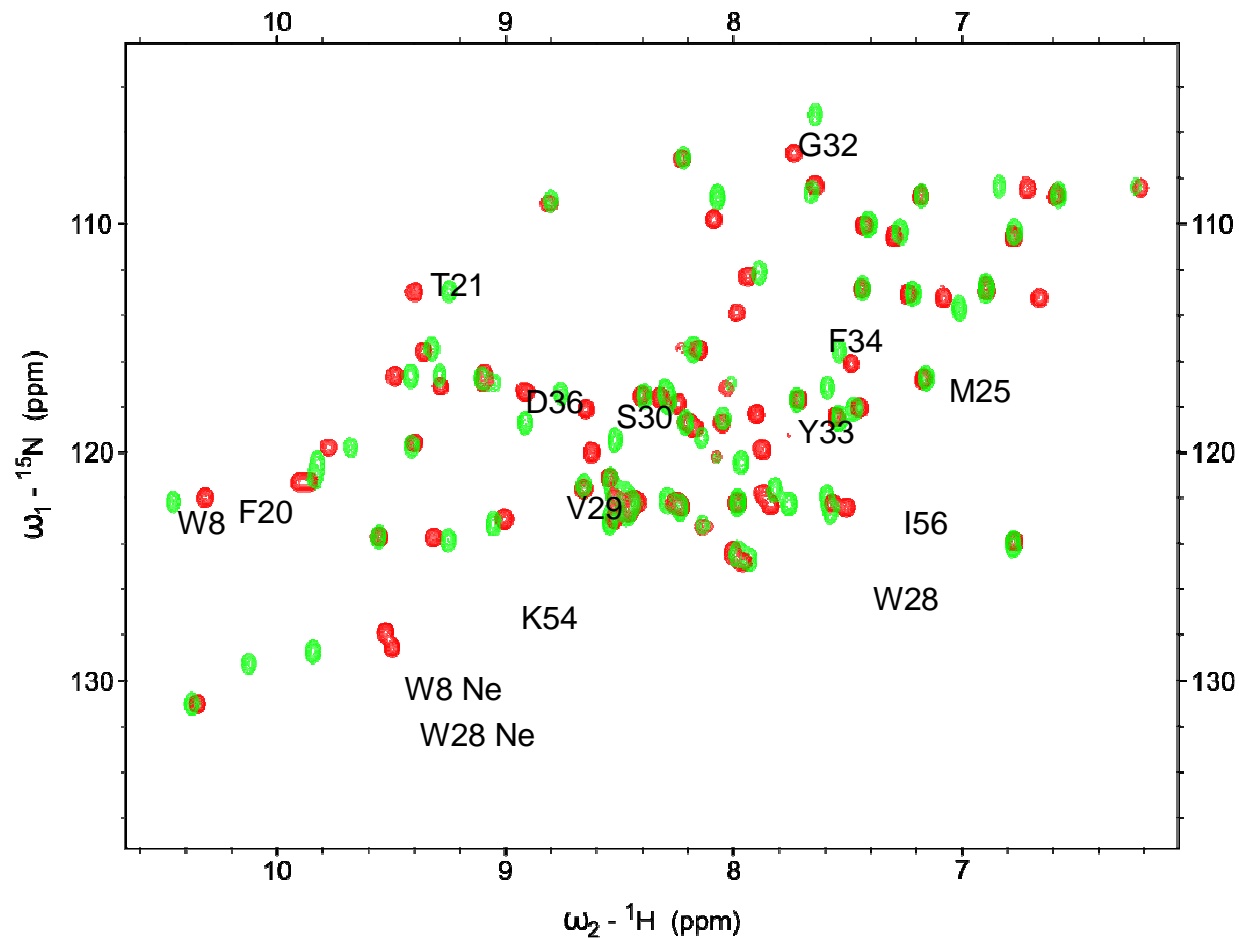
# Chemical shift changes : two non-disruptive mutations

Wt(rot)/Y33AW8R(blau)



Chemical shift changes: Fast exchange:  
GYF binding to spliceosomal SmB

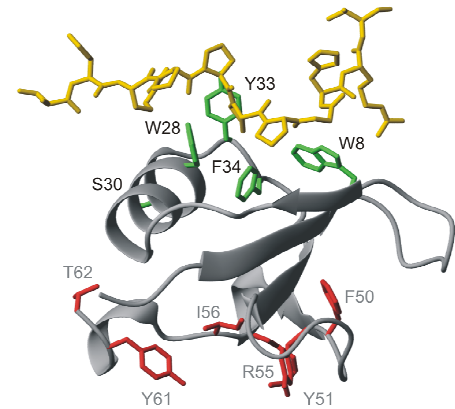
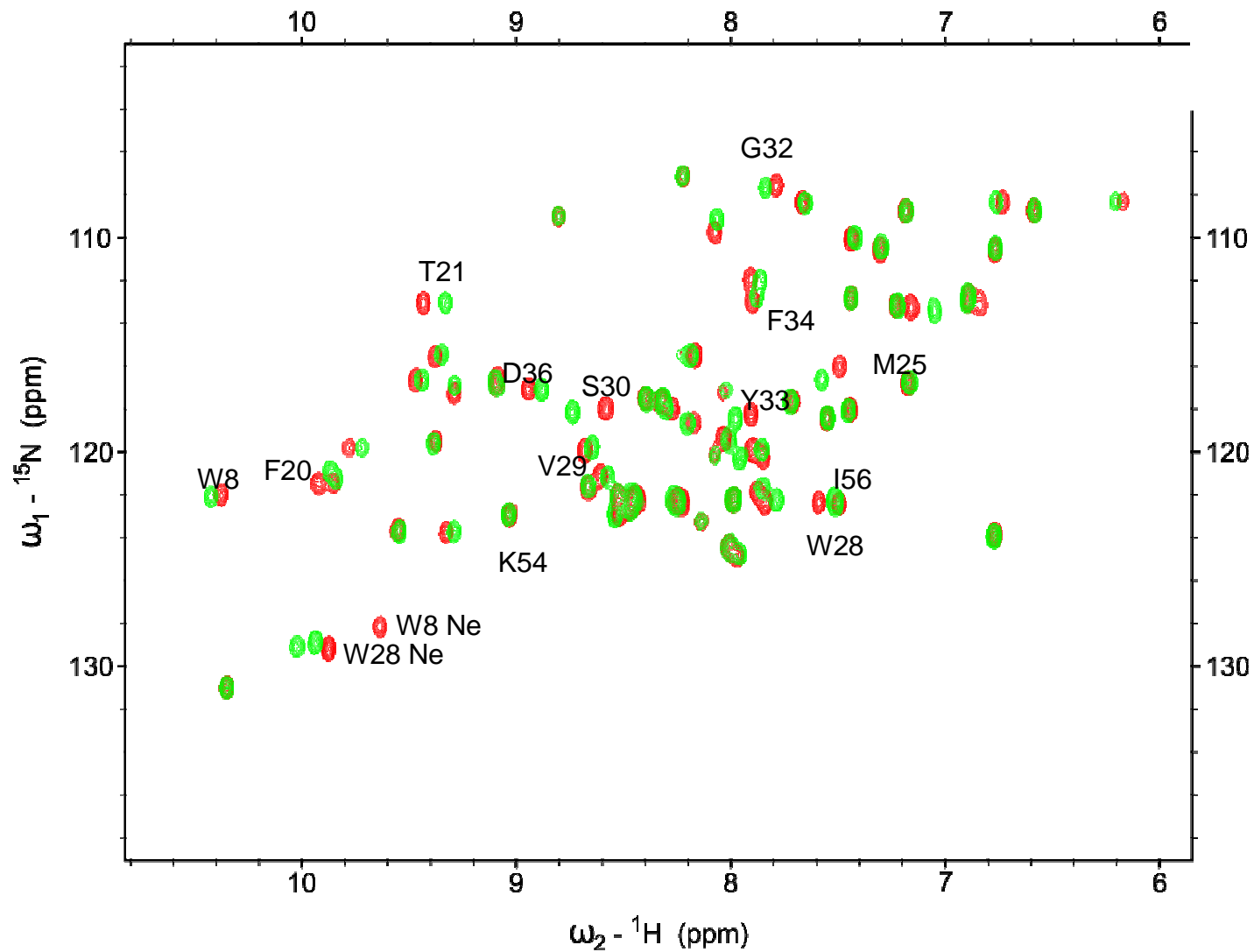
Wt(rot)/Wt\_SmB(grün)



