

NMR course at the FMP:  
NMR of organic compounds and  
small biomolecules

- II -

16.03.2009

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AG Solution NMR

## The program

CW vs. FT NMR

What is a pulse ?

Vectormodel

Water-  
flip-back

# CW vs. FT

## CW vs. FT

Two methods exist to record NMR spectra, which differ substantially in the way the spectrum is acquired:

**CW-Technik**

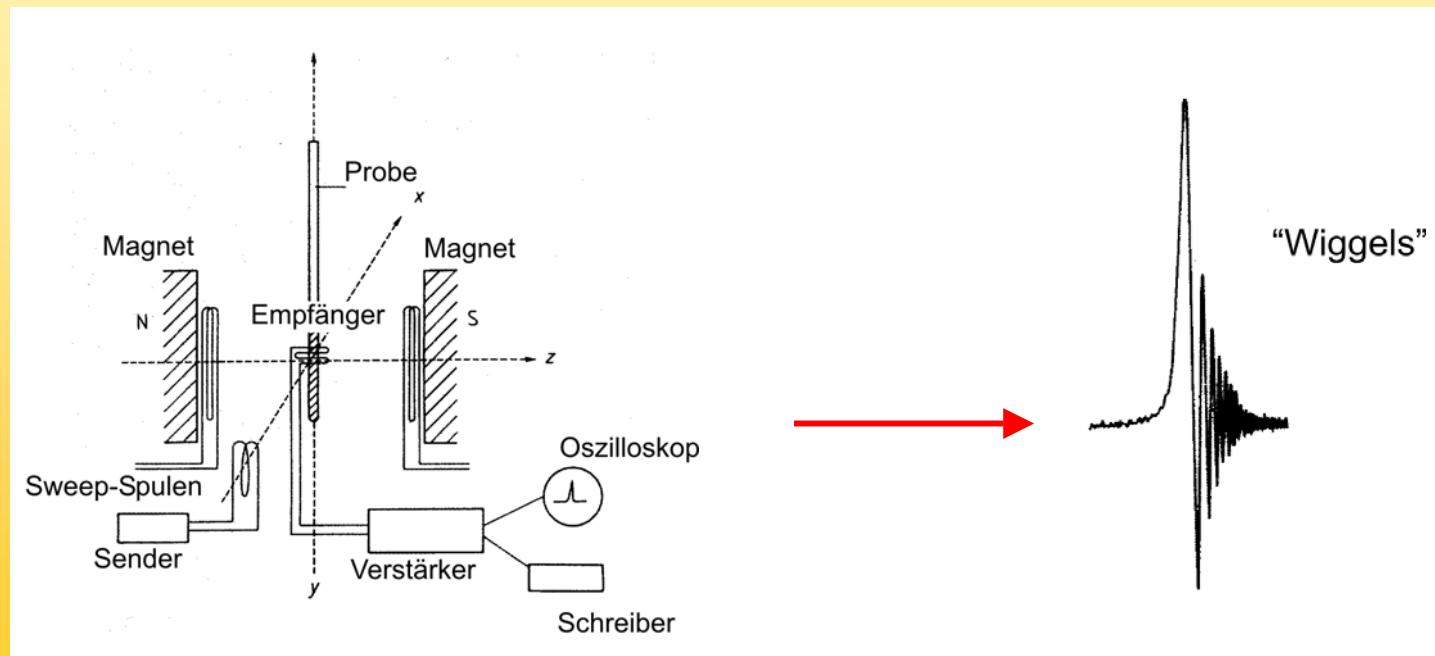
(continuous wave)

**FT-Technik**

(fourier transform)

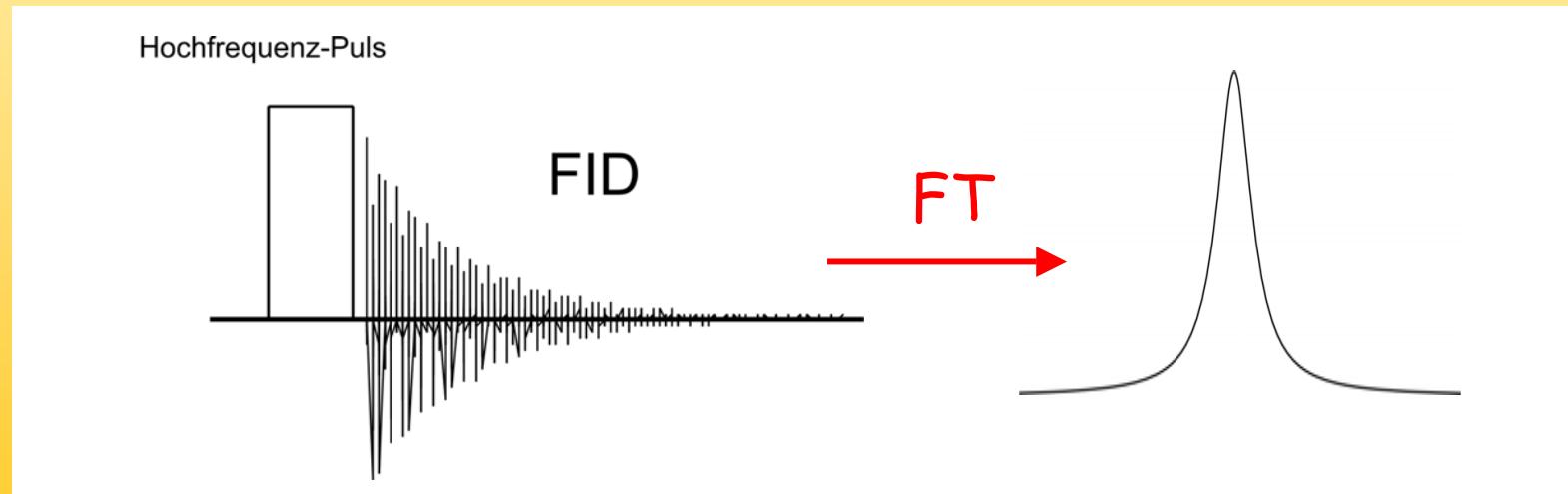
## CW vs. FT

The CW-technique is the „typical“ methods, but it is hardly used these days because of the signal-to-noise problem in NMR

