



# **NMR-lecture April 6th, 2009, FMP Berlin**

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## **Outline:**

- **Basic understandings:**
  - Relaxation
  - Chemical exchange
- **Mapping interactions:**
  - Chemical shift mapping (fast exchange)
  - Linewidth analysis (slow exchange)
  - Cross saturation transfer
  - Transfer NOE/STD NMR
  - Half filter experiments/isotope labeling

# Monitoring protein:protein interactions: Capitalizing on chemical shift and relaxation rate changes

In the absence of an applied rf field, the Bloch equations are defined as:

$$\frac{dM_x(t)}{dt} = -\Omega M_y(t) - R_2 M_x(t)$$

In the case of chemical exchange it is :

$$\frac{dM_y(t)}{dt} = -\Omega M_x(t) - R_2 M_y(t)$$

$$\frac{dM_{xy}(t)}{dt} = -(\Omega - R_2 + K)M_{xy}(t)$$

$$\frac{dM_z(t)}{dt} = -\Omega\{M_z(t) - M_0\}$$

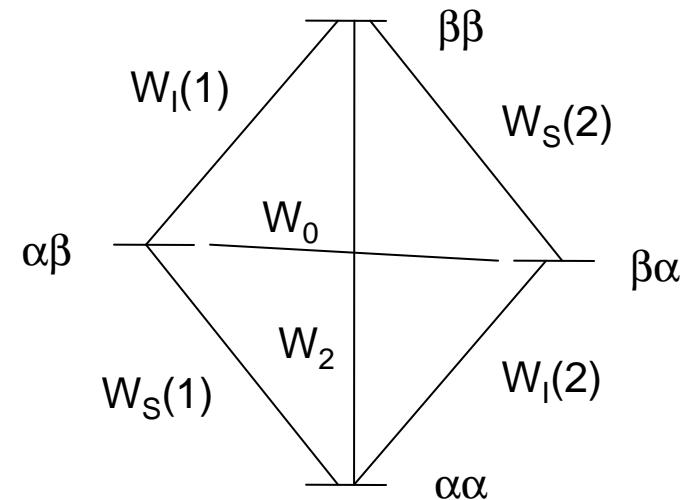


$$\frac{dM_z(t)}{dt} = -(\Omega + K)\Delta M_z(t)$$

Formal solution :  $\Delta M_z(t) = e^{-Rt} \Delta M_z(0)$

$$R = \begin{bmatrix} \rho_I & \sigma_{IS} \\ \sigma_{IS} & \rho_S \end{bmatrix}$$

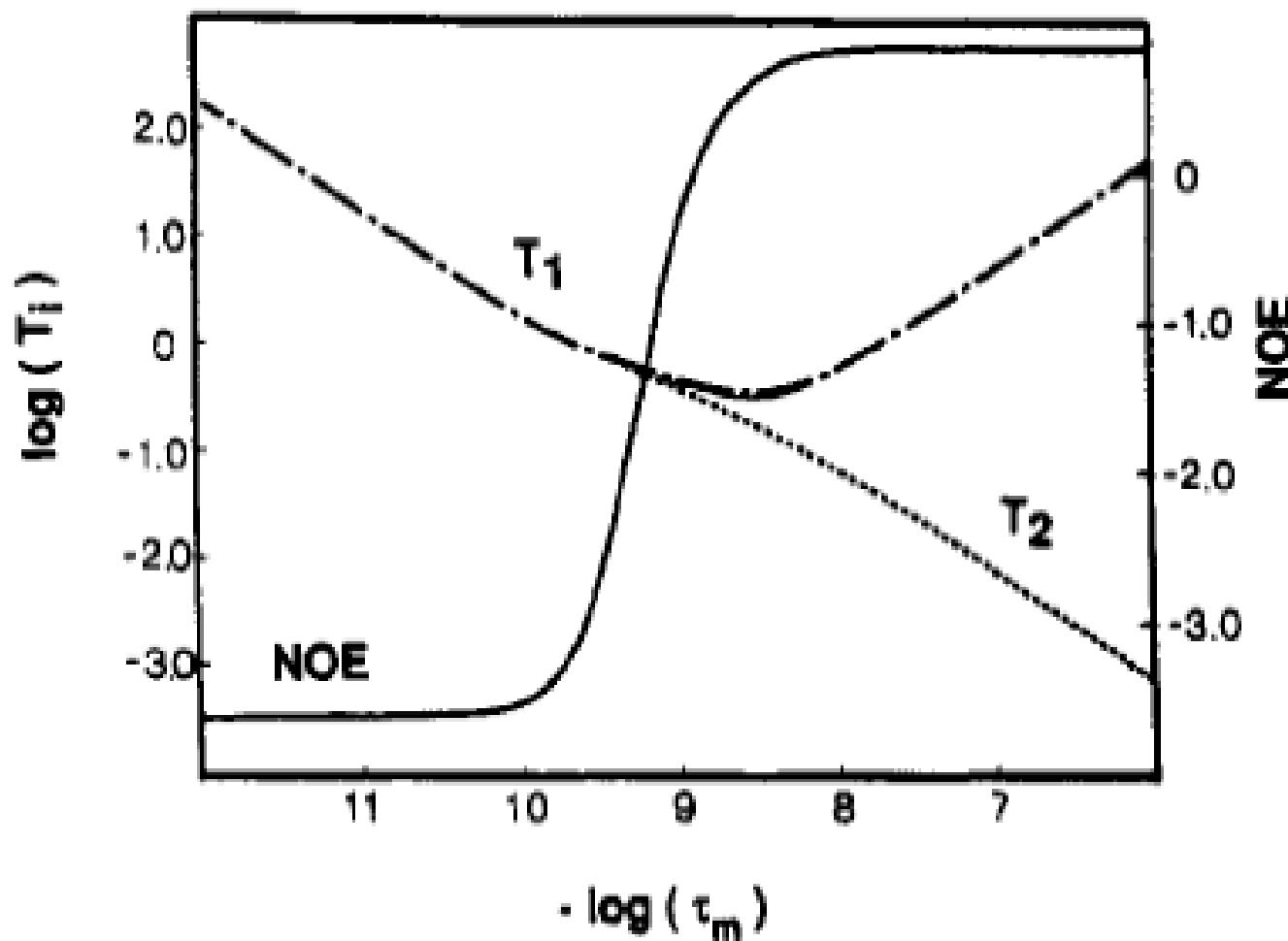
## Transitions between states in a two-spin system



$$\sigma = W_2 - W_0$$

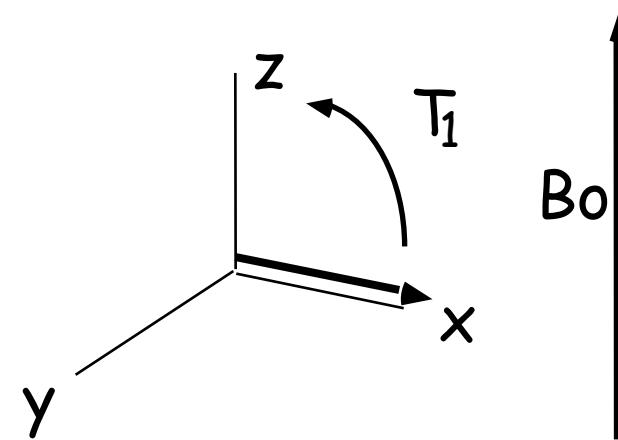
$$\sigma_{ij} \sim 1/r_{ij}^6 * [6J(2\omega_0) - J(0)]$$

Relaxation times depend on the overall tumbling time of molecules which is proportional to molecular weight

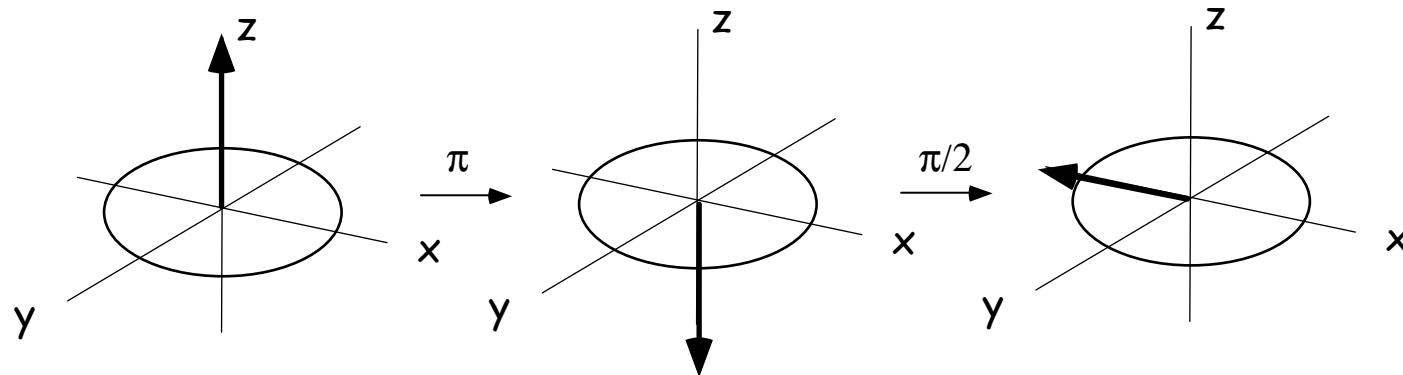


$$\tau_c = \frac{4\pi\eta r^3}{3kT}$$

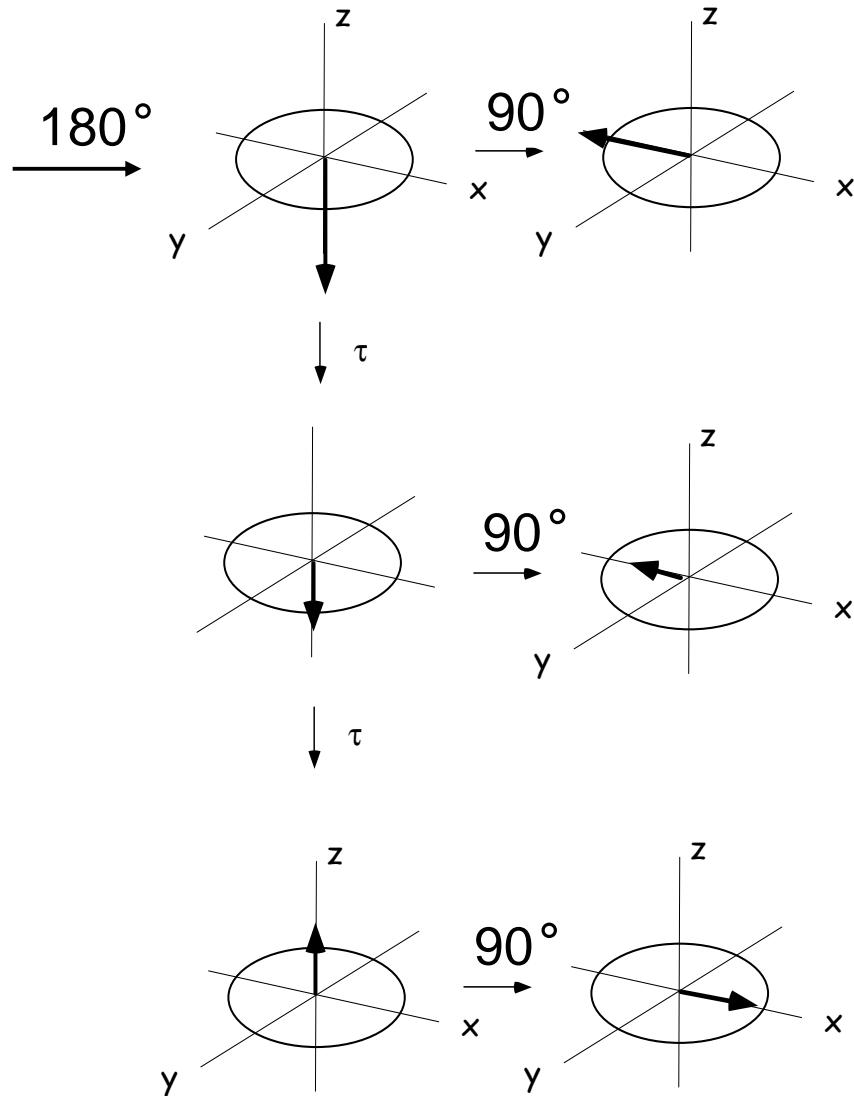
## T<sub>1</sub> relaxation



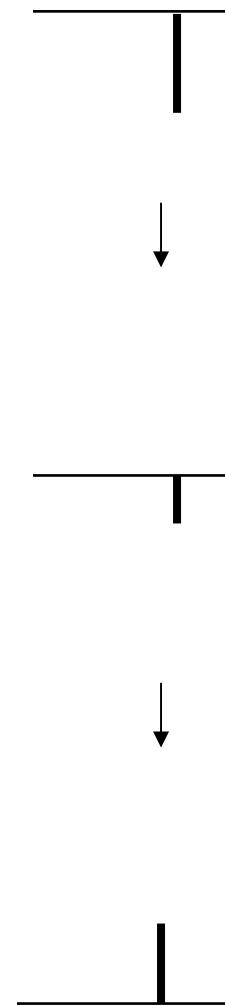
Measuring T1 from inversion recovery pulse sequence