$$[\text{PL}] = 1/2(K_D + [\text{P}]_0 + [\text{L}]_0) - \sqrt{1/4(K_D + [\text{P}]_0 + [\text{L}]_0)^2 - [\text{L}]_0 [\text{P}]_0}$$

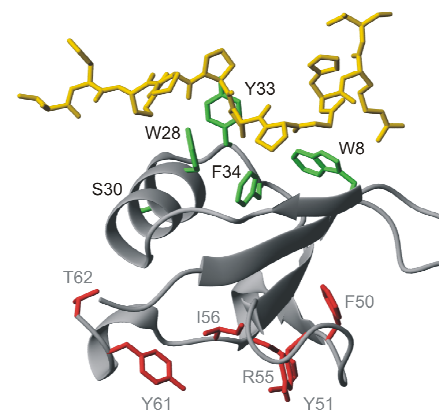
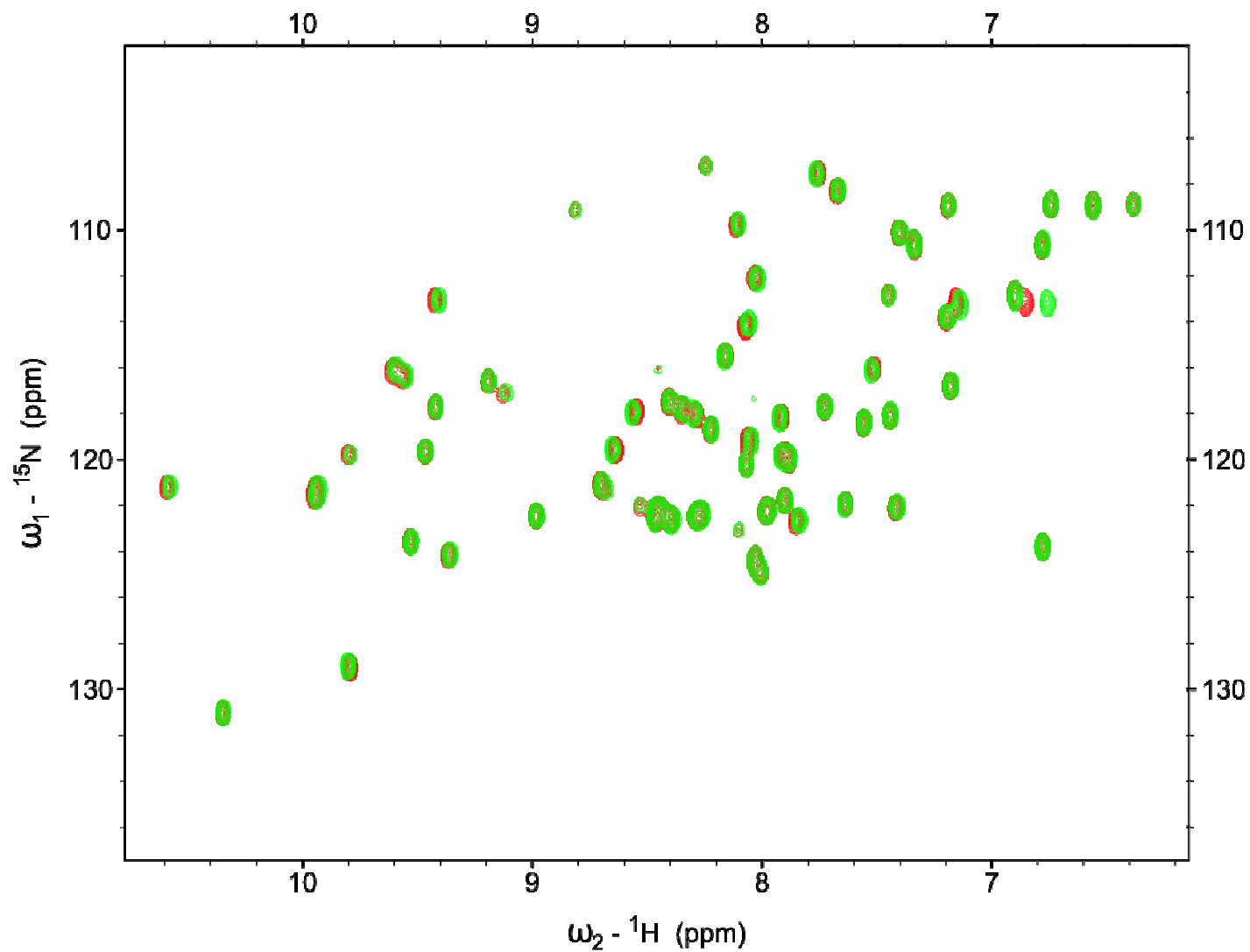
# Binding of the single-site mutant

Y33A(rot)/Y33A\_SmB(grün)