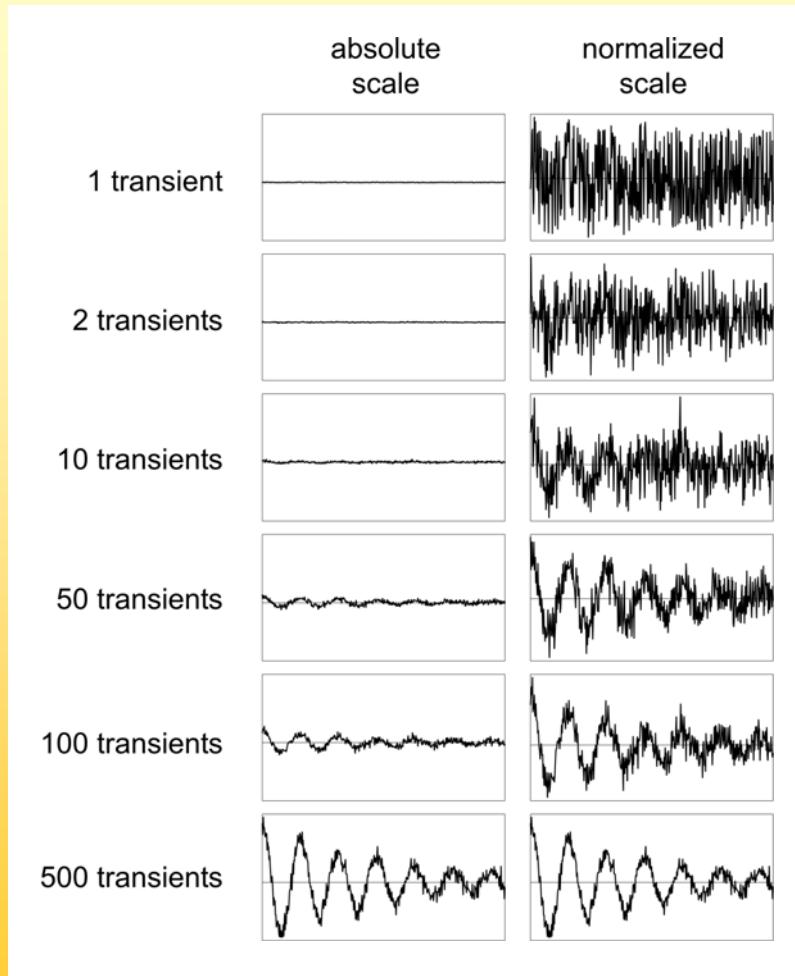


## CW vs. FT

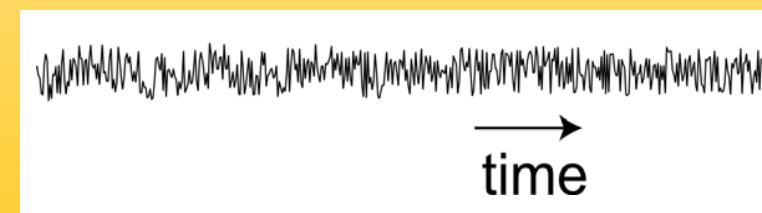
Modern NMR spectrometer all work with the FT-NMR-technique, which is also called „pulsed NMR“ and which makes it easier to improve the signal-to-noise ratio...



## CW vs. FT



.... by repetition and  
addition of the  
experiment



# What is a pulse

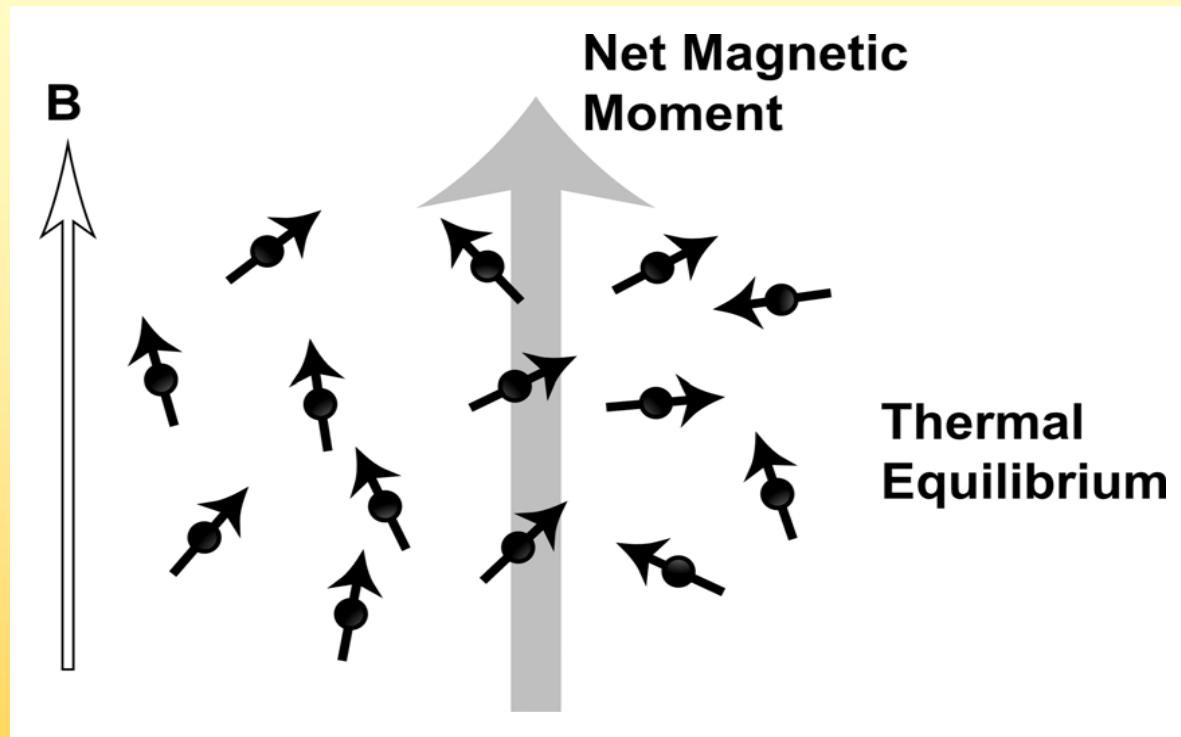
## What is a pulse

With respect to the FT-technique a pulse is an important tool to manipulate spins.