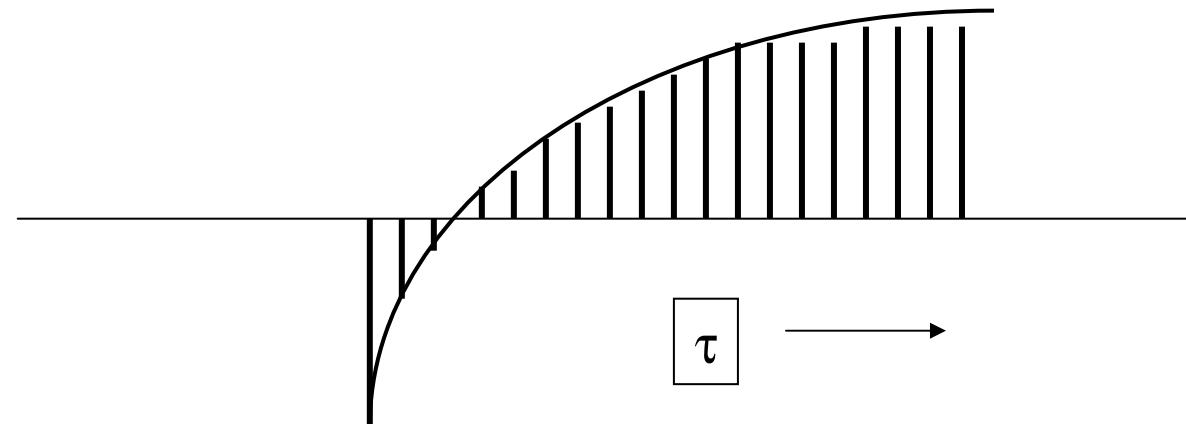
# Measuring T1 relaxation times



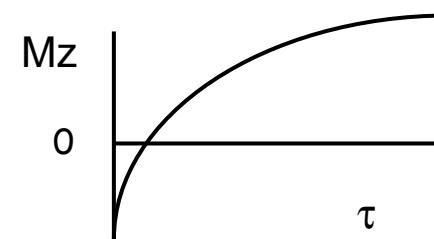
## Inversion Recovery



# Inversion Recovery - Measure NMR Intensity as a function of the delay time $\tau$ and fit to an exponential function



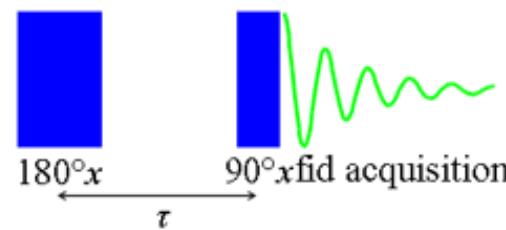
$$M_z = M_0 (1 - 2e^{-\tau/T_1})$$



## Inversion recovery pulse sequence for measuring $T_1$

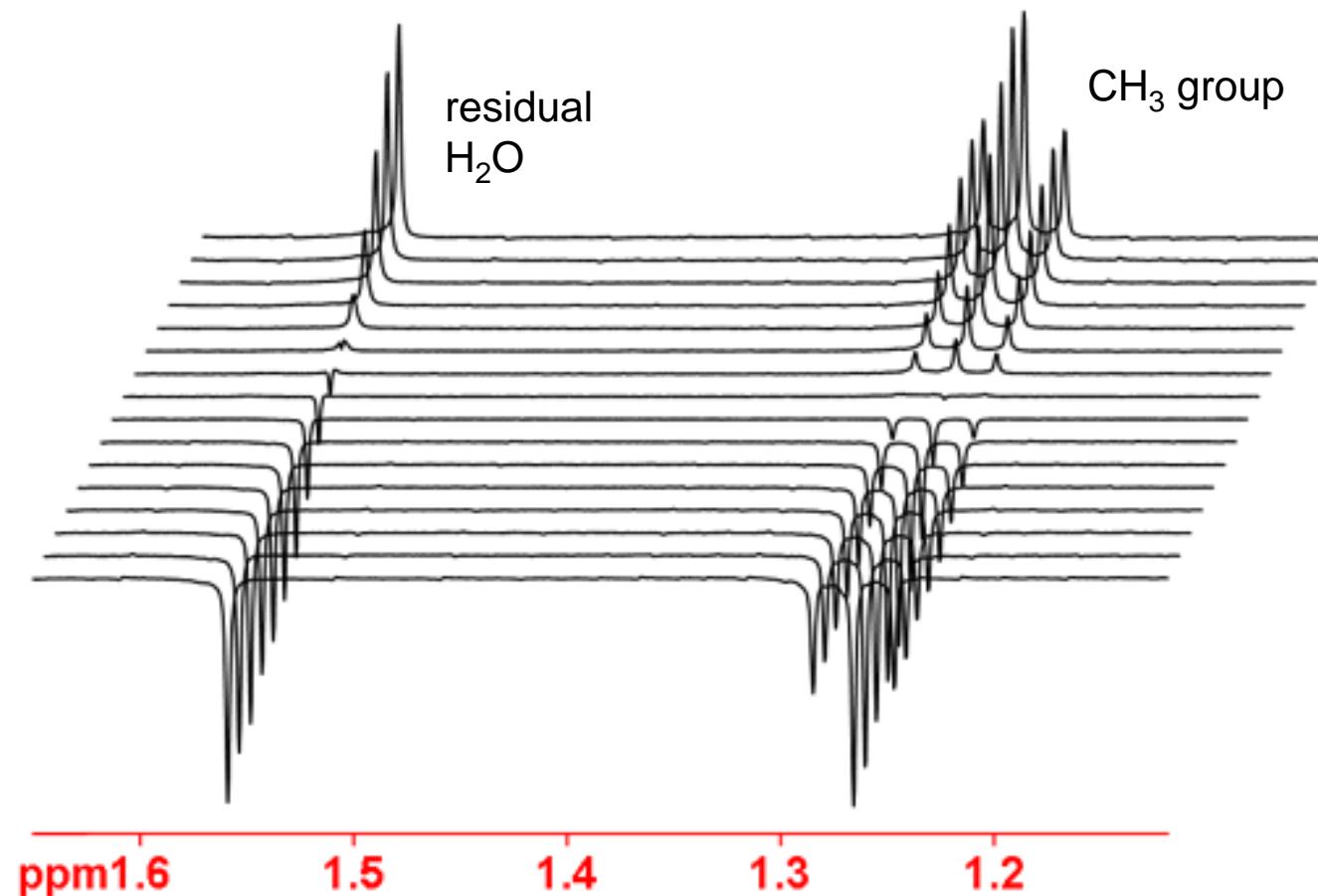
observation  
channel

relaxation time  
of at least  $5T_1$



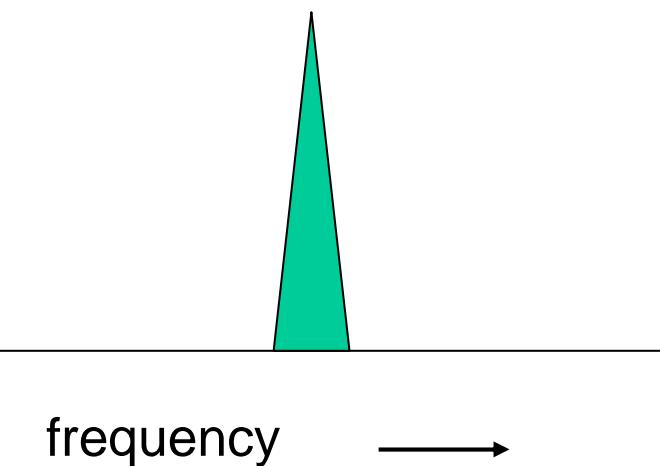
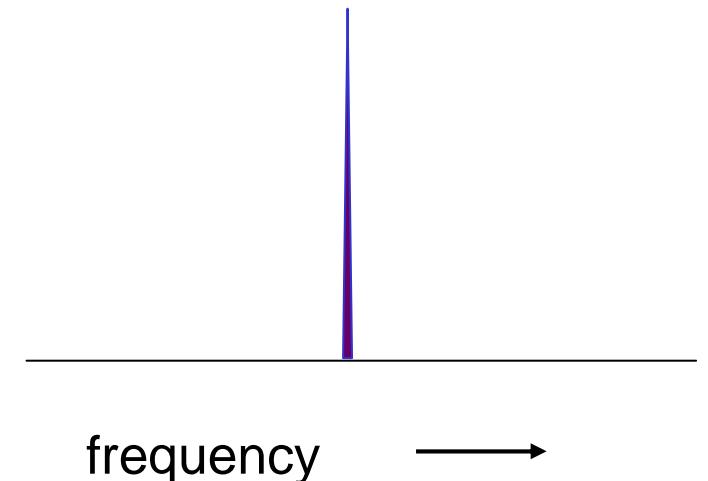
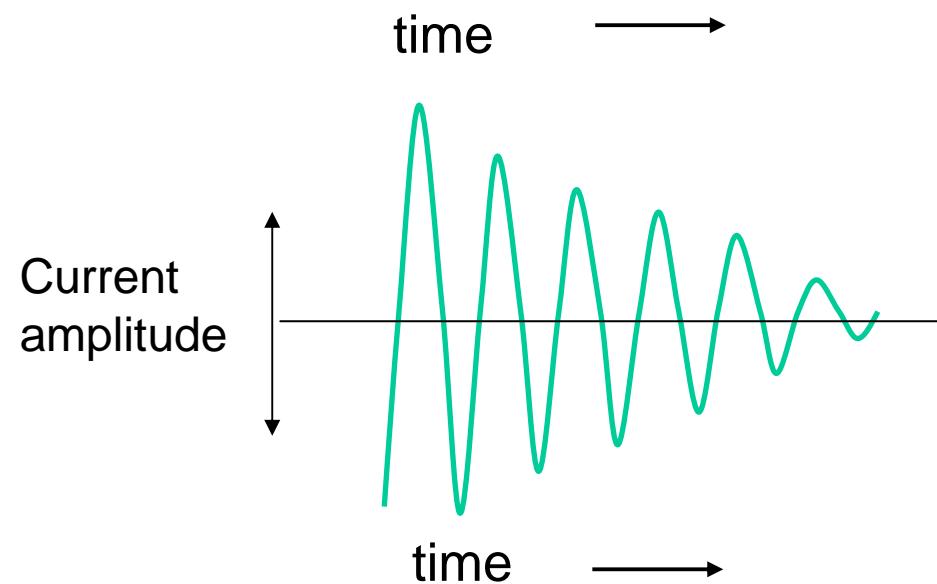
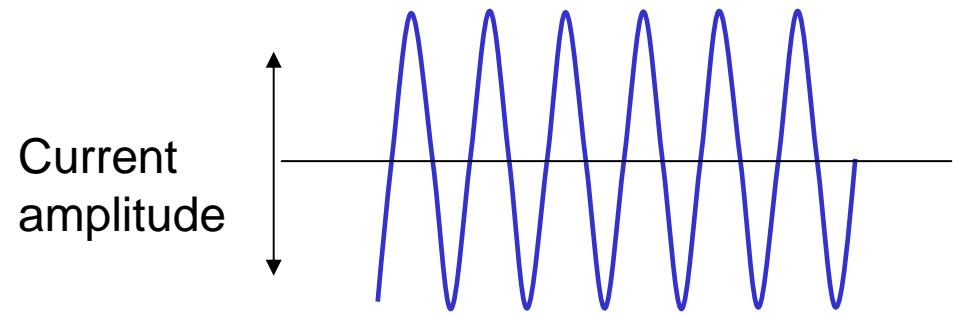
Adopted from Roy Hofmann,  
Hebrew University

The inversion recovery experiment yields T1 values for different signals that may have different relaxation times

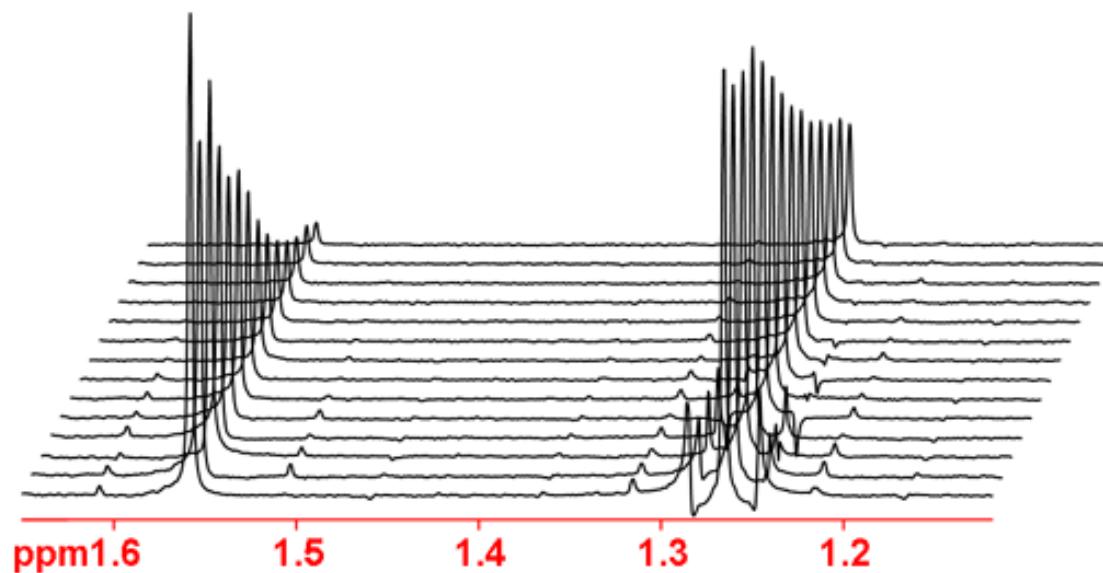
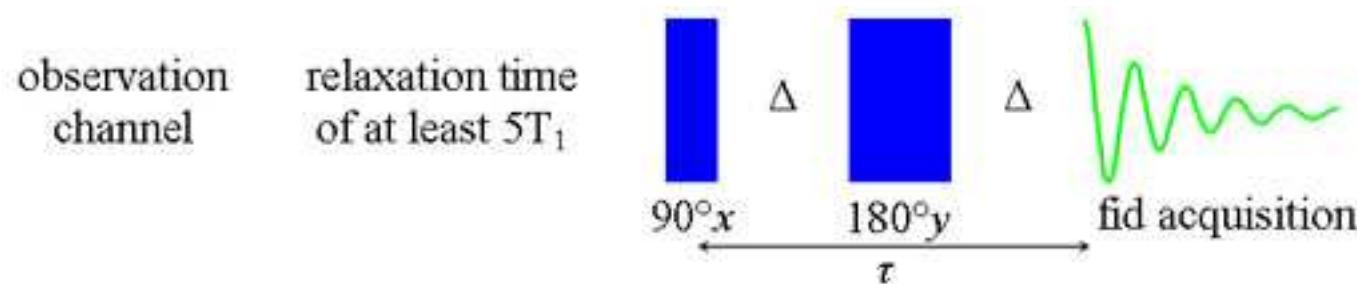


Example: Ethylbenzene in CDCl<sub>3</sub>

## $T_2$ relaxation leads to line-width broadening



# Spin-echo pulse sequence for measuring $T_2$



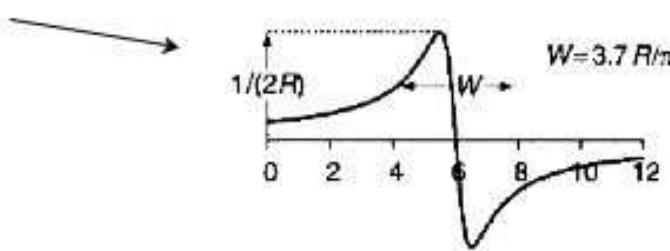
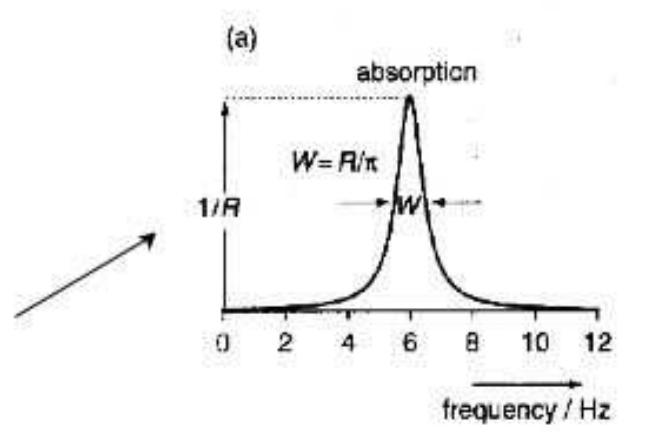
Example: Ethylbenzene in  $CDCl_3$