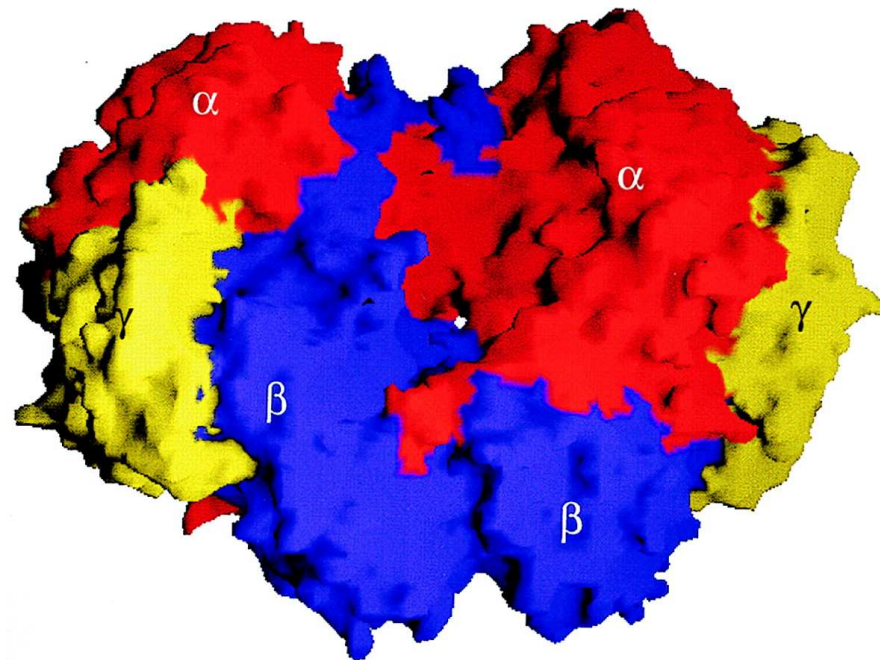
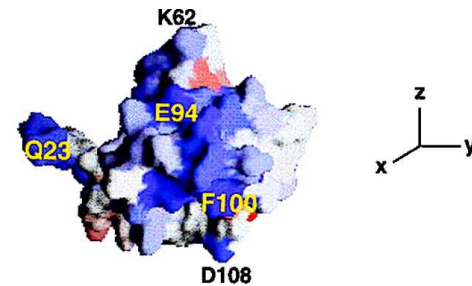
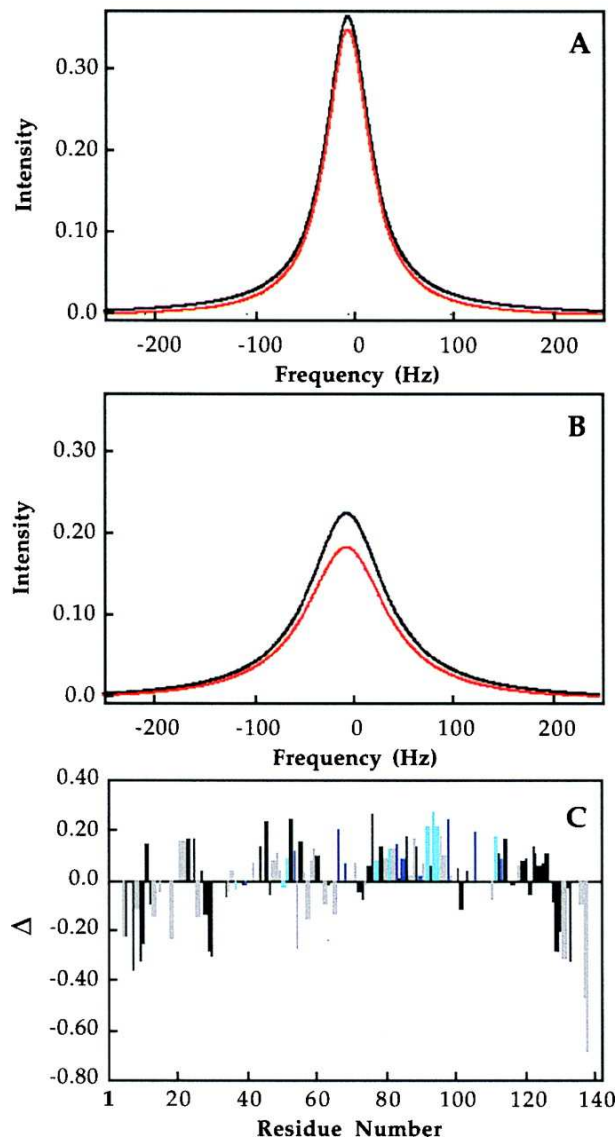


# (Non-)Binding of the double mutant

Y33AW8R(rot)/Y33AW8R\_SmB(grün)



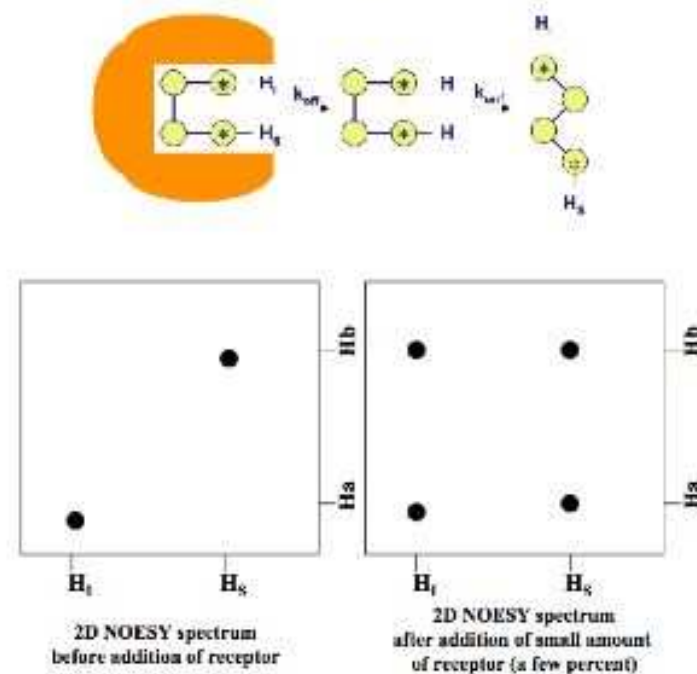
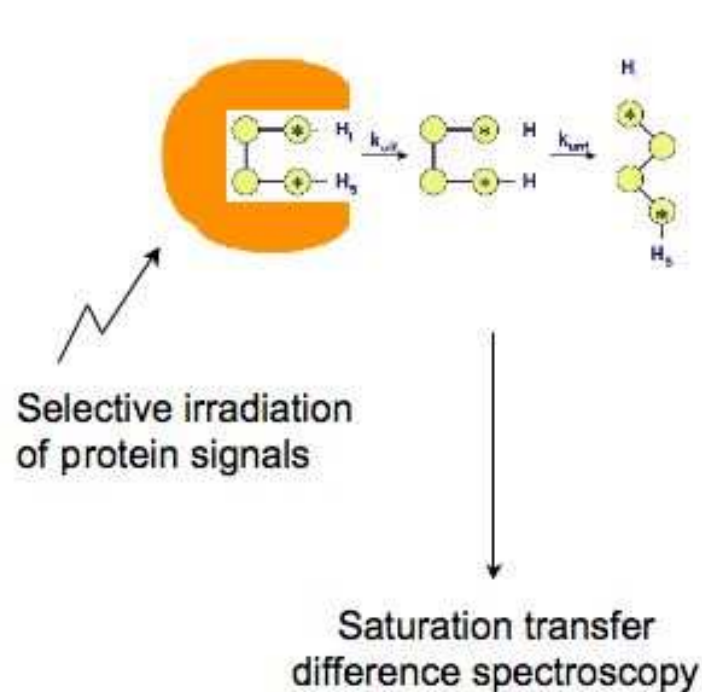
# Slow exchange: Linewidth analysis can be used to map binding sites



Walters et al., PNAS 1999, 96, 7877-7882

$k_{\text{off}}$  values of 3.2 s<sup>-1</sup> (A) or 25.6 s<sup>-1</sup> (B) for chemical shift differences of 0 Hz (black) and 500 Hz (red). R 1, R 2, and a are 23 Hz, 250 Hz, and 0.8, respectively

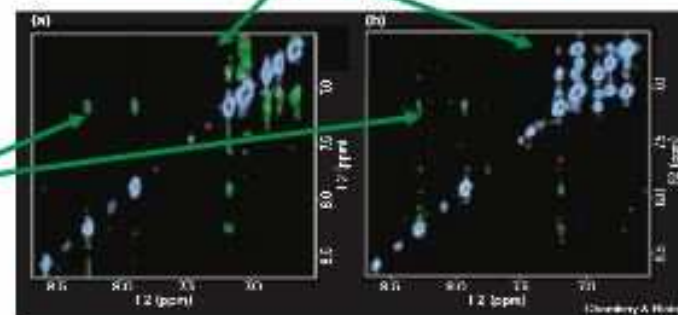
# Transferred NOEs for determination of bound ligand structures