But how can the relatively weak field of the pulse have such an effect when the much larger static field is always present.

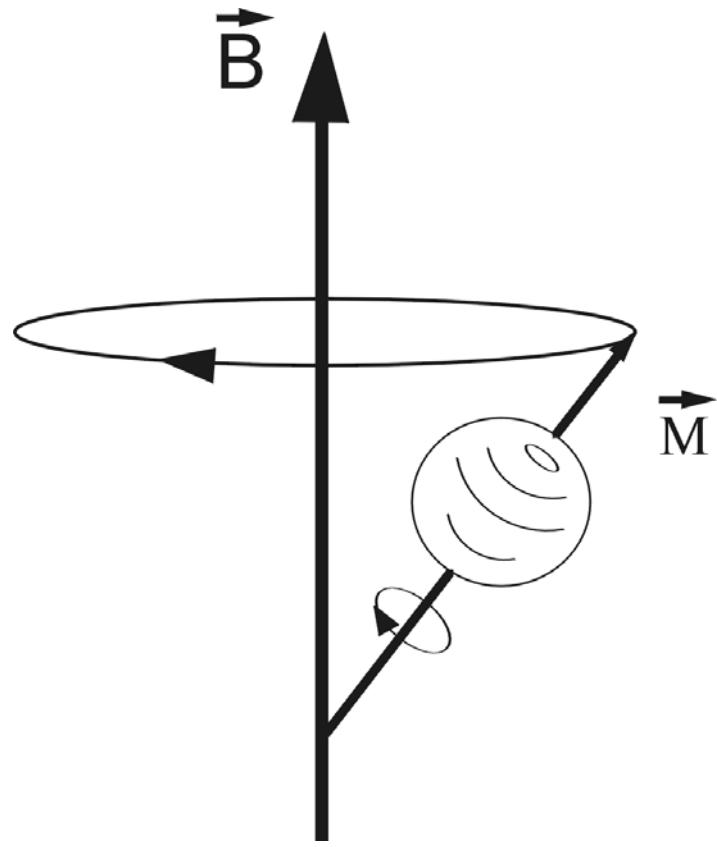
This is a typical resonance phenomenon which can be explained with the concept of the „rotating coordinate system“

## What is a pulse



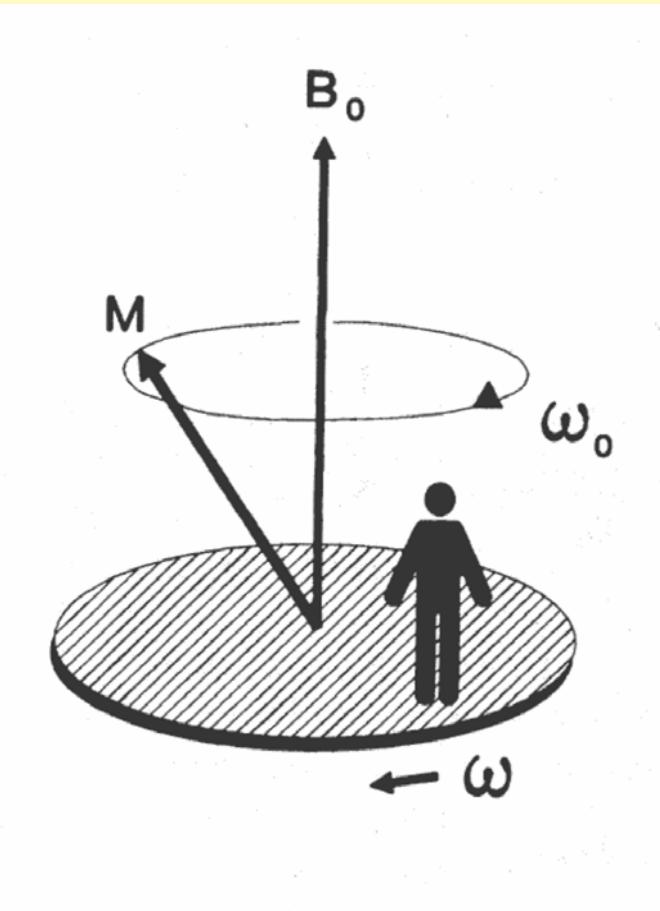
Starting point is the z-magnetization that results from the Boltzmann distribution

## What is a pulse



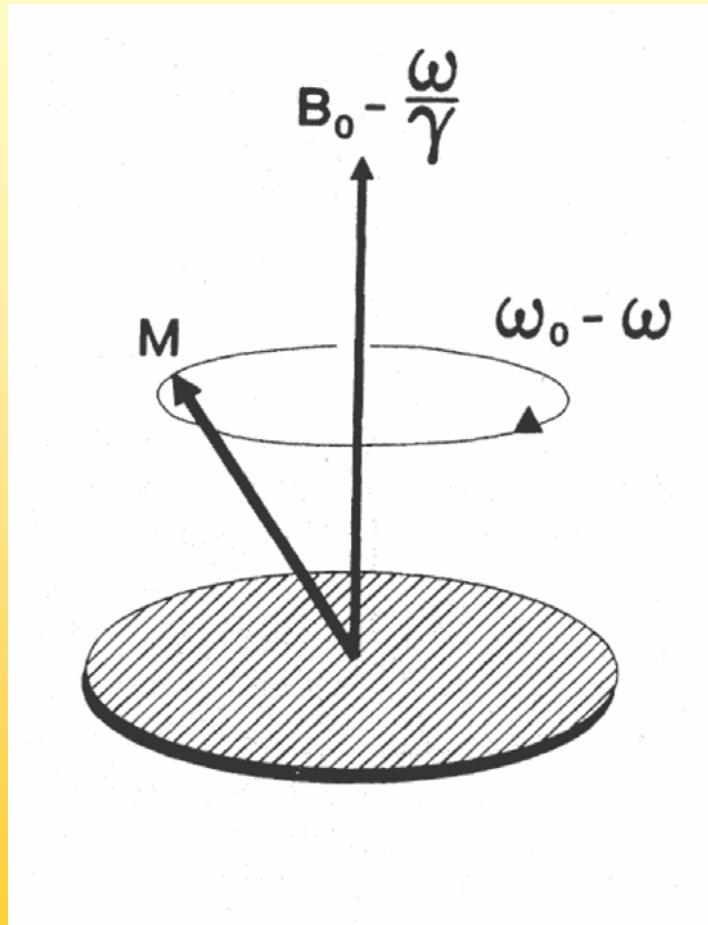
The nuclear spin are rotating around the magnetic field provided by the magnet

## What is a pulse



The concept of a rotating coordinate system is easy to grasp when we remind our self that we live on a rotating object our self. The observer rotates with a speed  $\omega$  the spin with a speed  $\omega_0$ .