## Linewidth depends on transverse relaxation

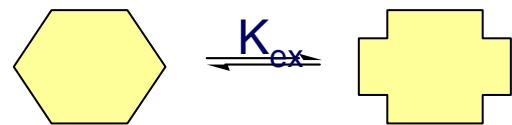
$$S(\omega) = \text{Re} \int_0^{\infty} s^+(t) \exp(-i\omega t) dt$$
$$= v(\omega) + iu(\omega)$$

$$v(\omega) = \lambda M_0 \frac{R_2}{R_2^2 + (\Omega - \omega)^2}$$

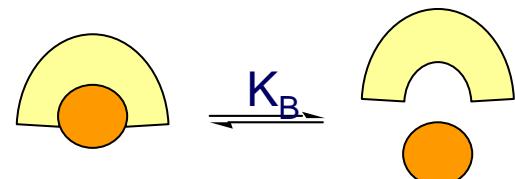
$$u(\omega) = \lambda M_0 \frac{\Omega - \omega}{R_2^2 + (\Omega - \omega)^2}$$



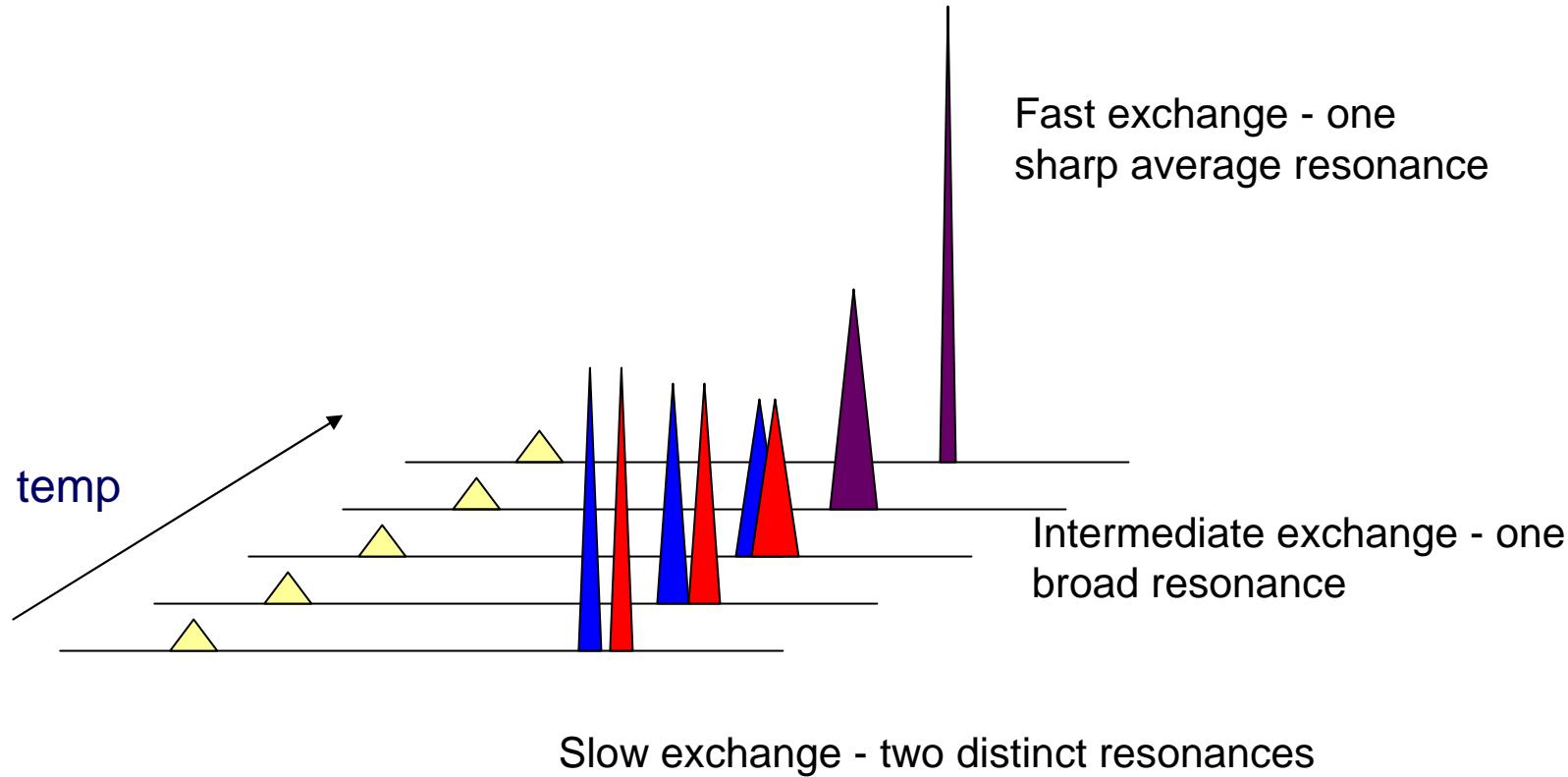
# Chemical exchange complicates matters



Conformational equilibrium



Chemical equilibrium

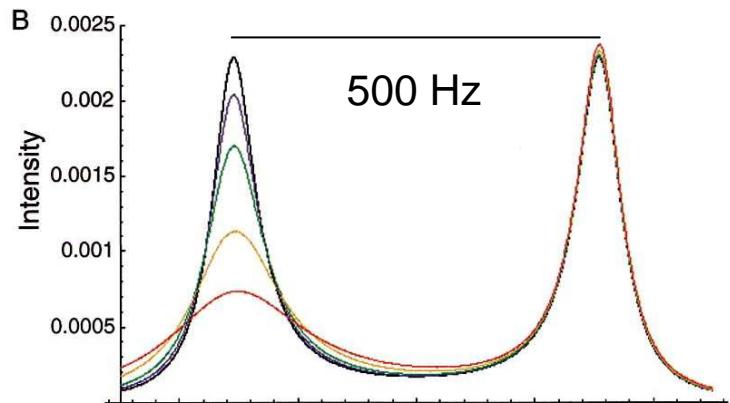


# Linewidth simulations for slow exchange interactions

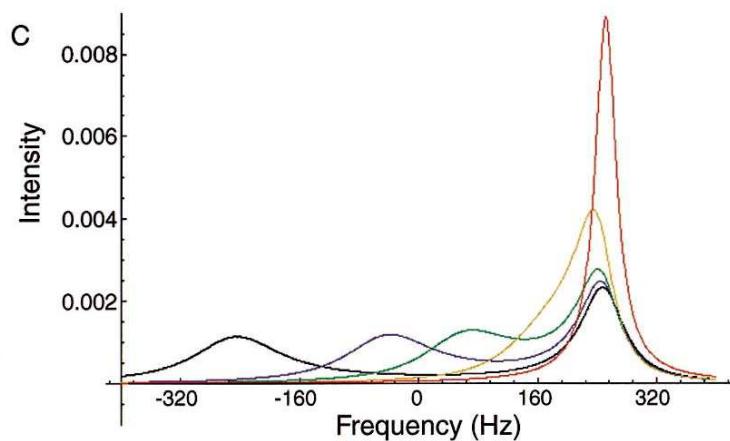


$$I(\omega) \sim \text{Re} \{W^* A^{-1} \mathbf{1}\}$$
$$A = i(\Omega - \omega E) + K + R$$

Changing  $R_2$  of the bound state: 500, 250, 100, 50 and 23  $\text{s}^{-1}$ . No chemical shift difference of free and bound state

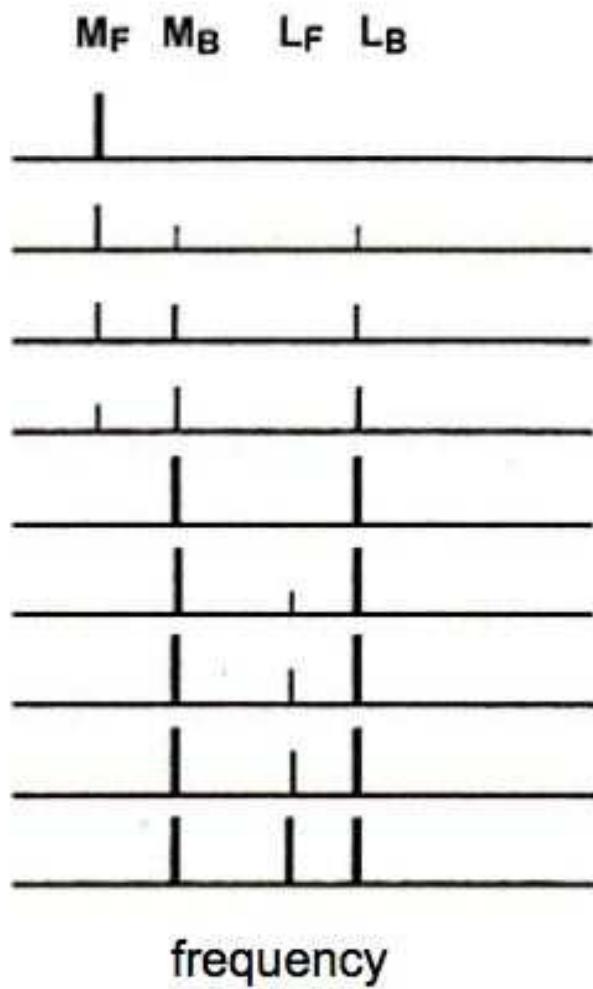


Same parameters used as above.  $R_2$  (free) is 23  $\text{s}^{-1}$  and  $k_{\text{off}} = 200 \text{ s}^{-1}$ . The fraction of free protein is 0.5.



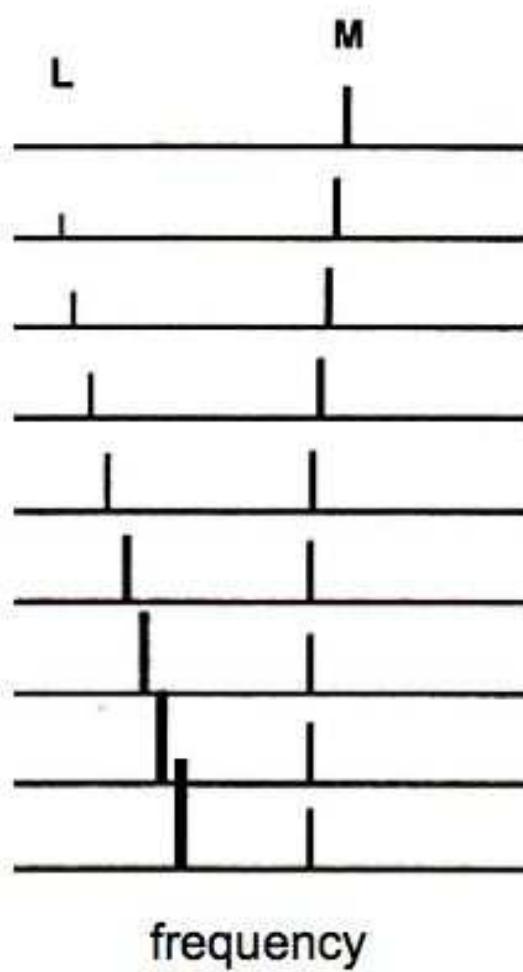
$R_2$  (bound) is set to 250  $\text{s}^{-1}$  and chemical shifts are varied : 500, 250, 100, 50 and 23 Hz

## What type of exchange ?



$L:M$

0:1
0.25:1
0.5:1
0.75:1
1:1
1.25:1
1.5:1
1.75:1
2:1

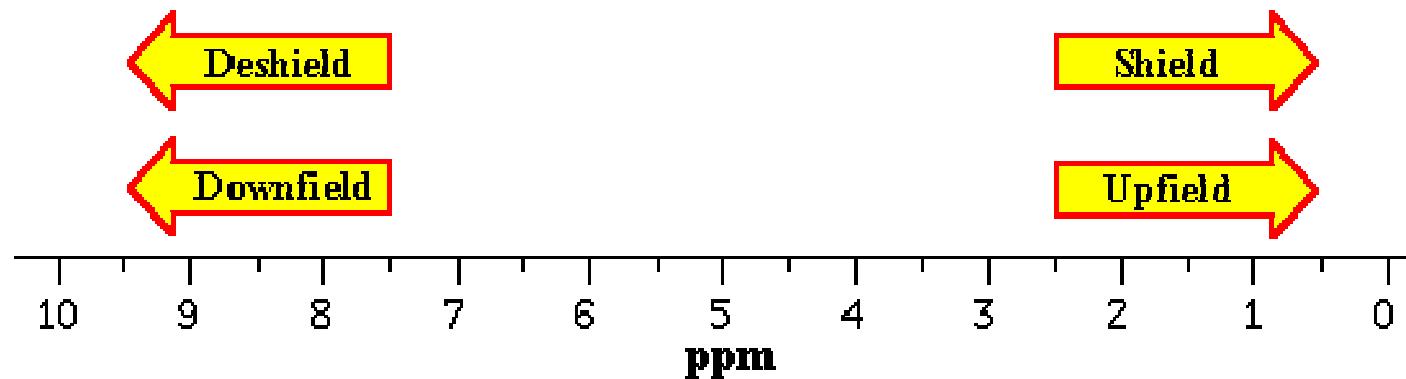




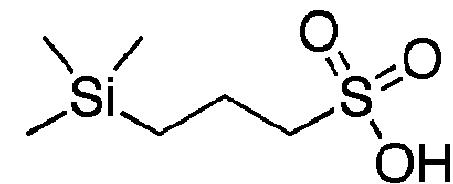
# Mapping protein interactions:

## Chemical shift as a measure of chemical environment :

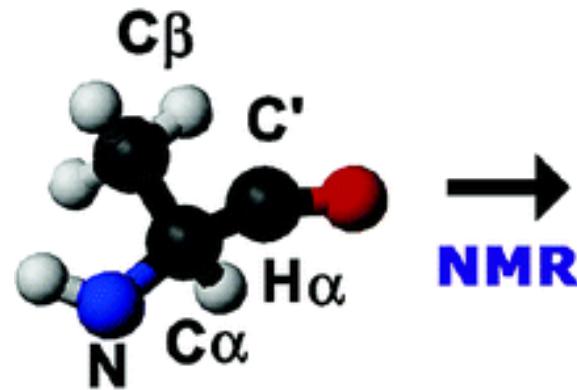
$$\delta = \frac{\text{difference in precession frequency between two nuclei}}{\text{operating frequency of the magnet}}$$



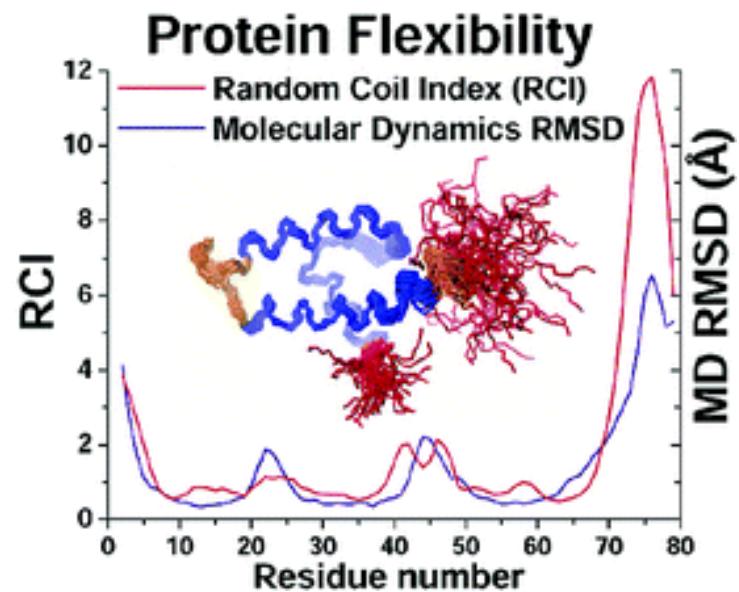
Reference against: 2,2-dimethyl-2-silapentane-5-sulfonic acid (DSS)