2D NOESY spectra  
Positive peaks - cyan  
Negative peaks - green

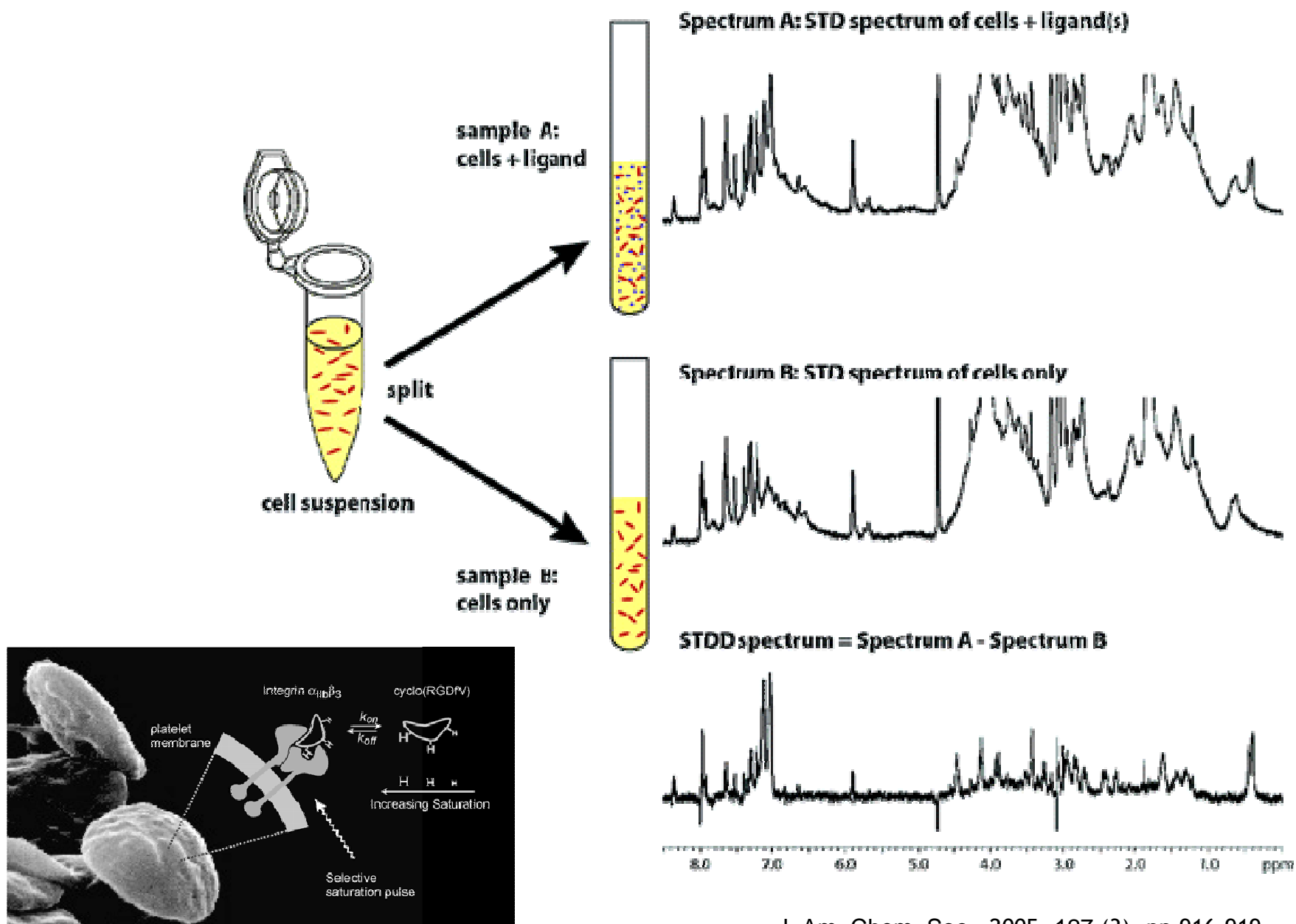
No change in sign, no binding

Change in sign of cross peak indicates binding



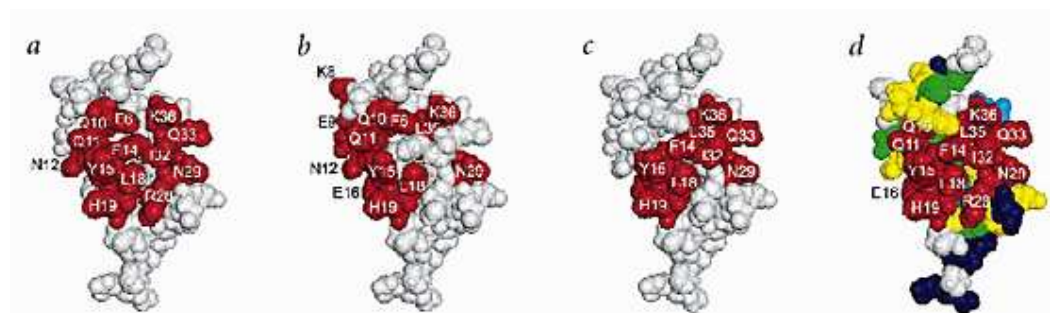
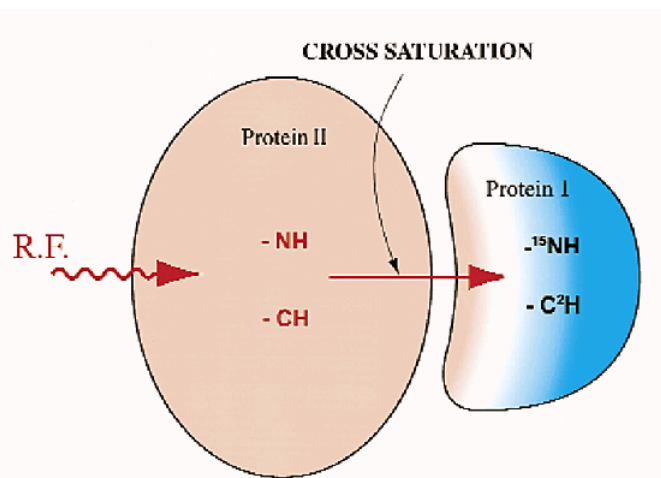
Adopted from Mark Girvin,  
Albert-Einstein College, NY

# STD-NMR can be used to observe binding in complex mixtures

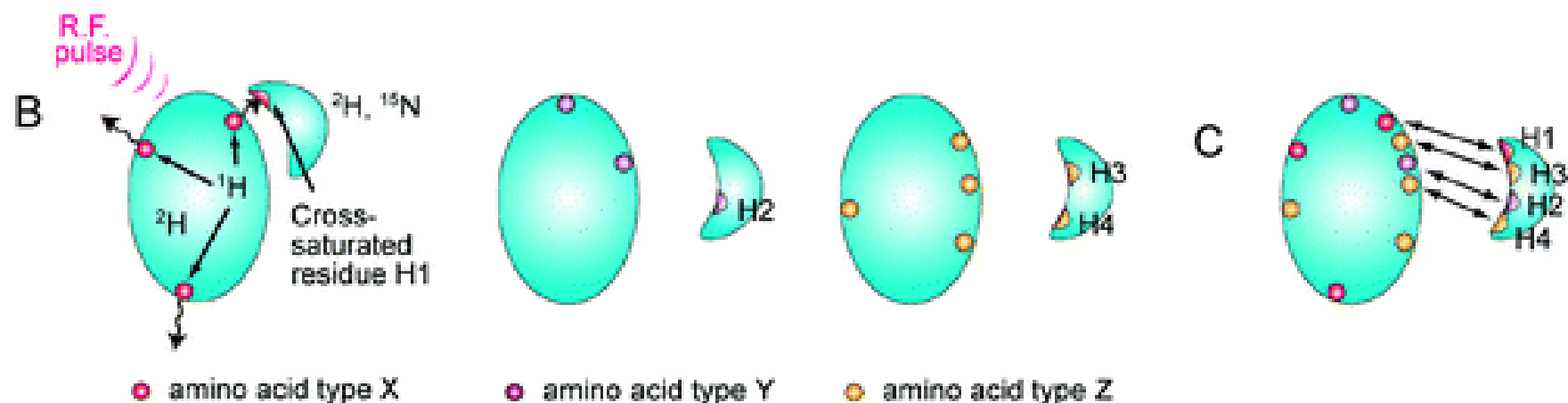


# Cross saturation: detection of $^{15}\text{NH}$ groups of a deuterated acceptor protein

Takahashi et al., Nat. Struct. Biol.(2000)