## What is a pulse



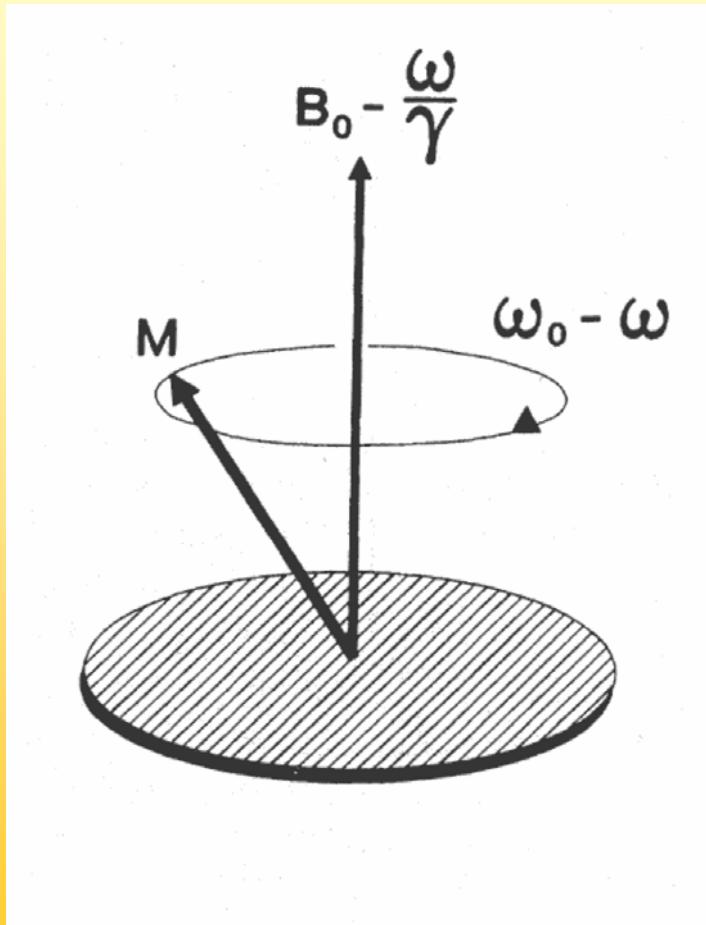
The movement of the spins (the rotation) is caused by the magnetic field

$$\omega_0 = 2\pi v_0 = \gamma B_0$$

Is the movement slower the observer has to conclude that the magnetic field is weaker

$$\omega_0 - \omega = \Omega = \gamma (B_0 - \omega/\gamma)$$

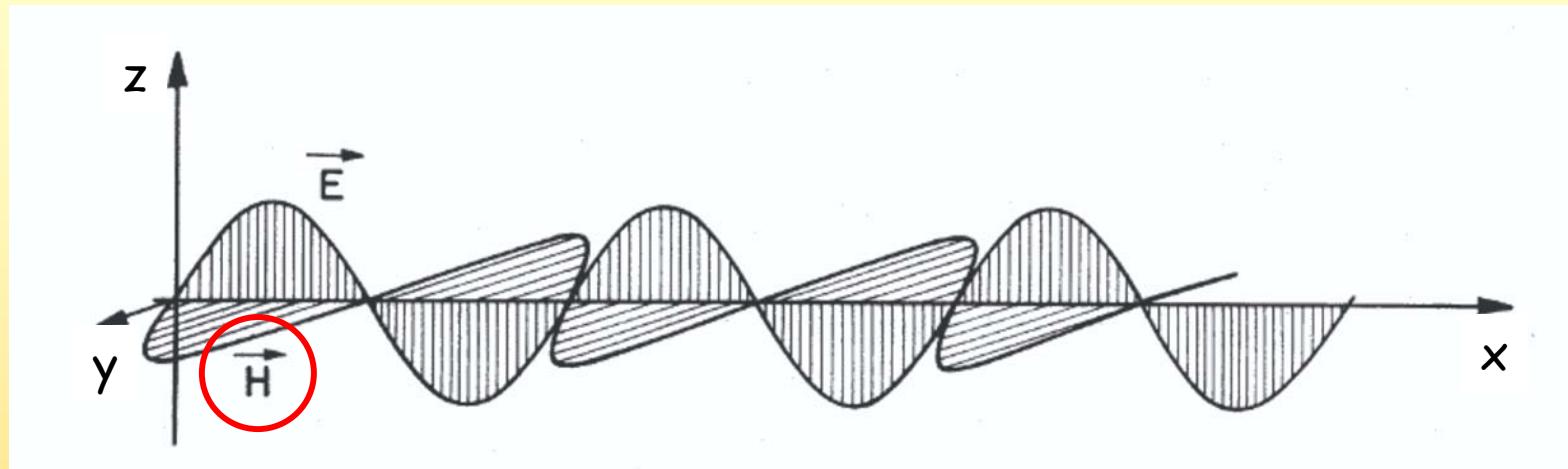
## What is a pulse



Within this concept also negative frequencies are possible, i.e. rotations in the other direction