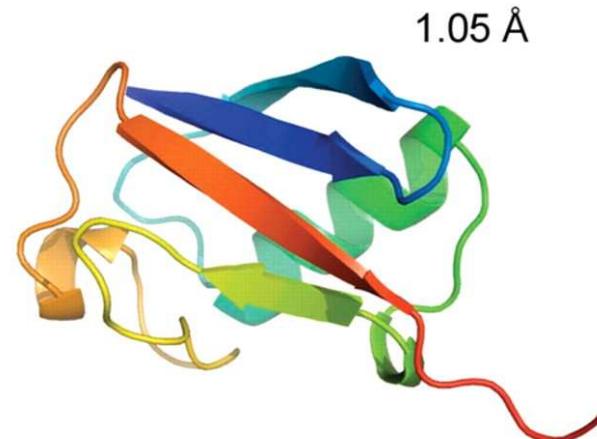
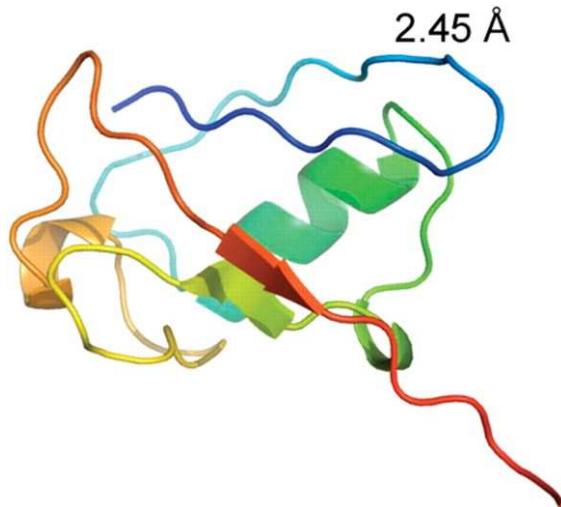
## Predicting protein chemical shifts via CSI



→ **NMR**



## Structure refinement via CSI

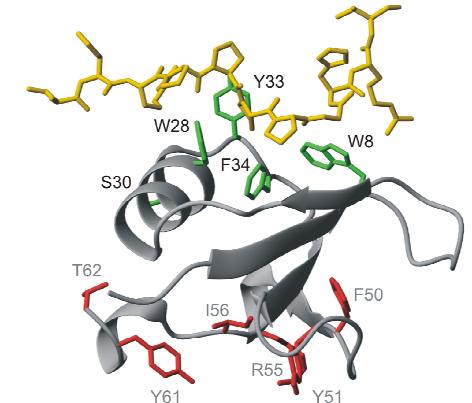
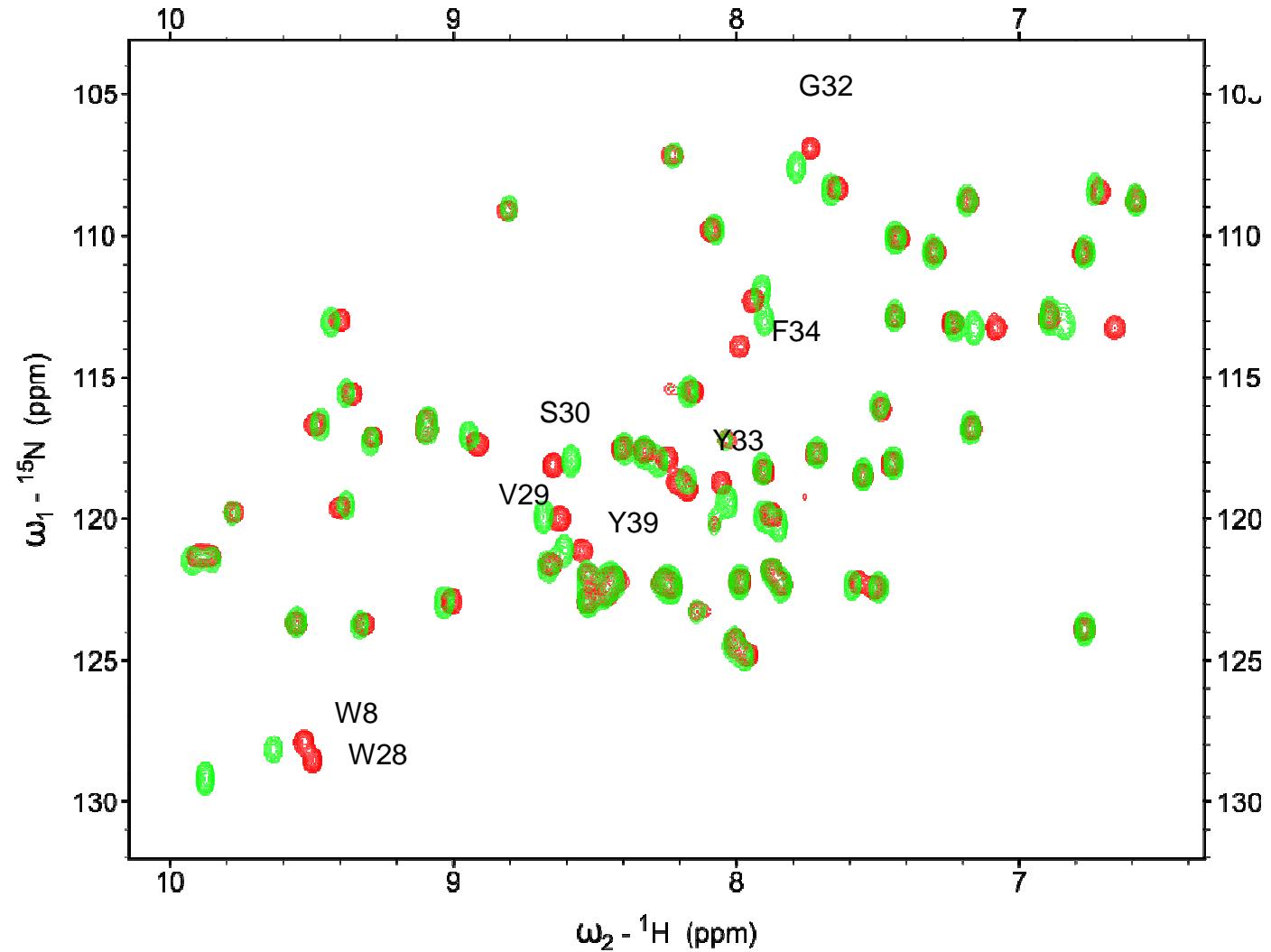


<http://www.cs23d.ca/>

Berjanskii & Wishart,  
Nature Protocols 1, - 683 - 688 (2006)

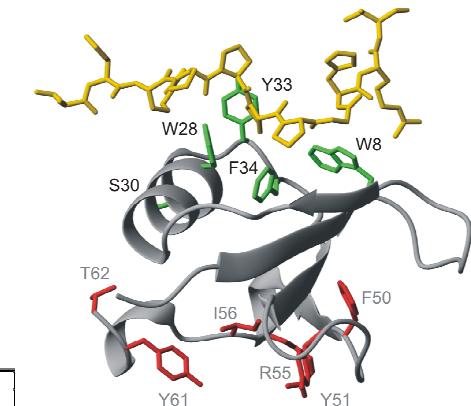
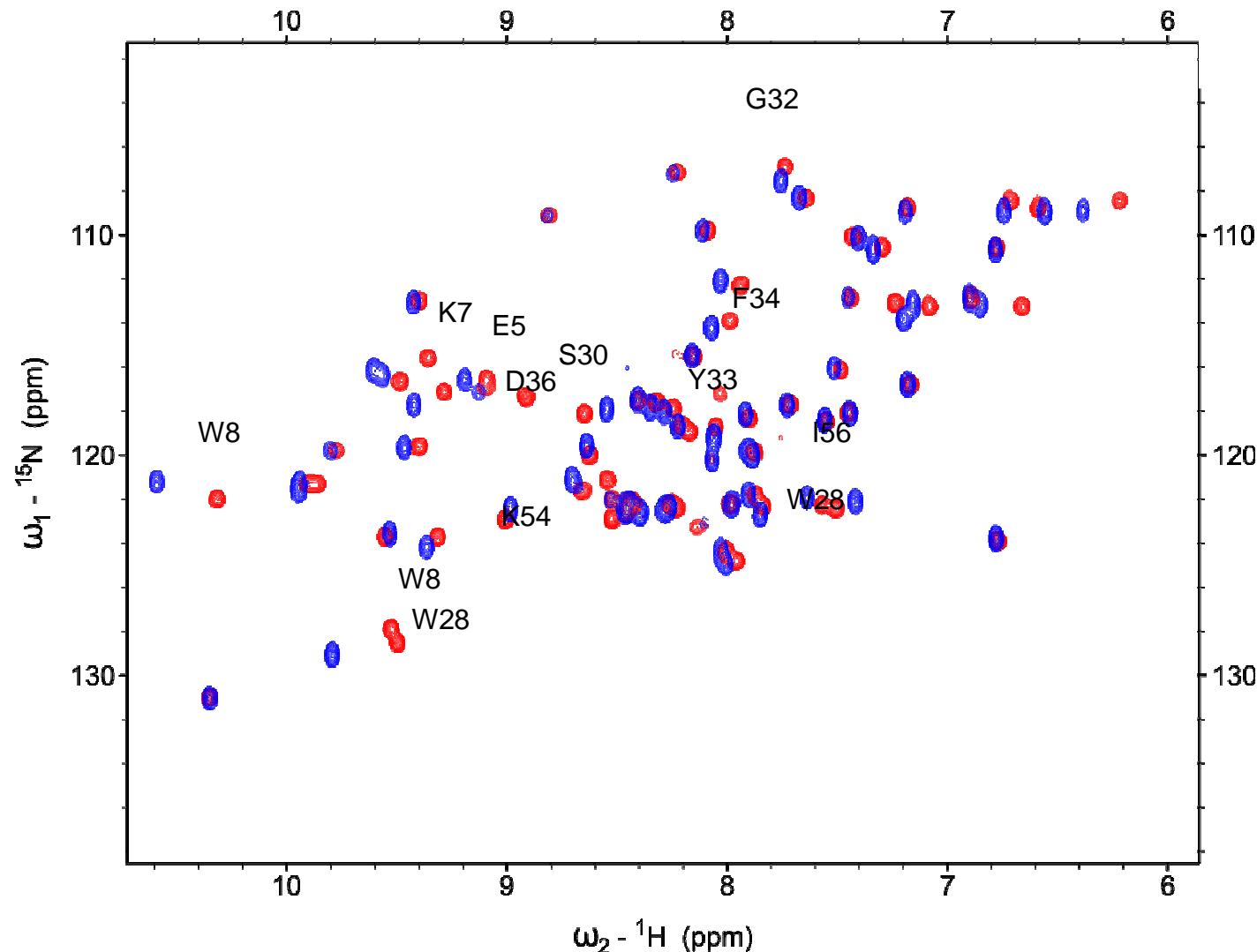
# Chemical shift changes : a single non-disruptive mutation

Wt(rot)/Y33A(grün)

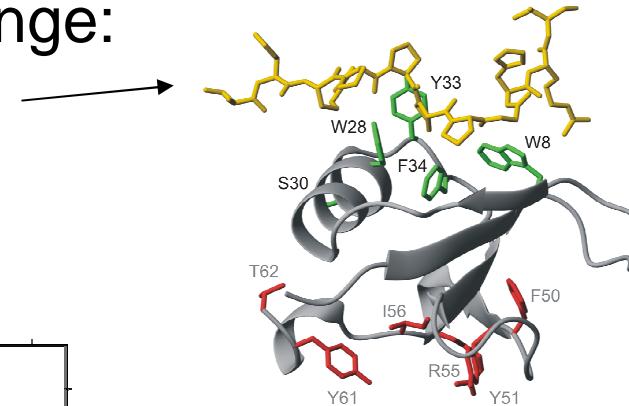
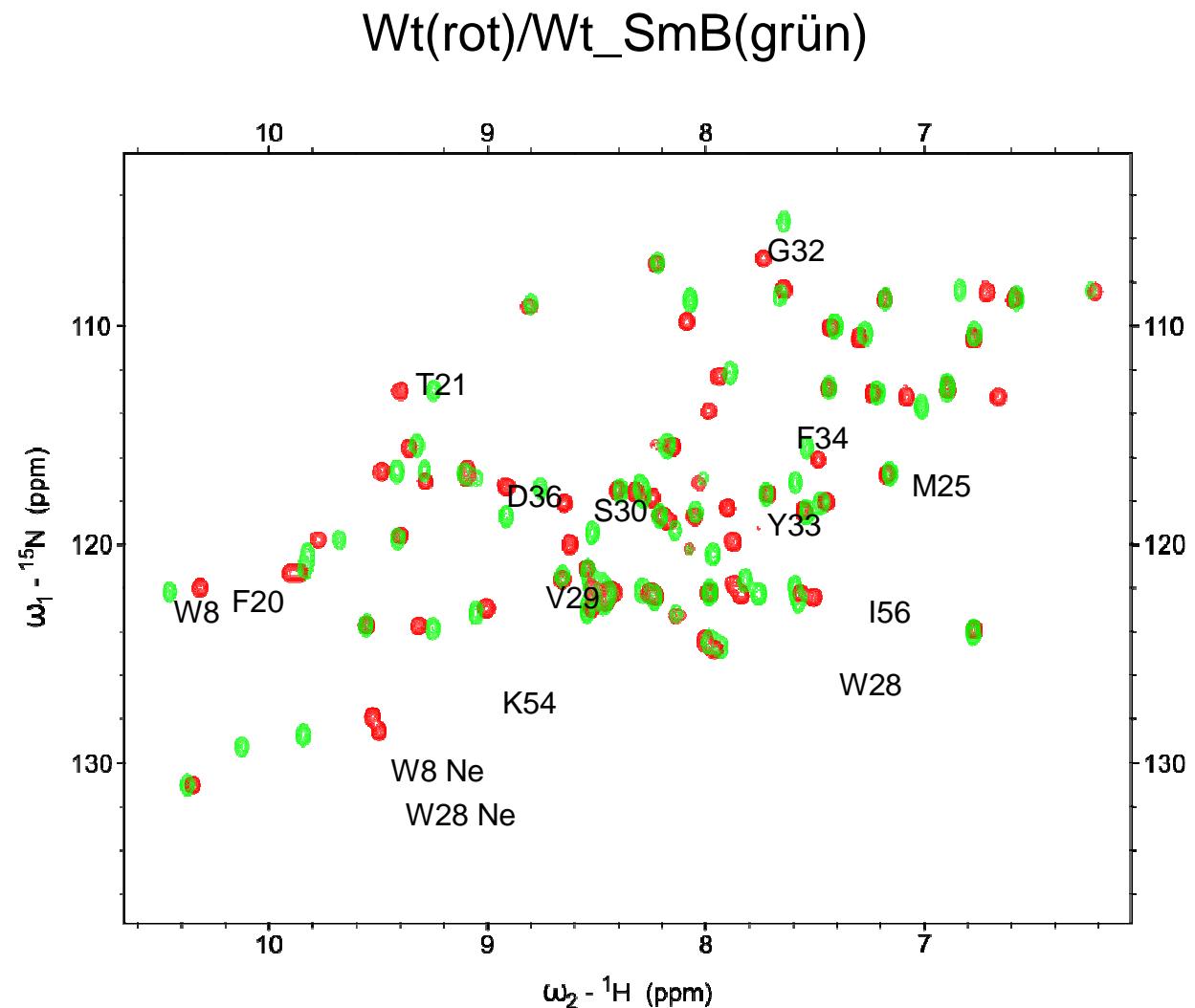