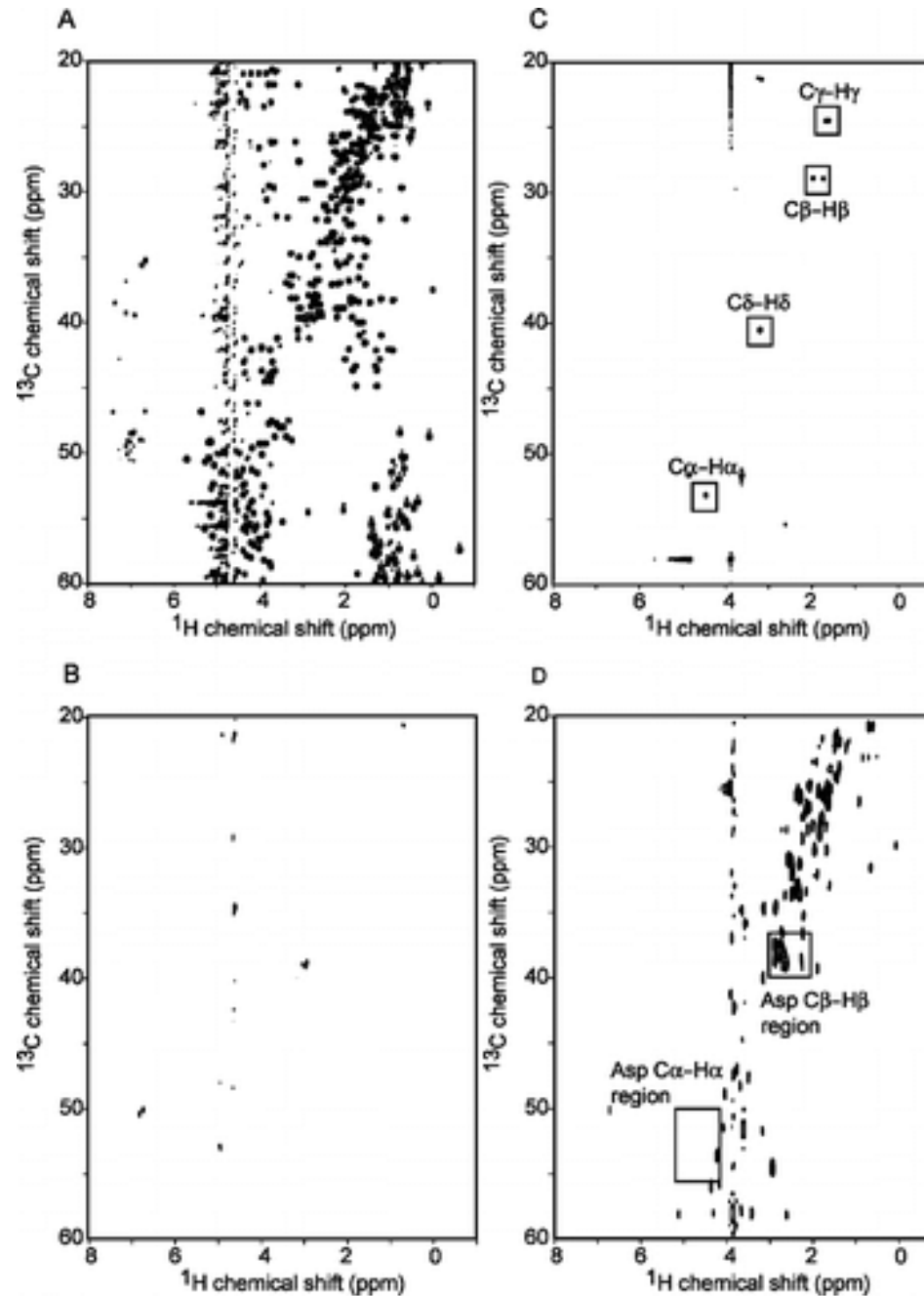


## Variant: Selective protonation of an otherwise deuterated donor protein



Igarashi et al., JACS 2008

# Selective protonation of amino acids with different efficiencies

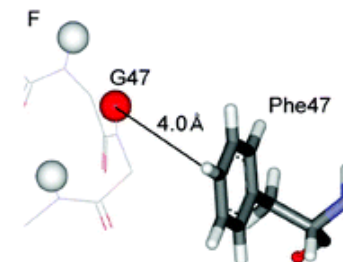
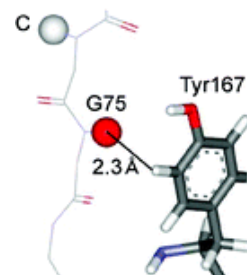
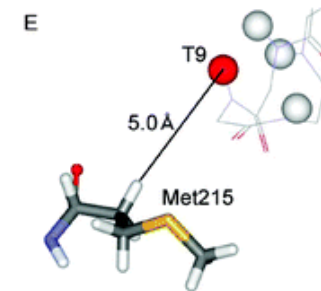