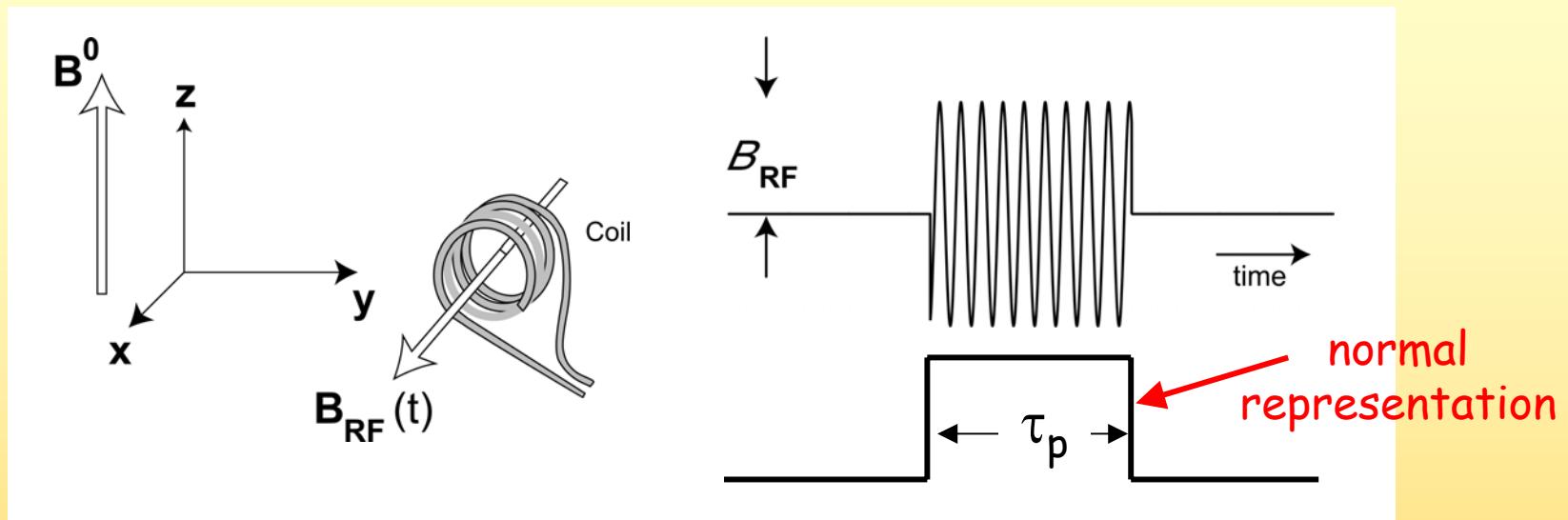
No movement means no magnetic field !!

## What is a pulse



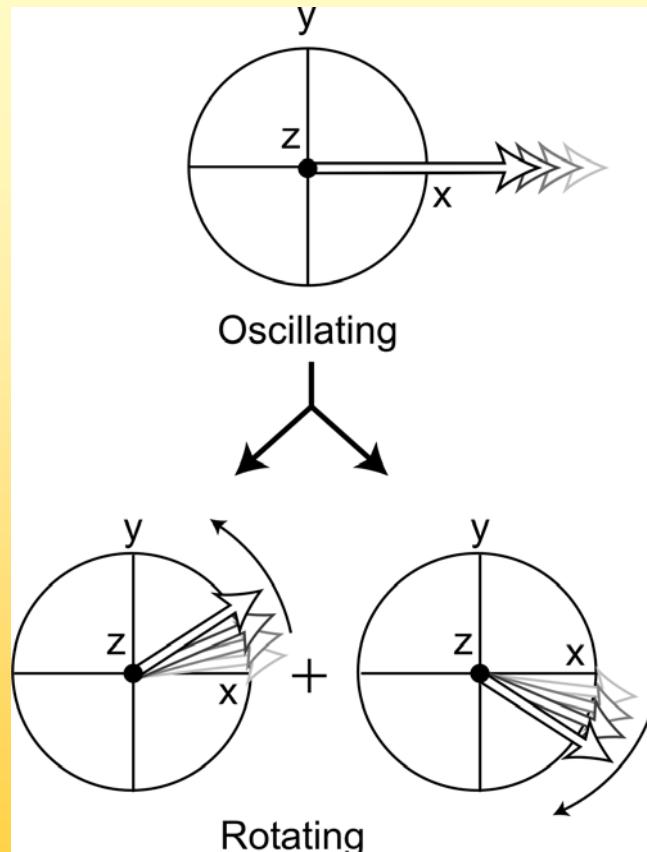
The pulse itself is the irradiation of radio waves. They are linearly polarized and have an electric and a **magnetic** component, only the latter is of interest here.

## What is a pulse



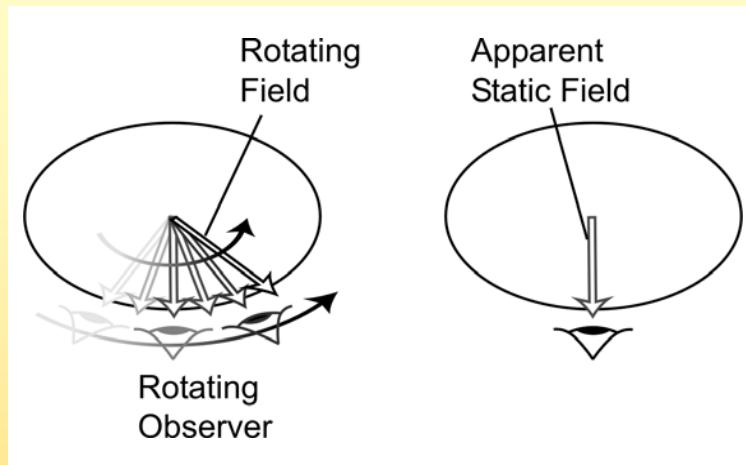
The irradiation uses the coil, radio waves are sent to the sample in form of a „pulse“, i.e. a short RF-burst.  
The field is in the x,y-plane