# Chemical shift changes : two non-disruptive mutations

Wt(rot)/Y33AW8R(blau)



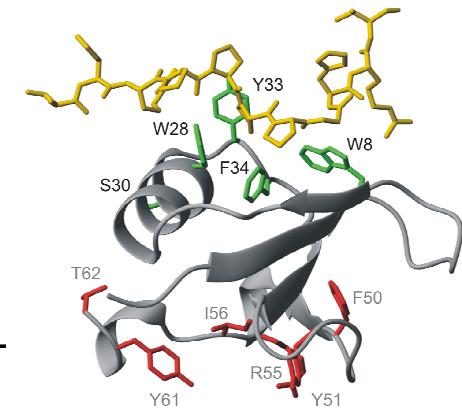
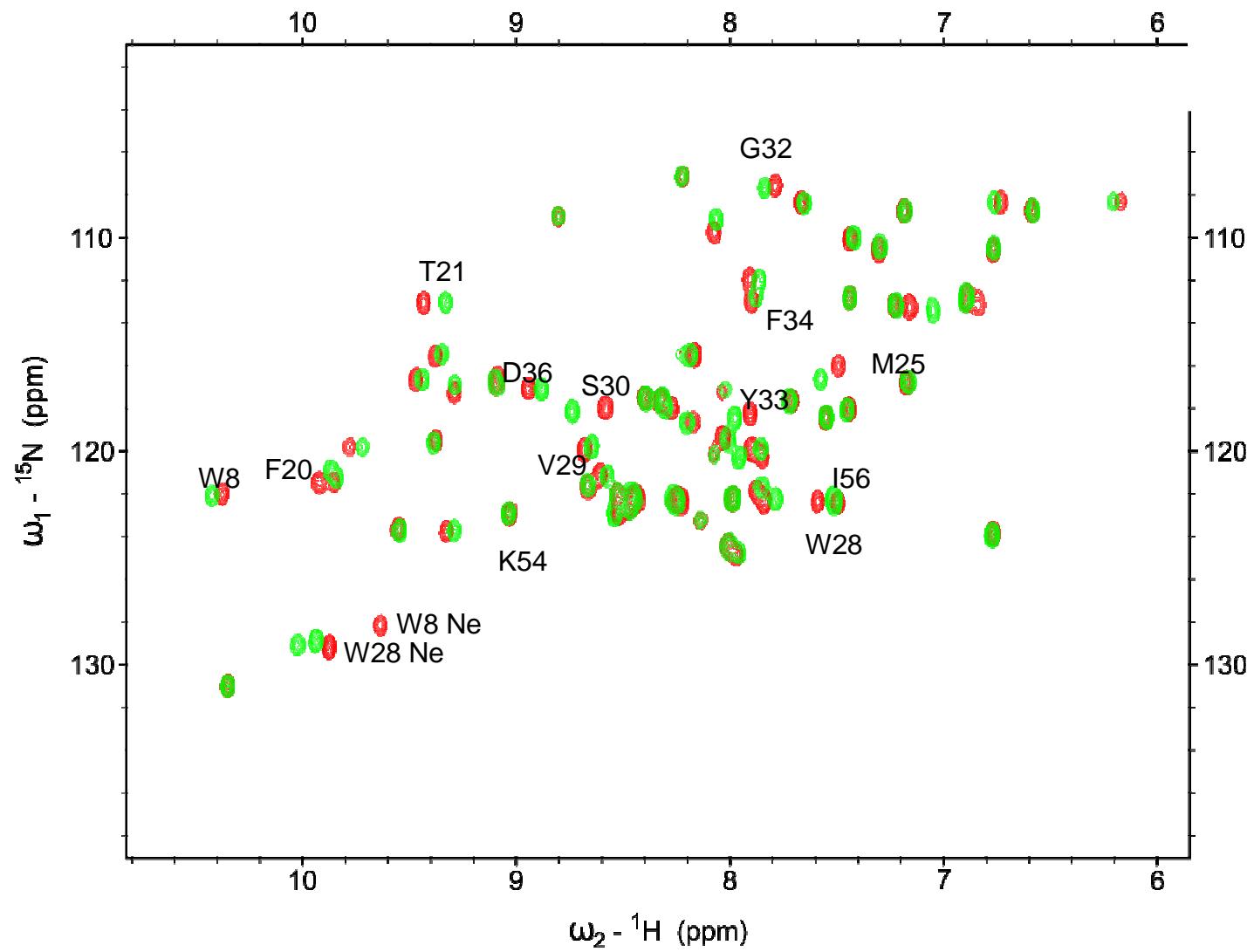
# Chemical shift changes:Fast exchange: GYF binding to spliceosomal SmB



$$[\text{PL}] = 1/2(K_D + [\text{P}]_0 + [\text{L}]_0) - \sqrt{1/4(K_D + [\text{P}]_0 + [\text{L}]_0)^2 - [\text{L}]_0 [\text{P}]_0}$$

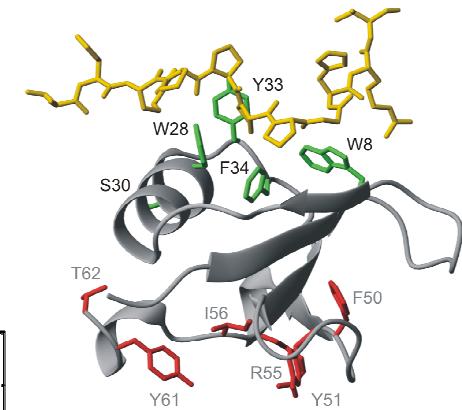
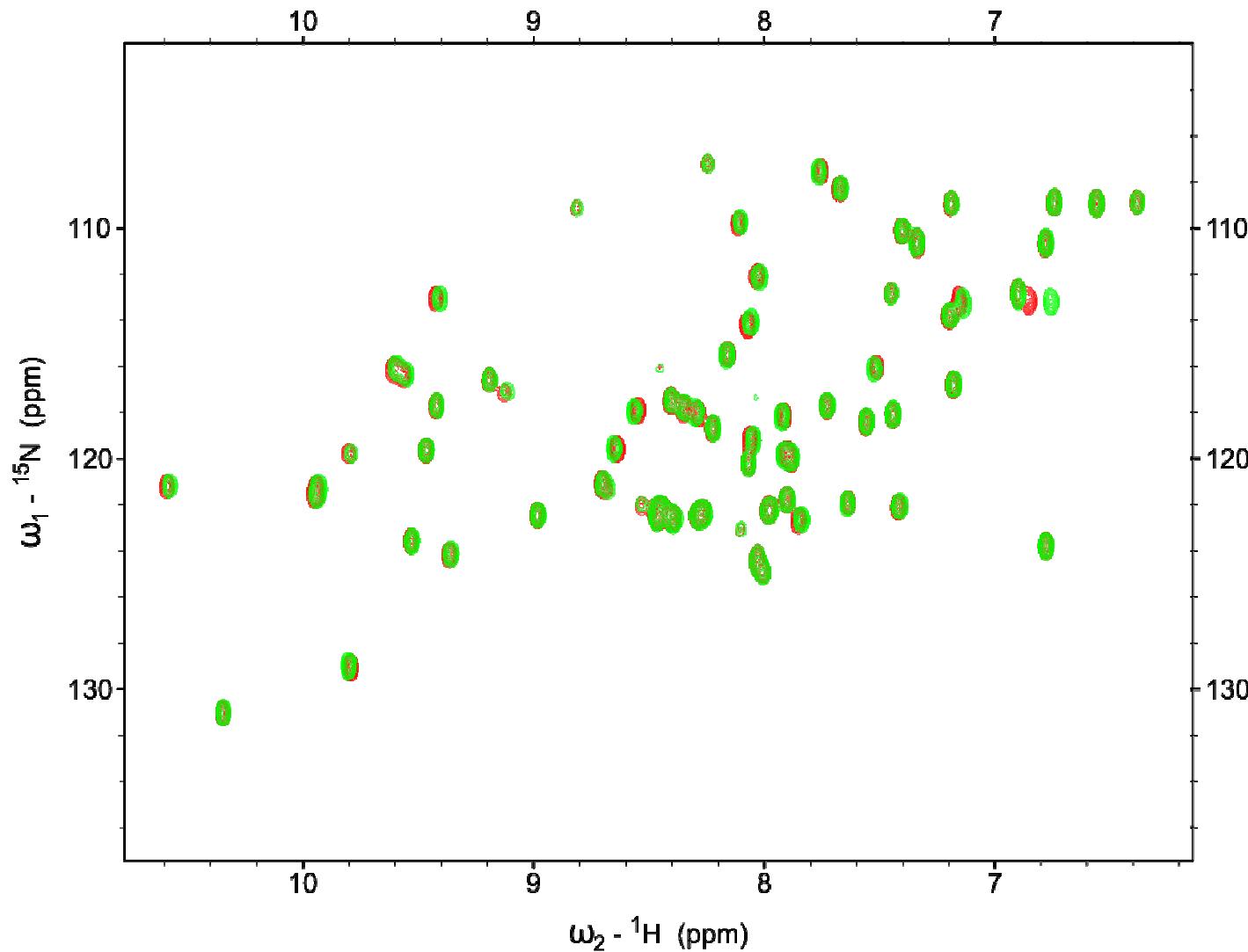
# Binding of the single-site mutant

Y33A(rot)/Y33A\_SmB(grün)

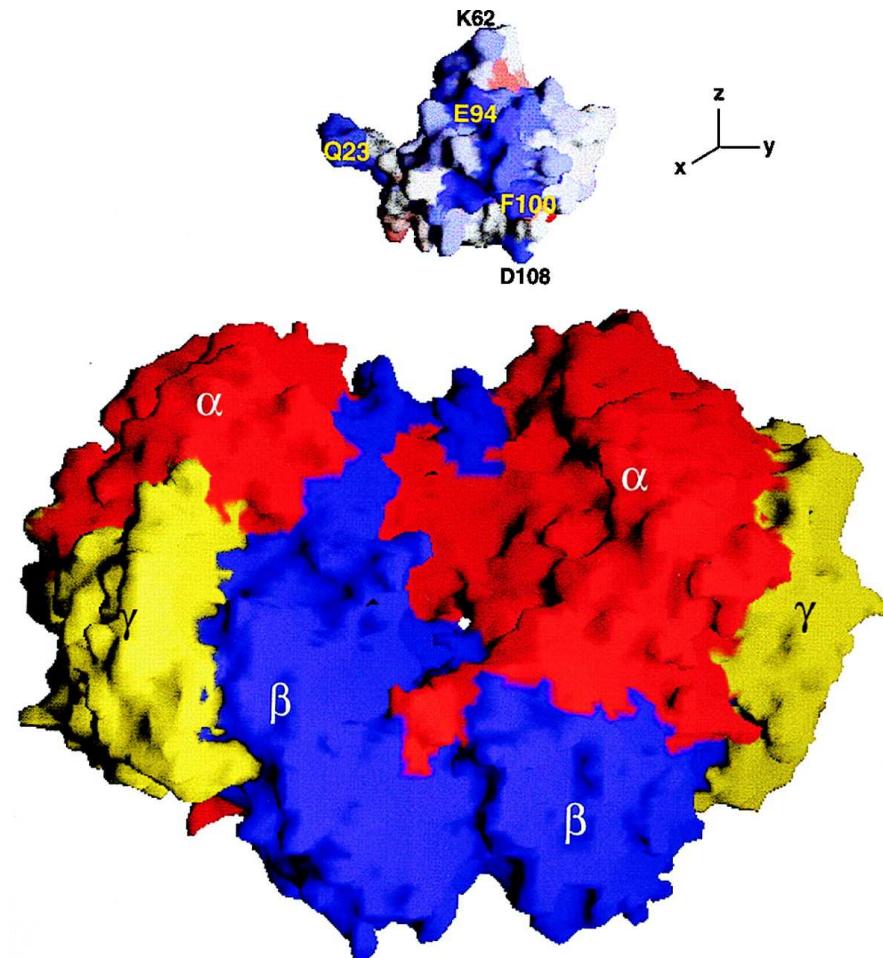
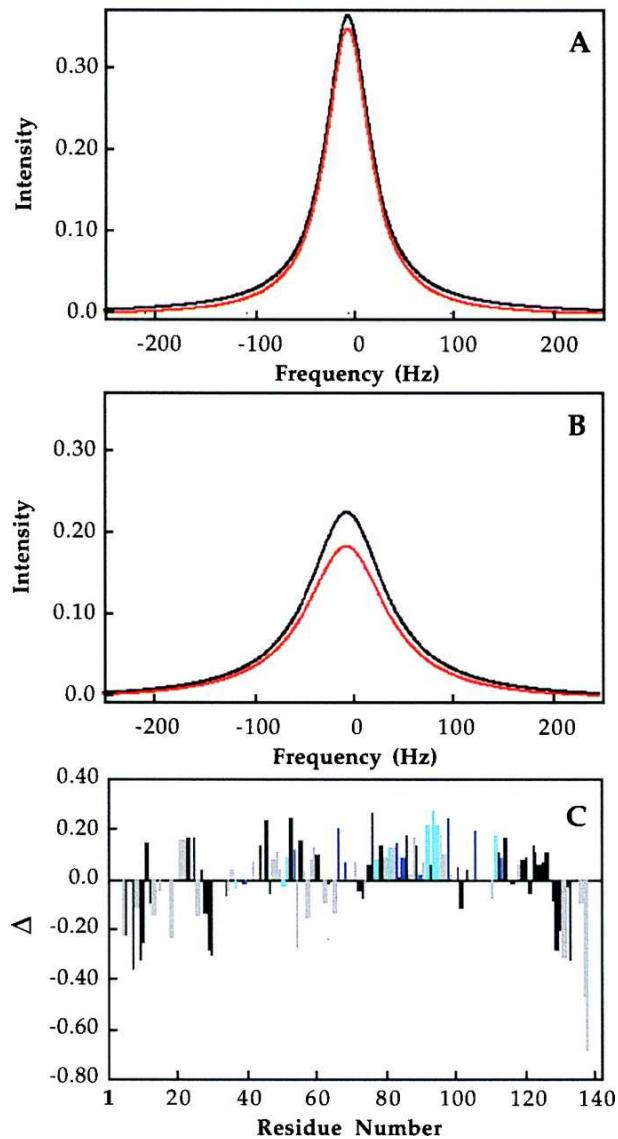