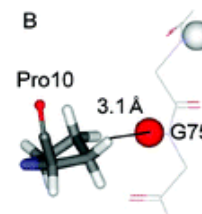
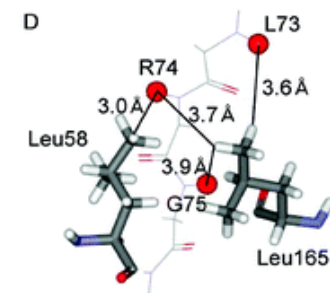
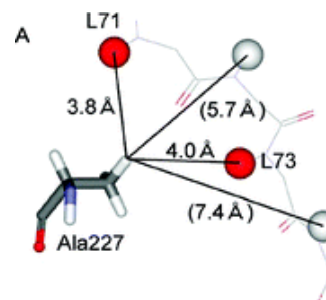
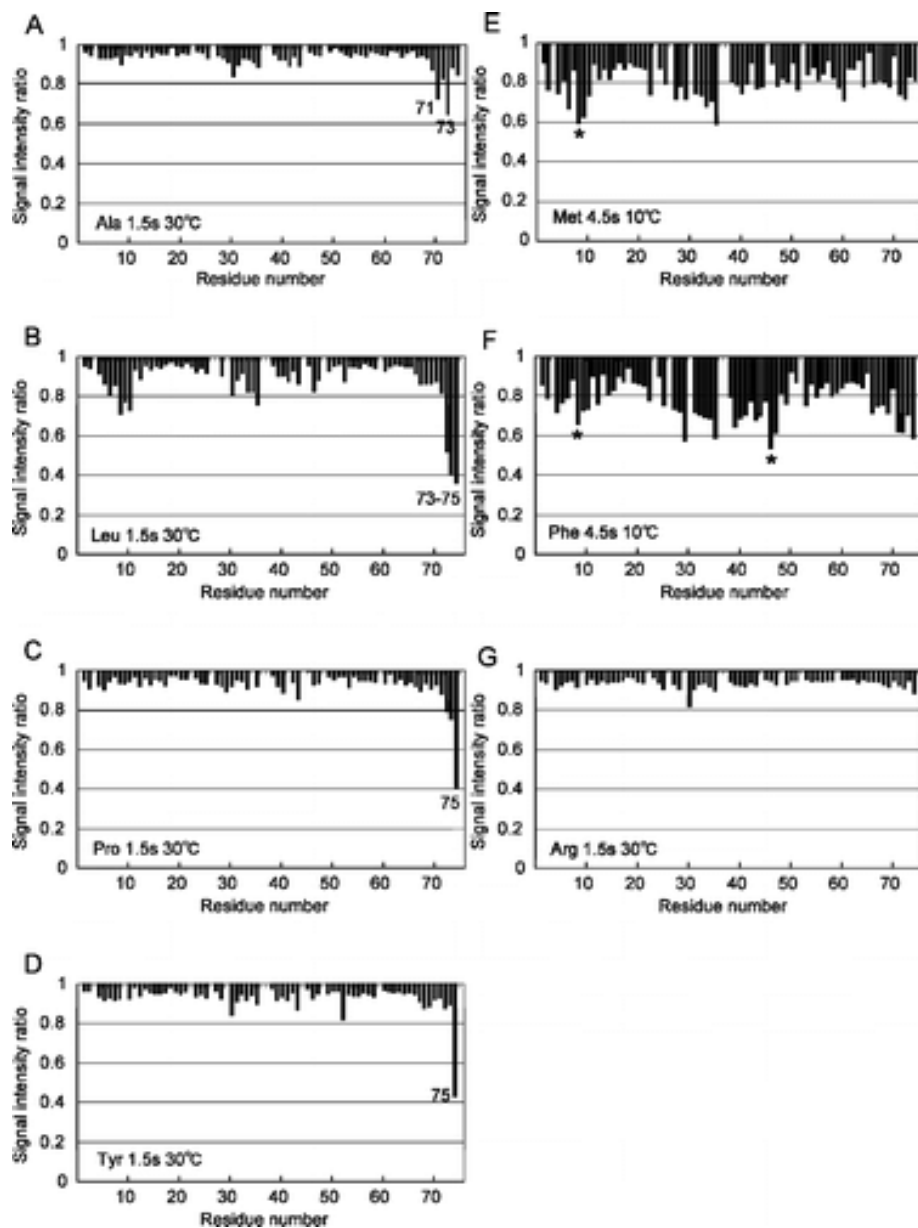


Arginine

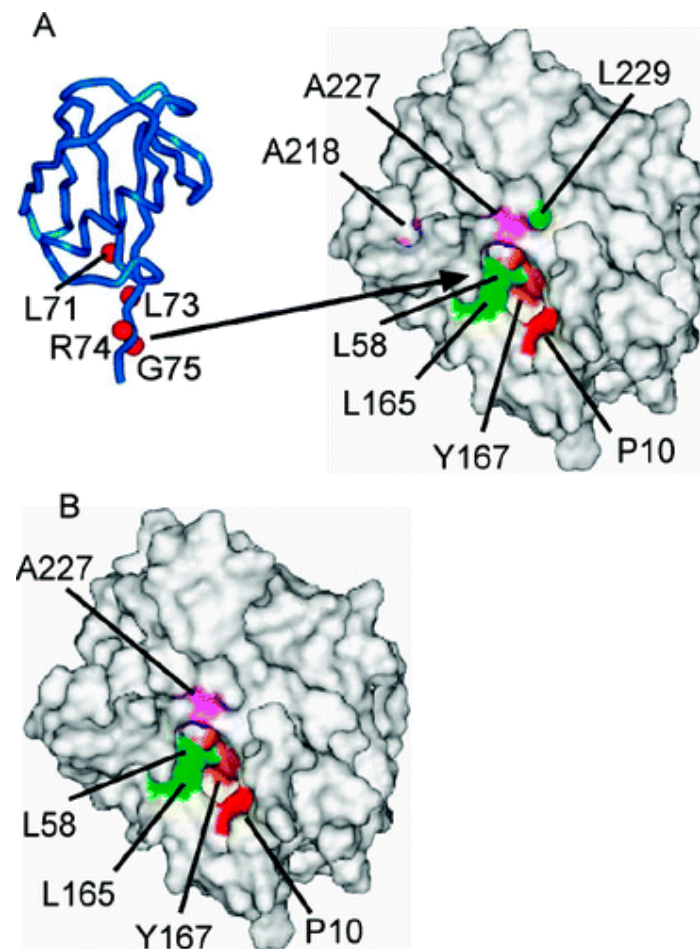
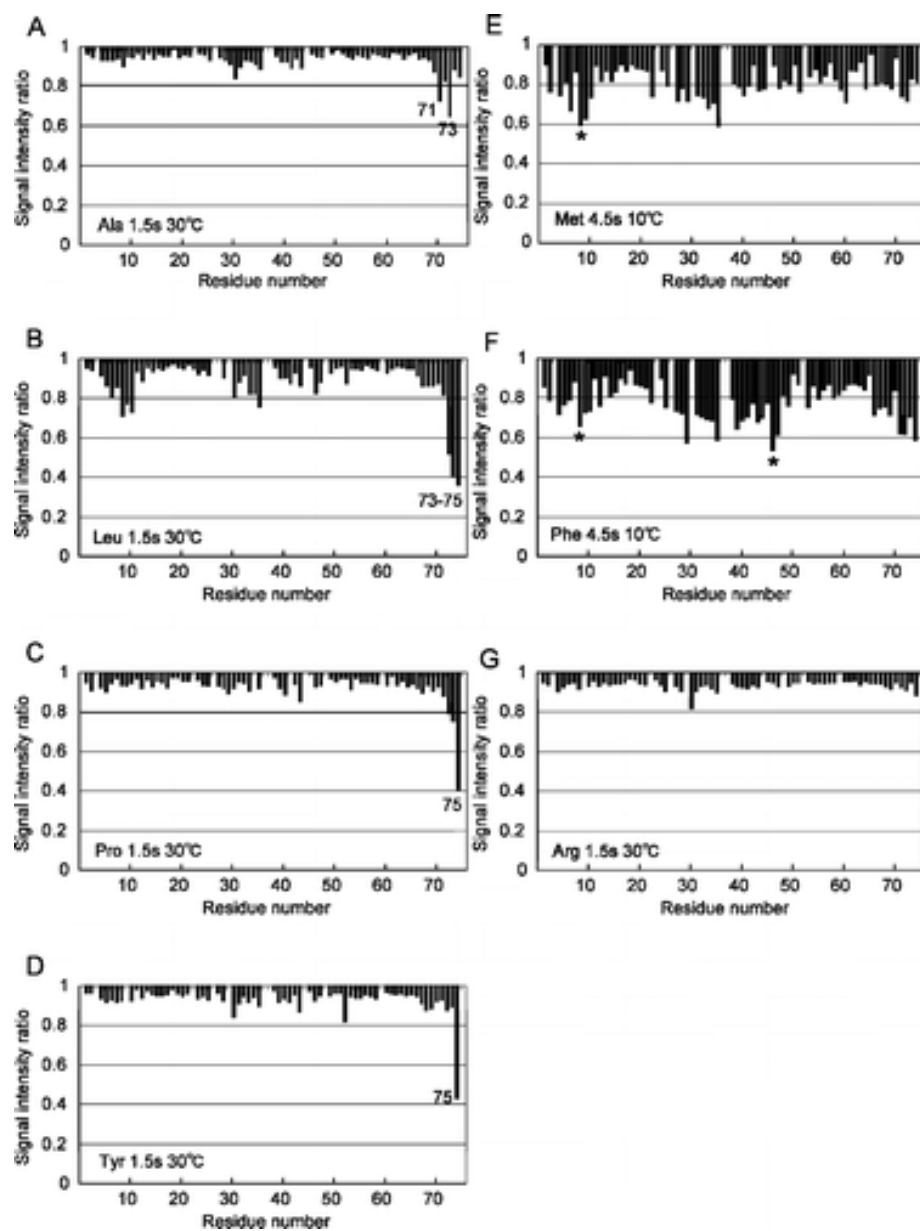
Feasible for: Ala, Arg, Cys, Gly, His, Ile, Leu, Lys, Met, Phe, Pro, Trp, and Tyr