## What is a pulse



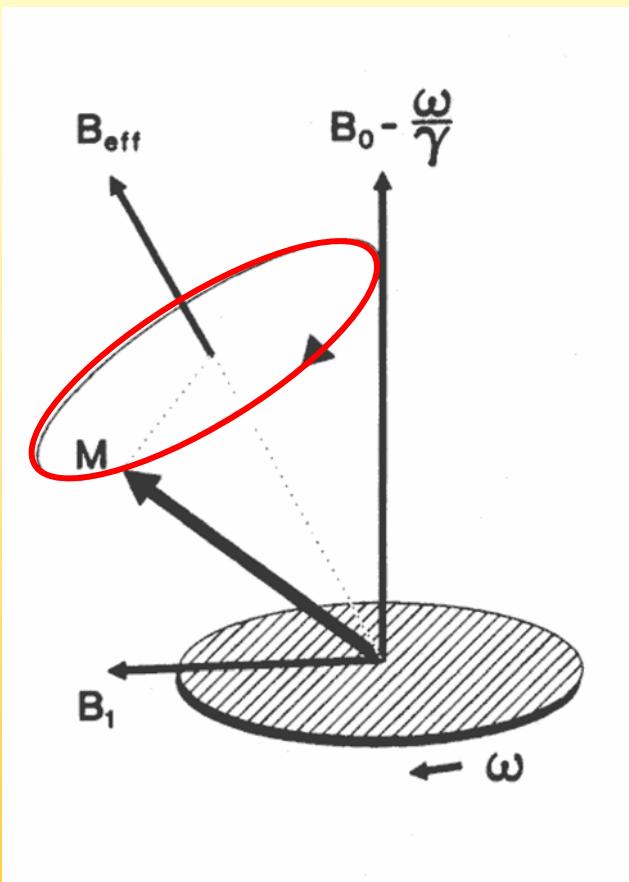
A linearly polarized oscillation can be split into two components rotating in opposite directions. One component is quite fast in the rotation coordinate system and will be ignored....

## What is a pulse



.... while the other is almost static in the rotating coordinate system, it is „on resonance“ or at least close, it is called the  $B_1$ -field

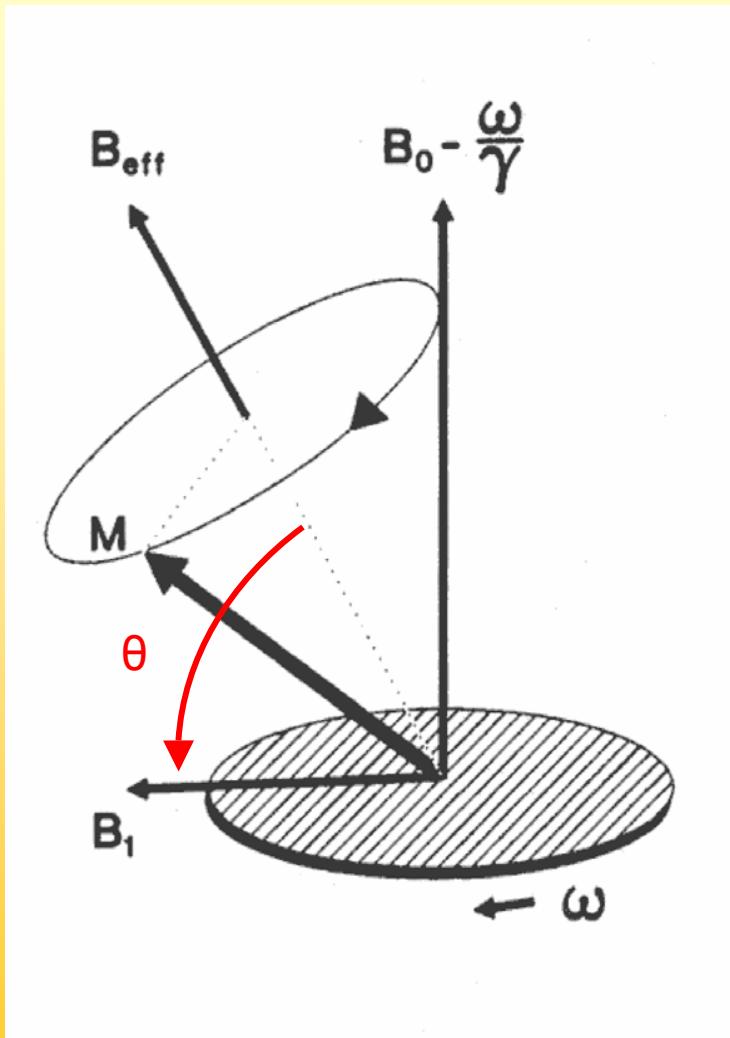
## What is a pulse



In the rotating coordinate system we then have a weakened static  $B_0$  field and a relatively strong  $B_1$  field which ends up being of similar strength close to resonance.

The movement of the magnetization is now determined by the new „effective field“,  $B_{\text{eff}}$

## What is a pulse



Strength and tilt angle of the effective field  $B_{\text{eff}}$  are easily calculated

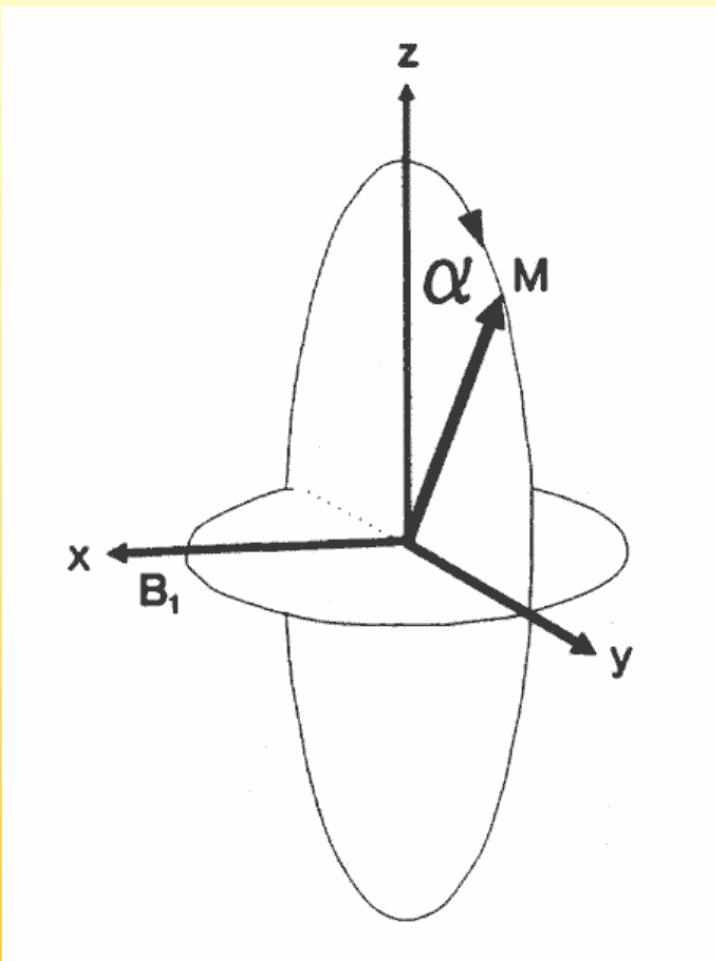
$$B_{\text{eff}} = \sqrt{(B_1)^2 + (B_0 - \omega/\gamma)^2}$$