# (Non-)Binding of the double mutant

Y33AW8R(rot)/Y33AW8R\_SmB(grün)



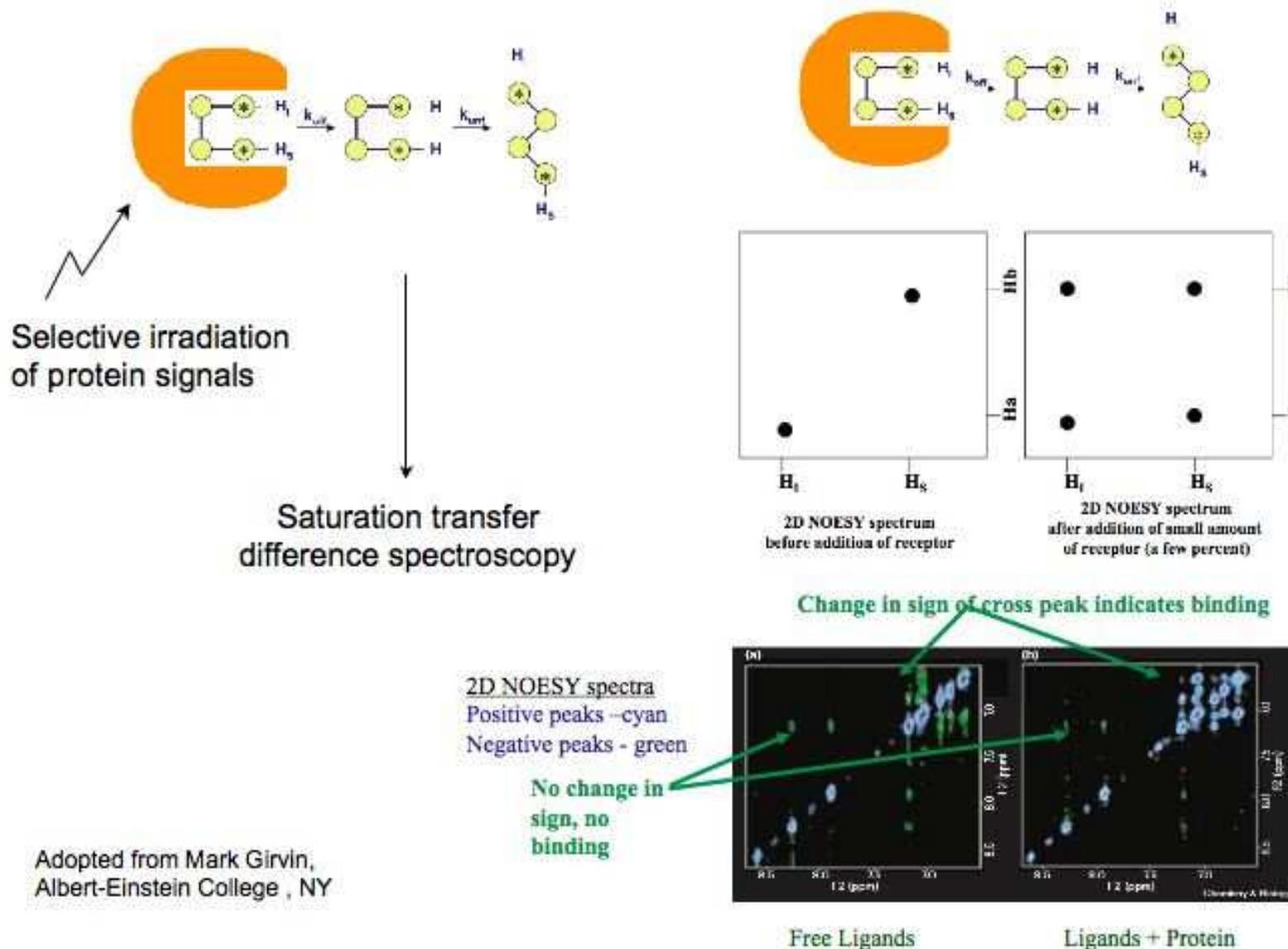
# Slow exchange: Linewidth analysis can be used to map binding sites



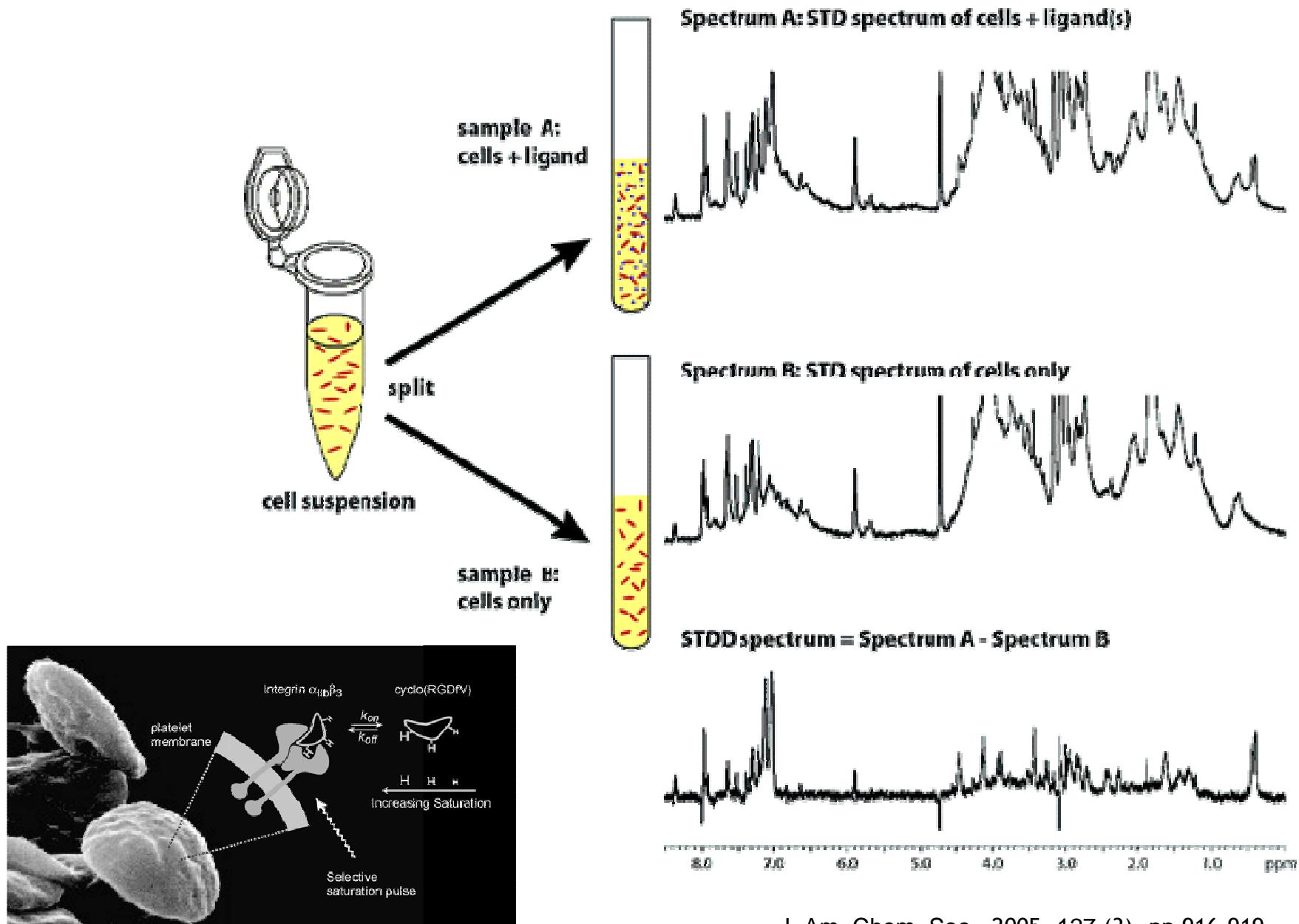
Walters et al., PNAS 1999, 96, 7877-7882

$k_{\text{off}}$  values of 3.2 s<sup>-1</sup> (A) or 25.6 s<sup>-1</sup> (B) for chemical shift differences of 0 Hz (black) and 500 Hz (red). R 1, R 2, and a are 23 Hz, 250 Hz, and 0.8, respectively

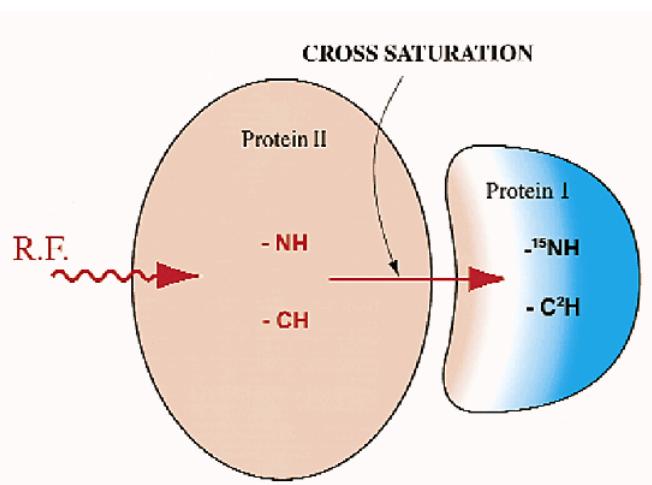
# Transferred NOEs for determination of bound ligand structures



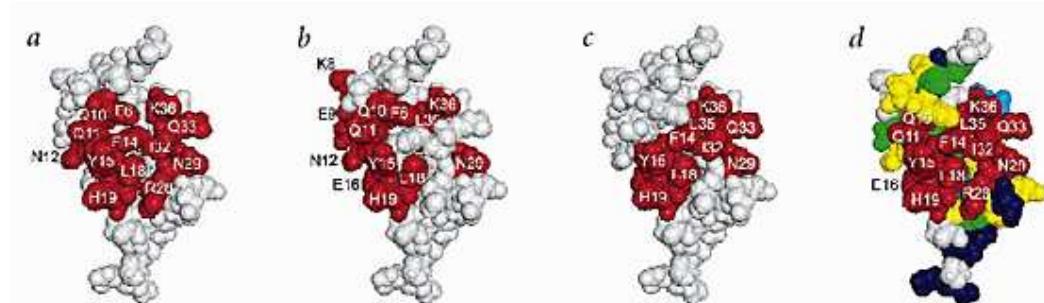
# STD-NMR can be used to observe binding in complex mixtures



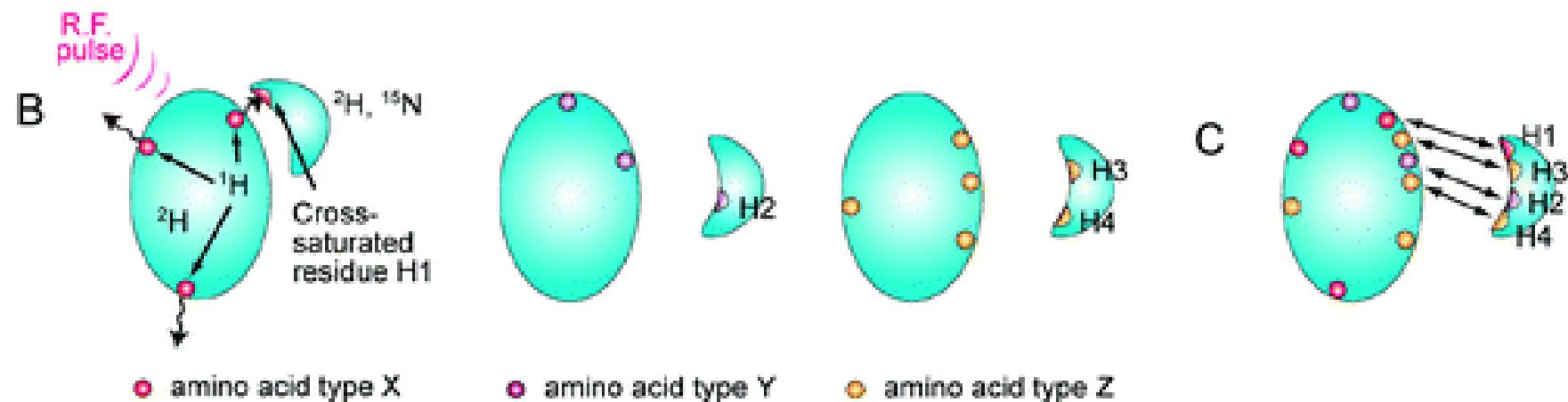
## Cross saturation: detection of $^{15}\text{NH}$ groups of a deuterated acceptor protein



Takahashi et al., Nat. Struct. Biol.(2000)