Asparate

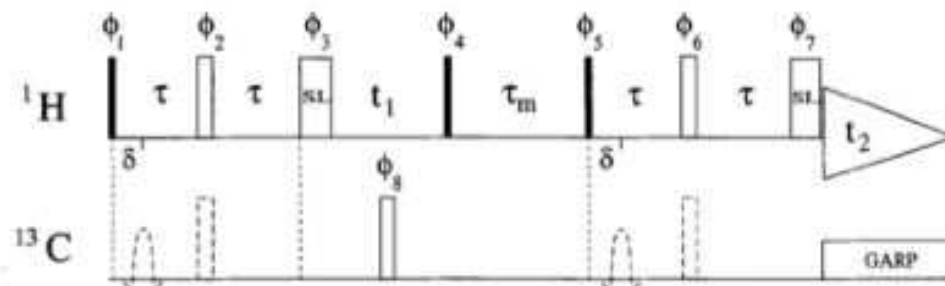
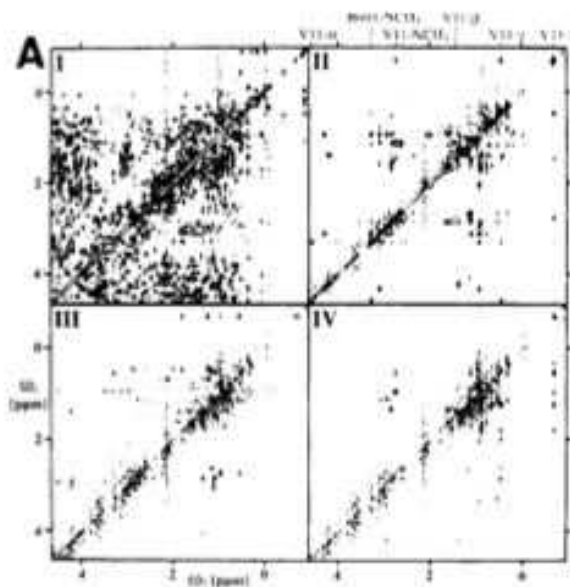
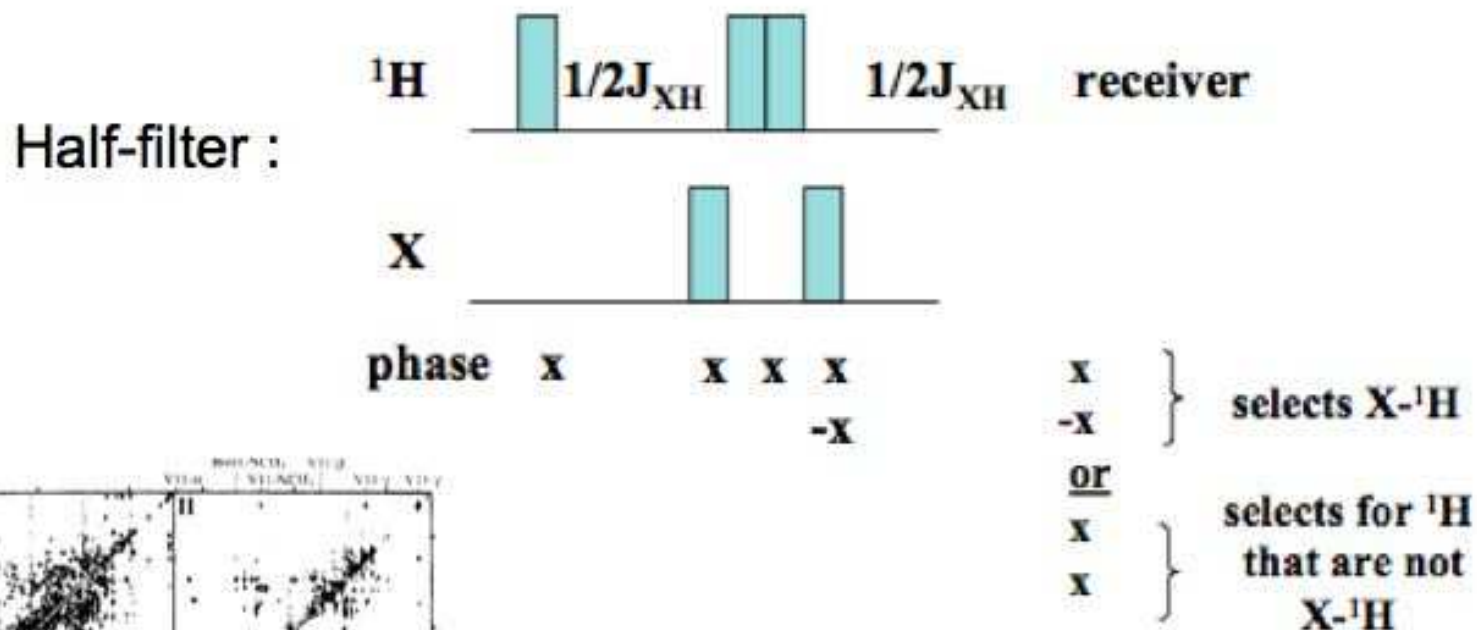
# Identification of donor residues close in space to affected acceptor amides



# Identification of donor and acceptor interfaces



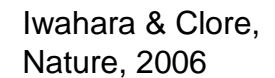
## Determining the structure of protein:ligand complexes