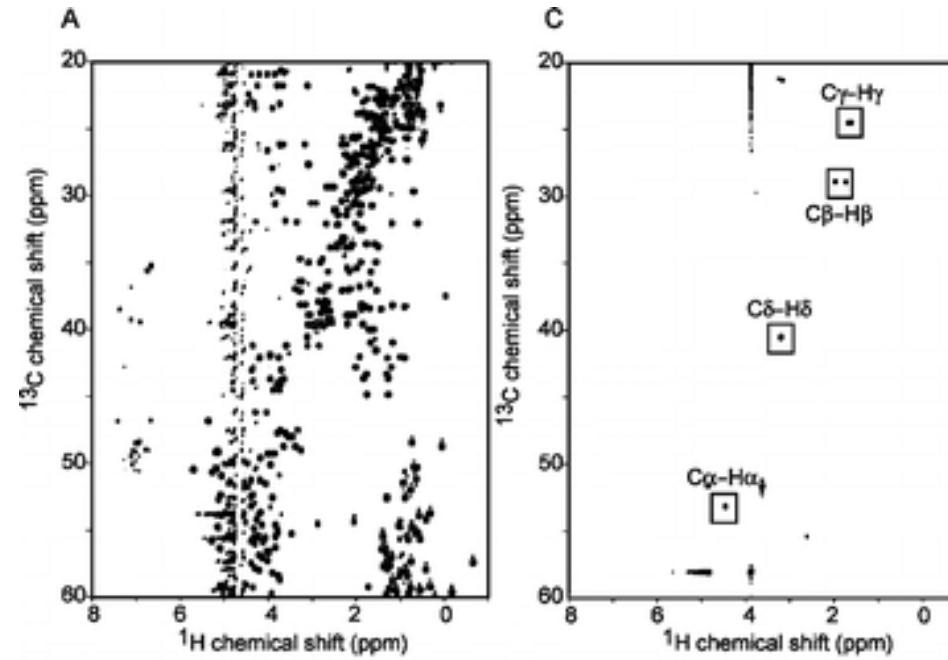


Variant: Selective protonation of an otherwise deuterated donor protein



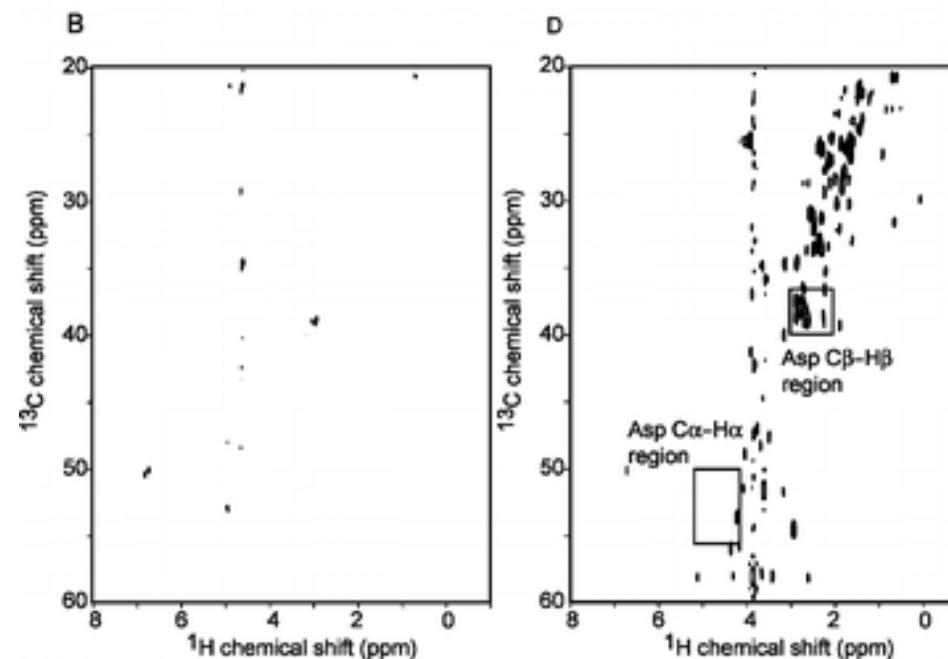
Igarashi et al., JACS 2008

# Selective protonation of amino acids with different efficiencies



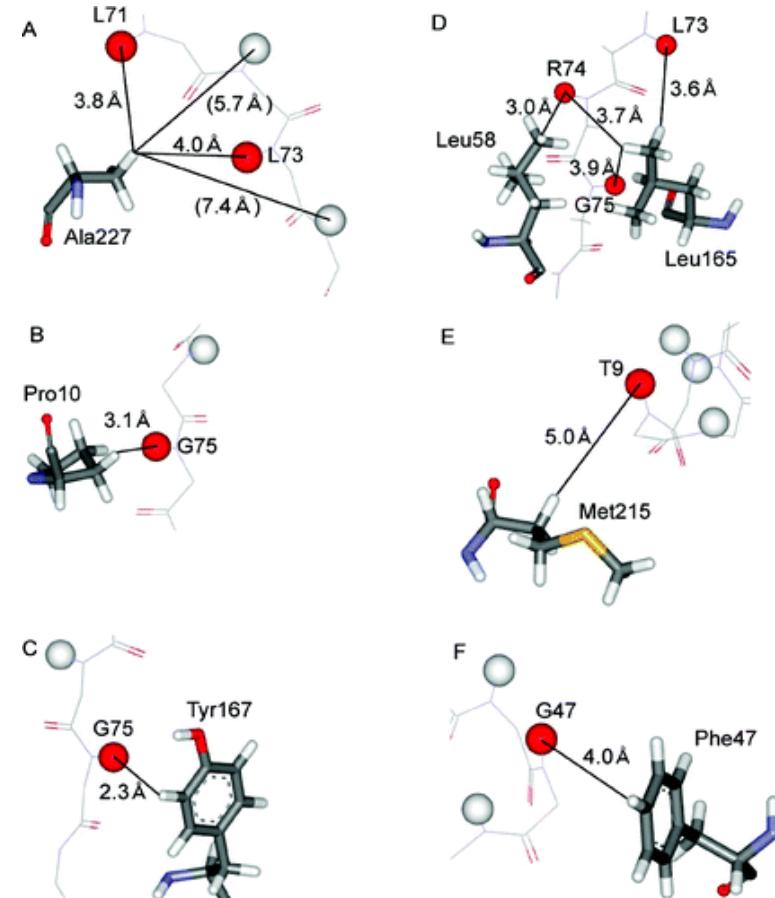
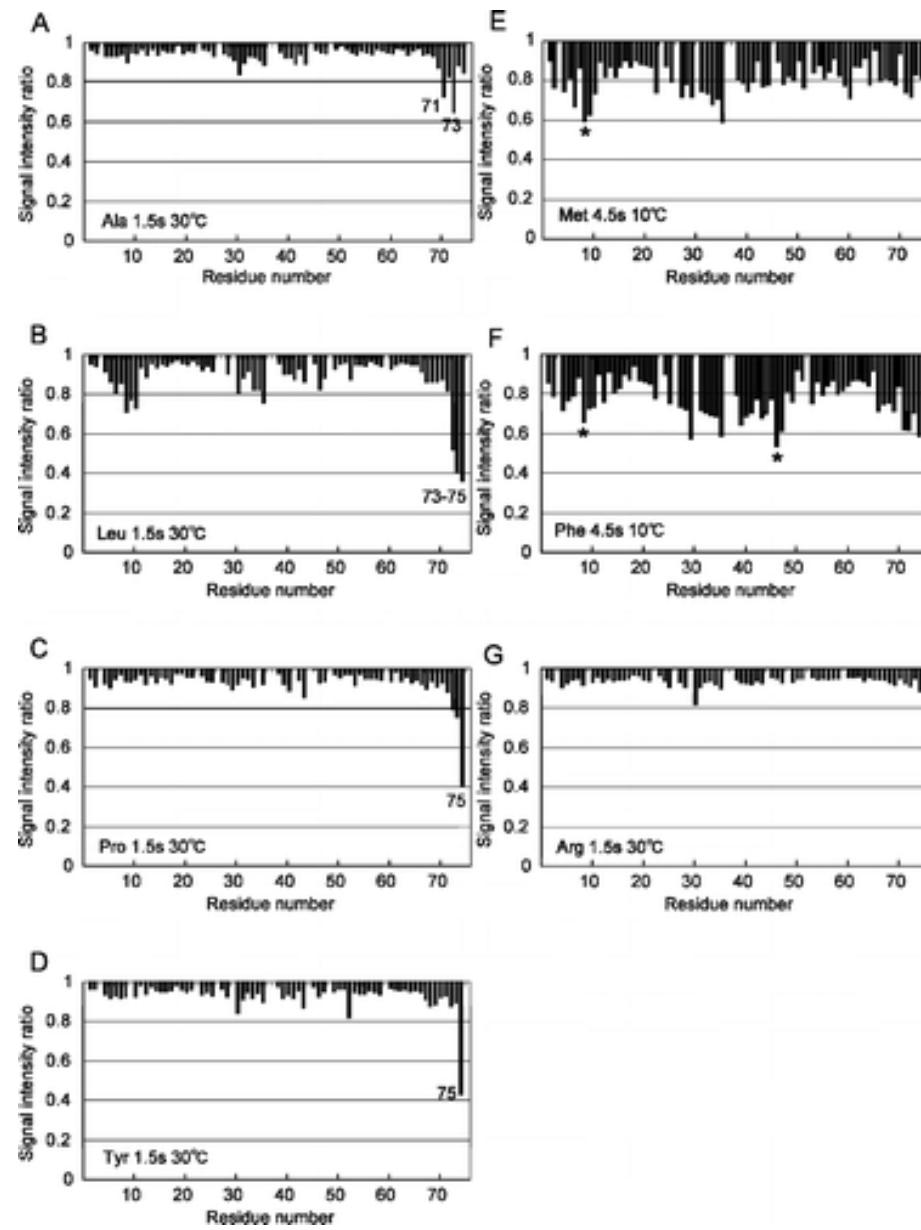
Arginine

Feasible for: Ala, Arg, Cys, Gly, His, Ile, Leu, Lys, Met, Phe, Pro, Trp, and Tyr

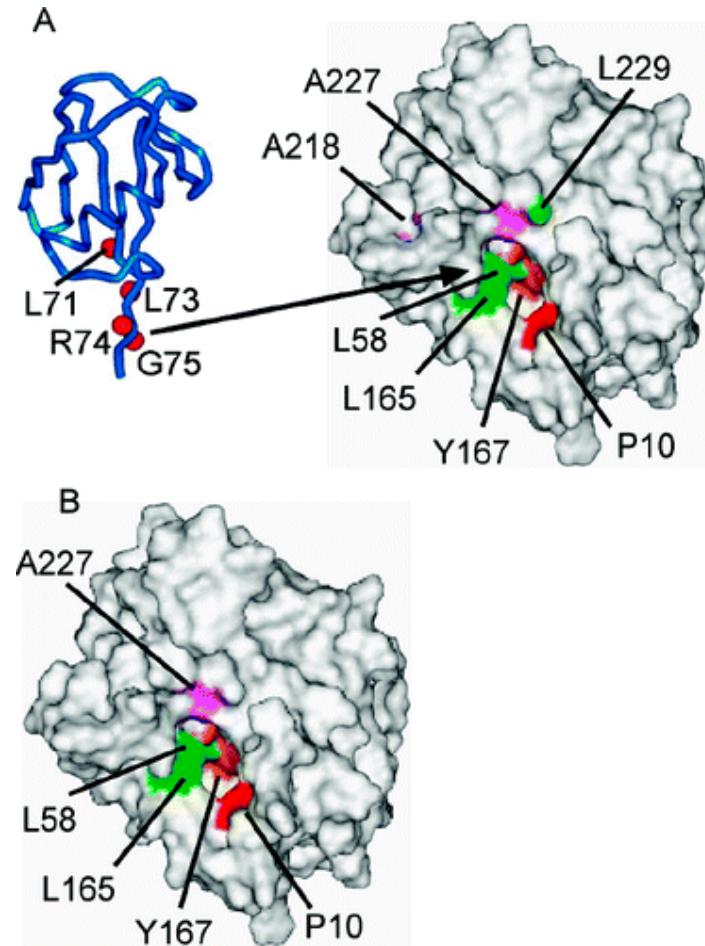
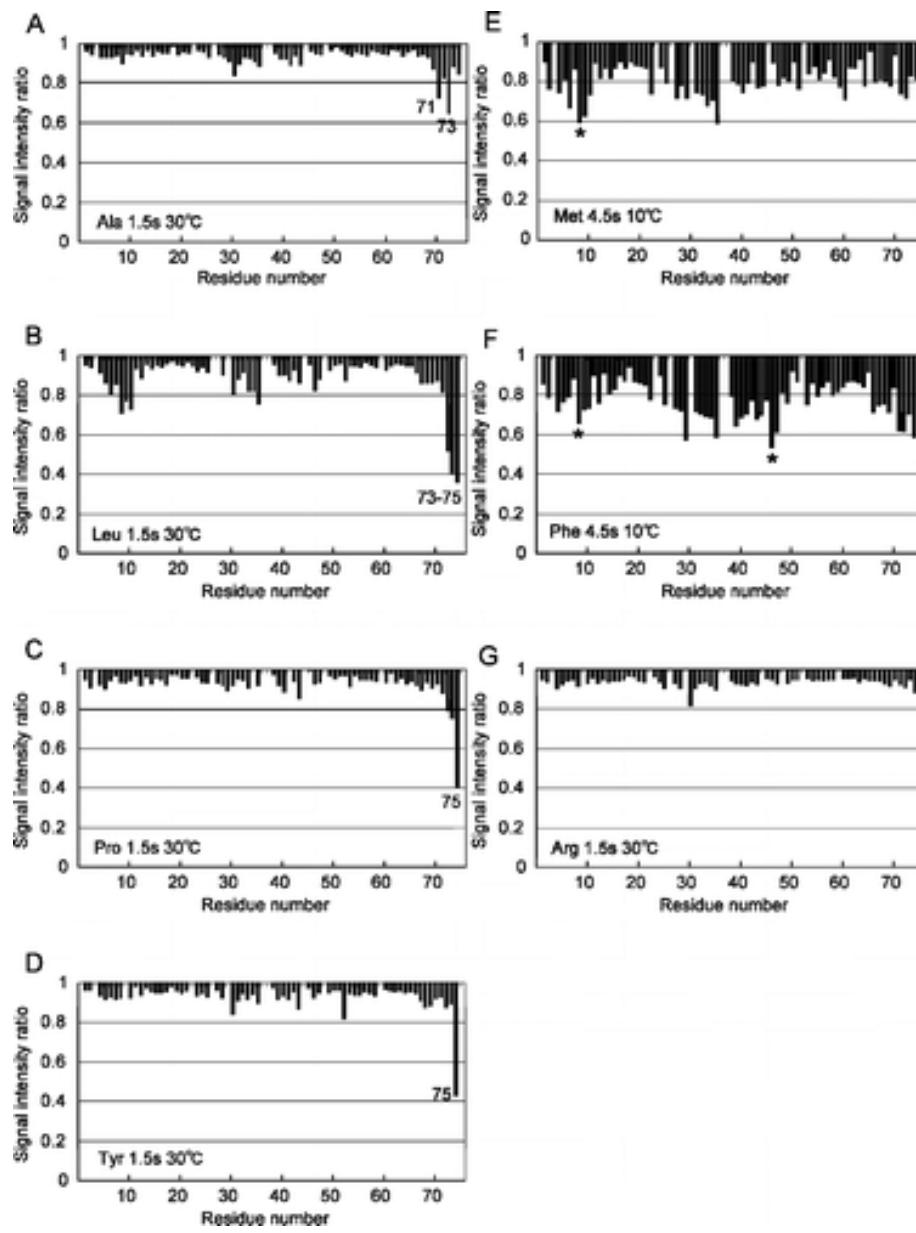


Aspartate

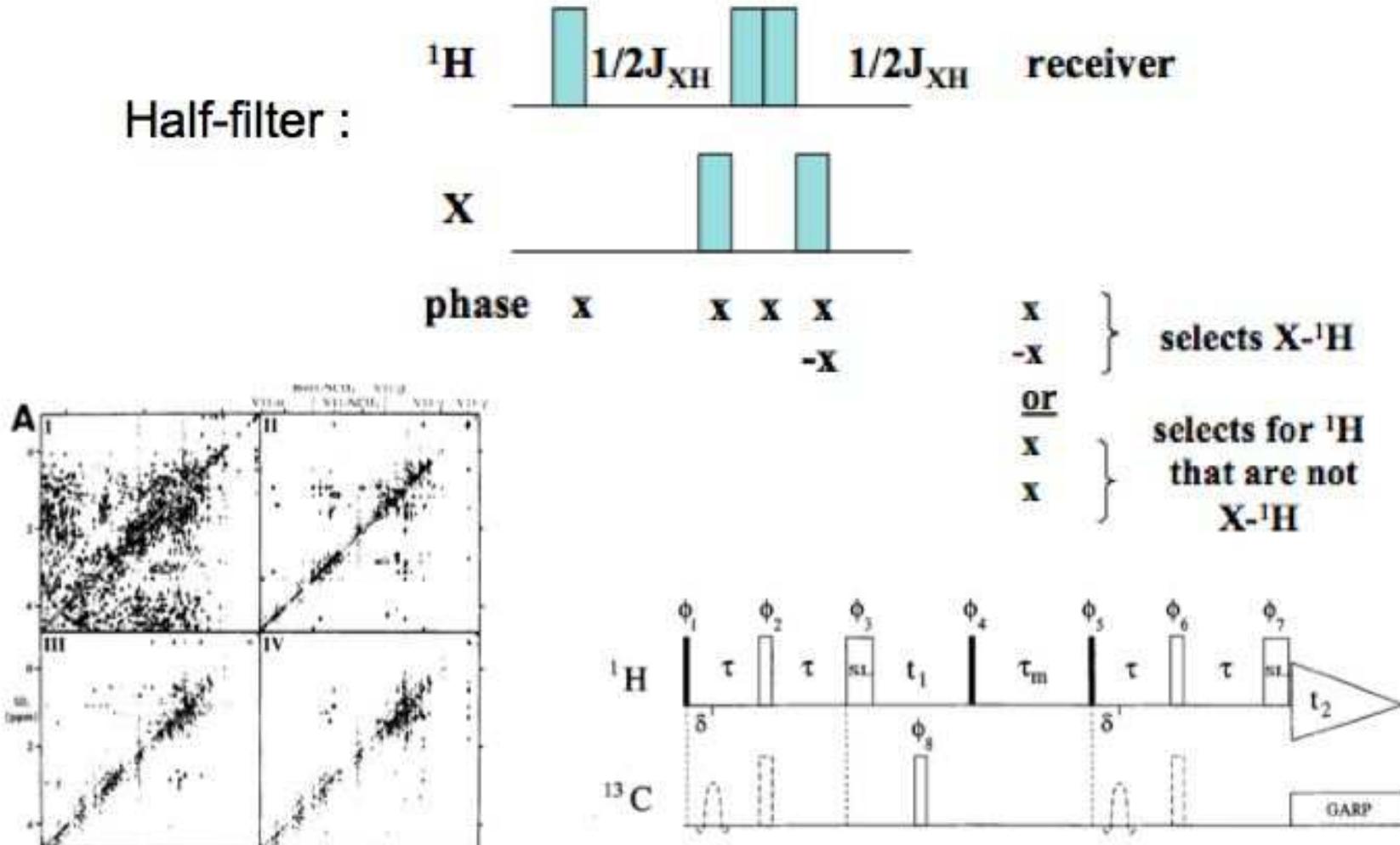
# Identification of donor residues close in space to affected acceptor amides



# Identification of donor and acceptor interfaces



# Determining the structure of protein:ligand complexes

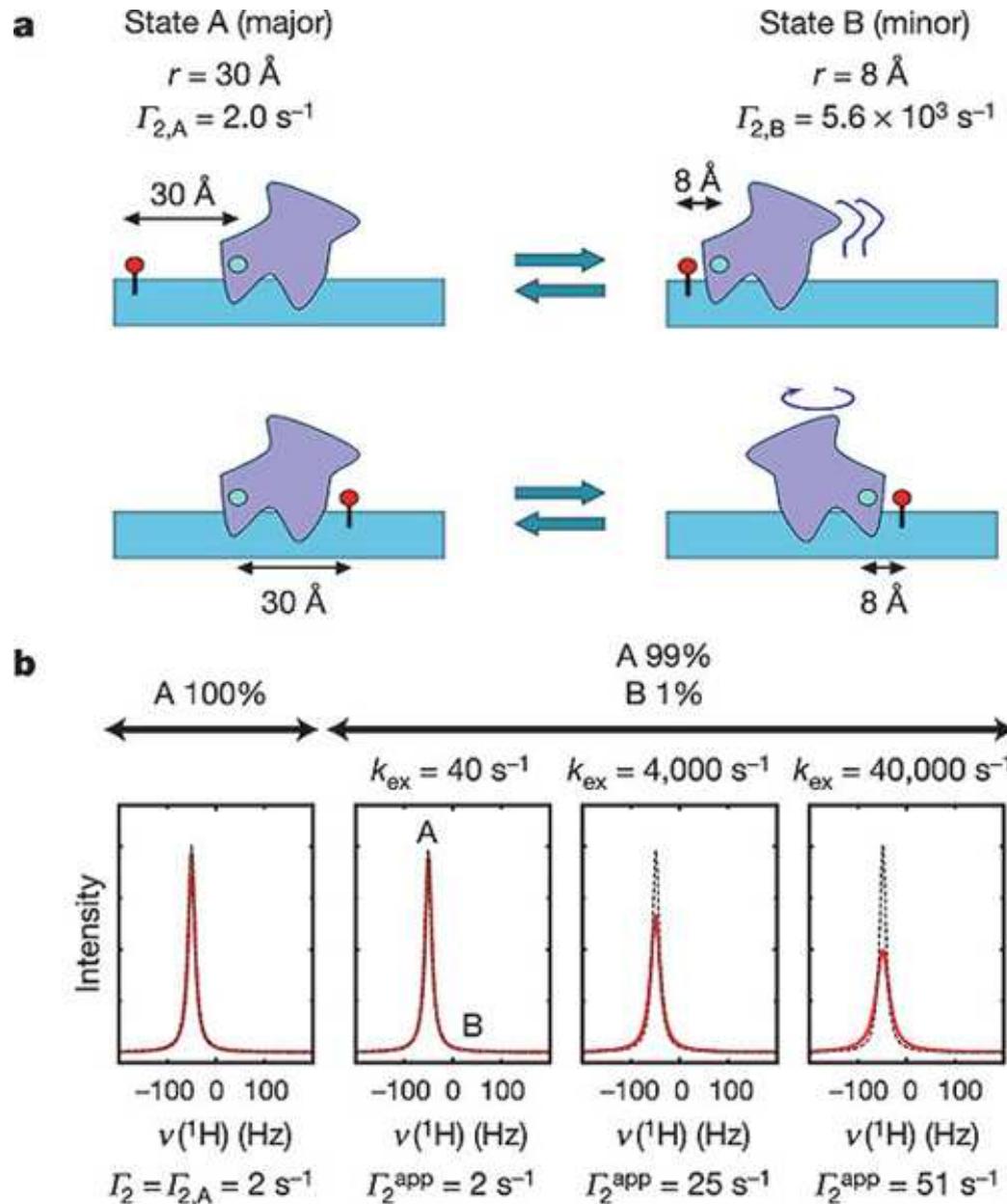


Wider et al., JACS, 1990

Folmer et al., J Biomol. NMR 1995

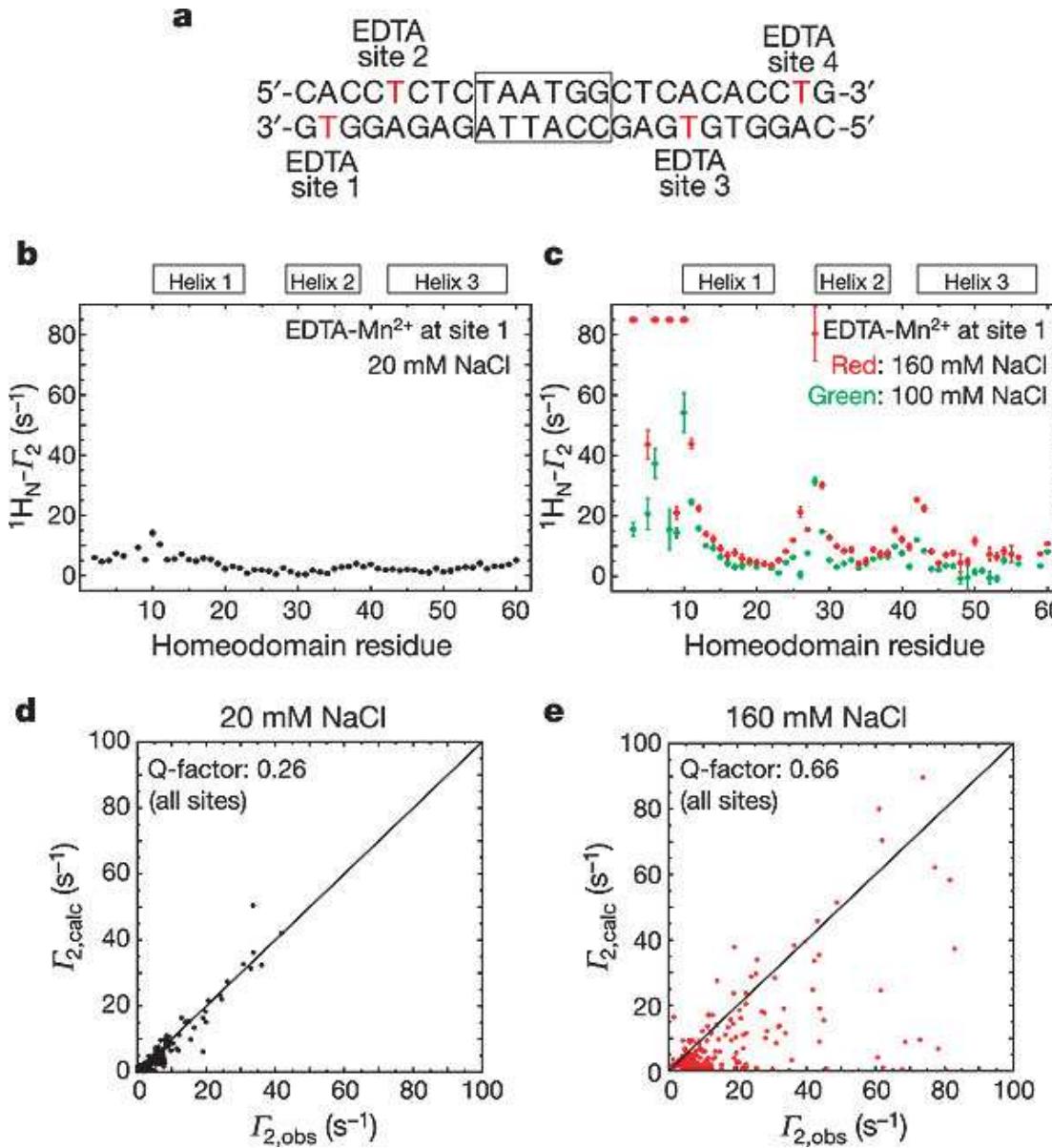
..to be continued in later sessions

# Paramagnetic relaxation enhancement



Iwahara & Clore,  
Nature, 2006

# At higher salt concentrations, $T_2$ relaxation data cannot be explained by the specific complex

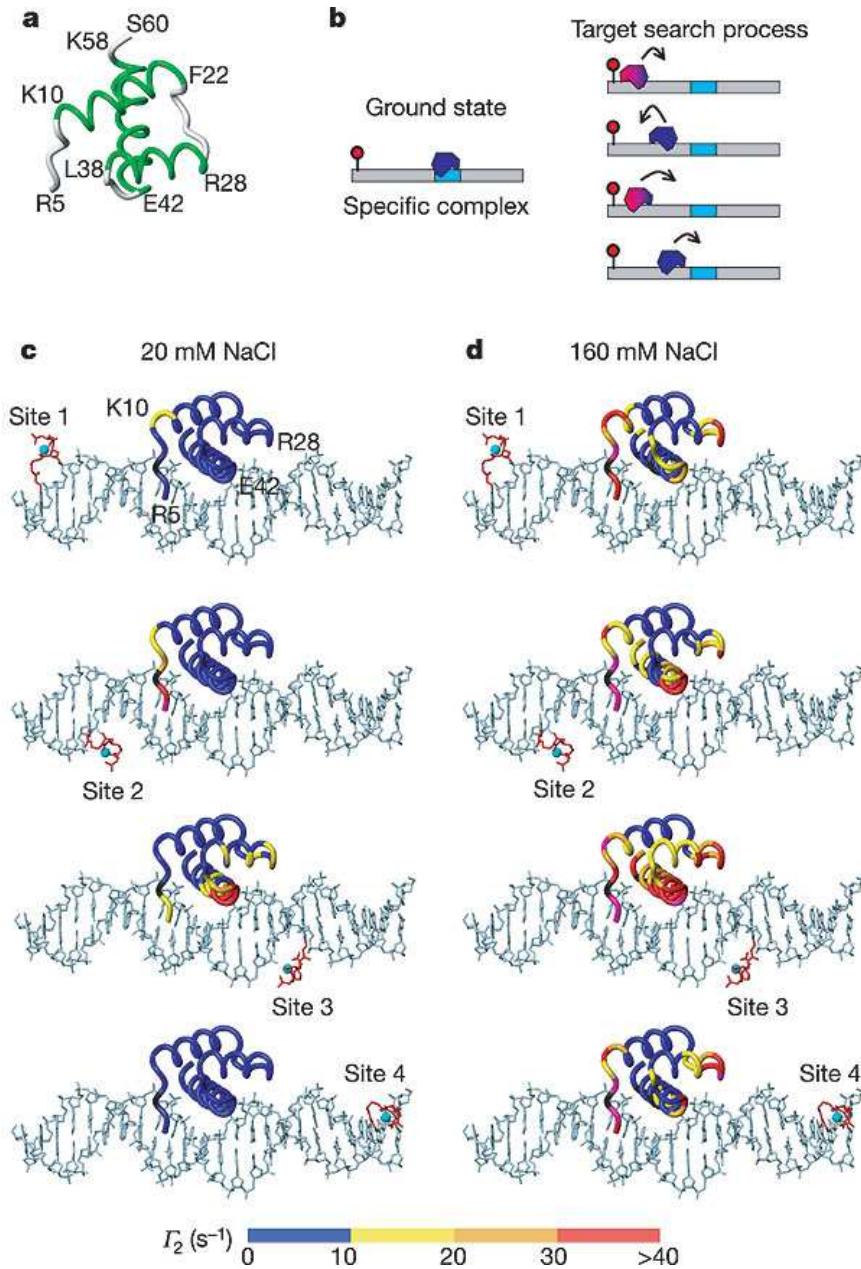


Model system:  
Homeodomain of human  
HOXD9 in complex with a  
24-base-pair DNA duplex

Incorporation of conjugated  
deoxy(d)T-EDTA-Mn<sup>2+</sup> into  
the DNA

$$Q = \left( \frac{\sum \{ \Gamma_2^{\text{obs}}(i) - \Gamma_2^{\text{calc}}(i) \}}{\sum \Gamma_2^{\text{obs}}(i)^2} \right)$$

## Low-affine interactions likely contribute to formation of the specific complex



$^{15}\text{N}-\text{H}$ -correlation spectra indicate that the structure of the specific complex does not change significantly when going from 20 mM to 160 mM salt!

Structural representations of the measured intermolecular PRE profiles.

At 20 mM NaCl, the data is compatible with the structure of the complex bound to the specific site.

At 160 mM NaCl the observed PRE are interpreted as footprints of minor species that are in rapid exchange with the specific complex.