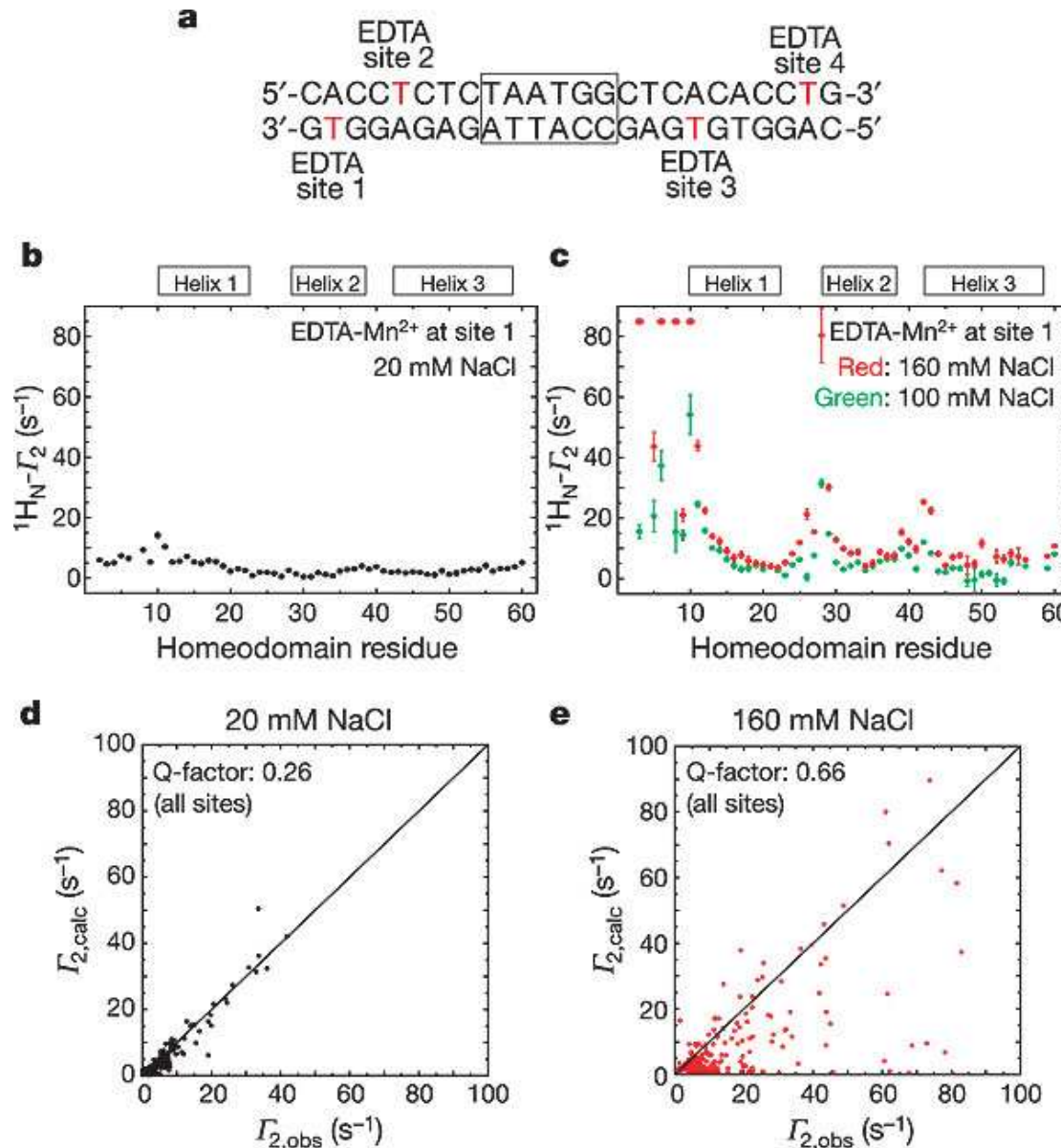
Wider et al., JACS, 1990

Folmer et al., J Biomol. NMR 1995

..to be continued in later sessions



At higher salt concentrations,  $T_2$  relaxation data cannot be explained by the specific complex

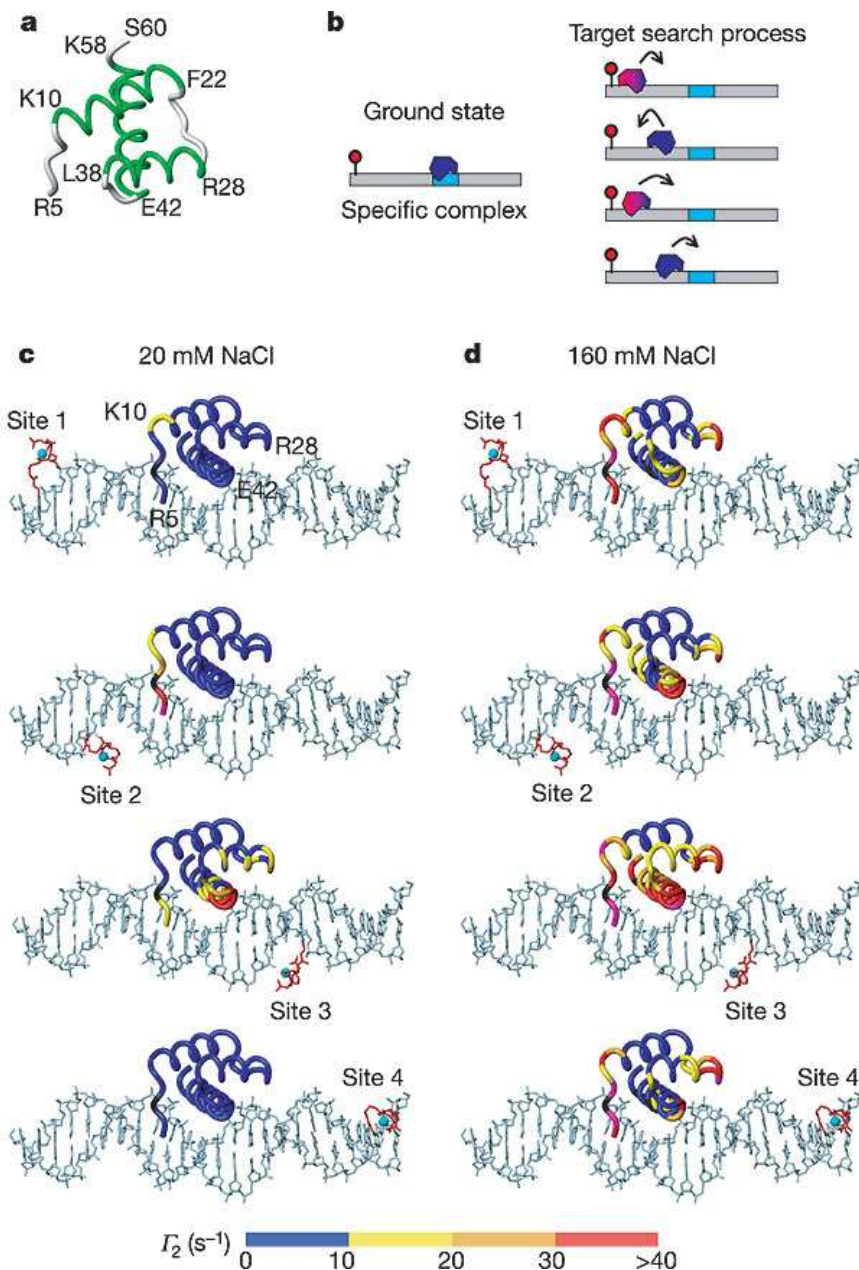


Model system:  
Homeodomain of human  
HOXD9 in complex with a  
24-base-pair DNA duplex

Incorporation of conjugated  
deoxy(d)T-EDTA-Mn<sup>2+</sup> into  
the DNA

$$Q = \left( \frac{\sum \{T_2^{obs}(i) - T_2^{calc}(i)\}}{\sum T_2^{obs}(i)^2} \right)$$

## Low-affine interactions likely contribute to formation of the specific complex



$^{15}\text{N}$ - $^1\text{H}$ -correlation spectra indicate that the structure of the specific complex does not change significantly when going from 20 mM to 160 mM salt!

Structural representations of the measured intermolecular PRE profiles.

At 20mM NaCl, the data is compatible with the structure of the complex bound to the specific site.

At 160 mM NaCl the observed PRE are interpreted as footprints of minor species that are in rapid exchange with the specific complex.