$$\gamma B_{\text{eff}} = \sqrt{(\gamma B_1)^2 + \Omega^2}$$

$$\tan \theta = \frac{(B_0 - \omega/\gamma)}{B_1} = \frac{\Omega}{\gamma B_1}$$

$$B_{\text{eff}} \geq B_1$$

## What is a pulse



If the frequency of the pulse matches that of the spin („on resonance“) the main field vanished and the precession is only around the  $B_1$ -field.

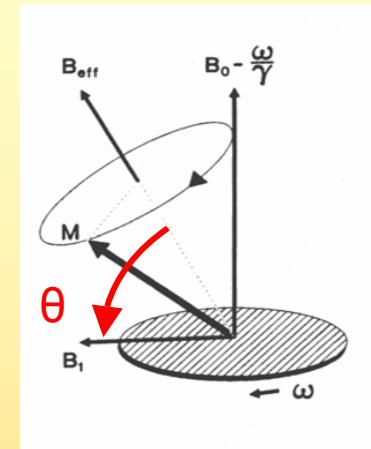
The angle  $\alpha$  is determined by the length and the strength of the pulse: A typical value for a  $90^\circ$  Puls is 10  $\mu$ sec

## What is a pulse

frequency 600 MHz

90° Puls = 10  $\mu$ sec

$\gamma B_1 = 25$  kHz



3000 Hz

10 ppm

0 Hz

5 ppm

-3000 Hz

0 ppm

on-resonance

$\Omega = 3000$

$\tan \theta = 0.12$

$\theta = 6.8^\circ$

$\Omega = 0$

$\tan \theta = 0$

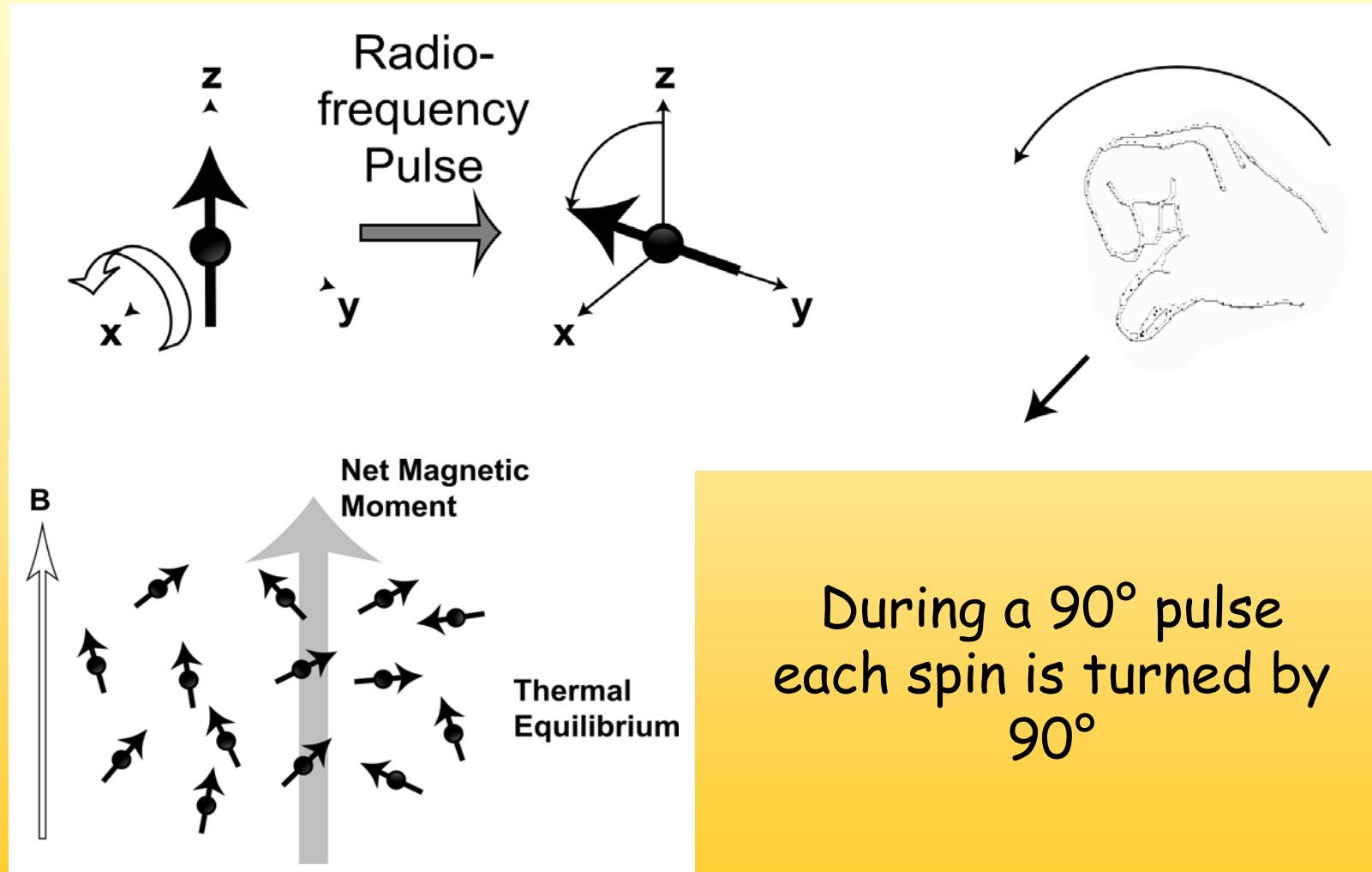
$\theta = 0$

$\Omega = -3000$

$\tan \theta = -0.12$

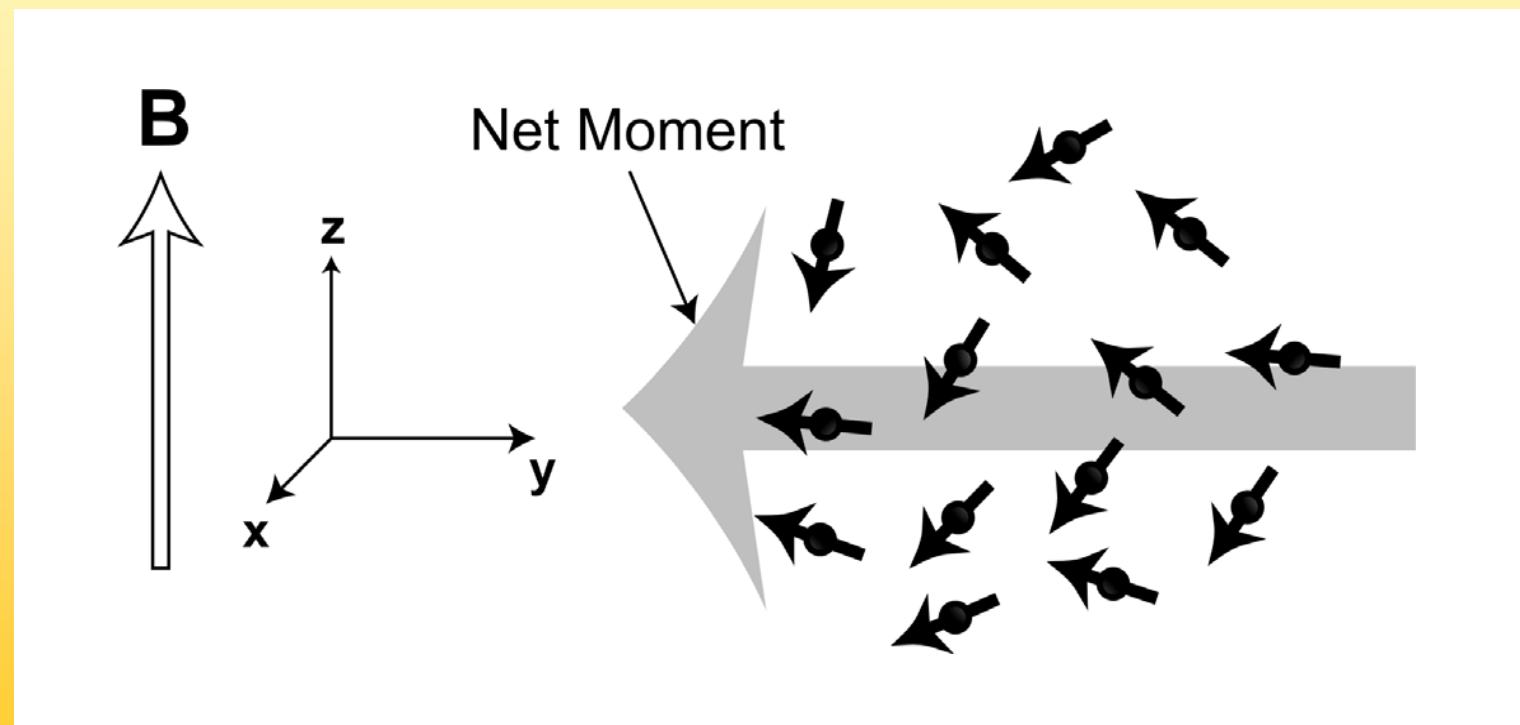
$\theta = -6.8^\circ$

## What is a pulse



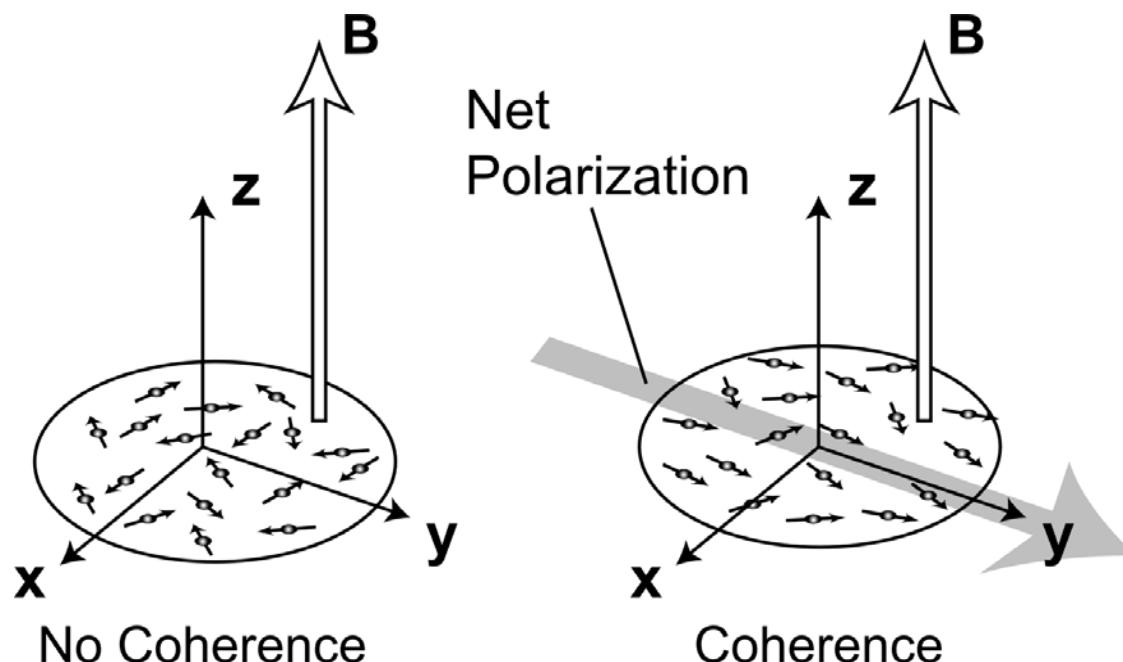
## What is a pulse

The resulting magnetic moment is positioned in the x,y-plane, no z-magnetization is present



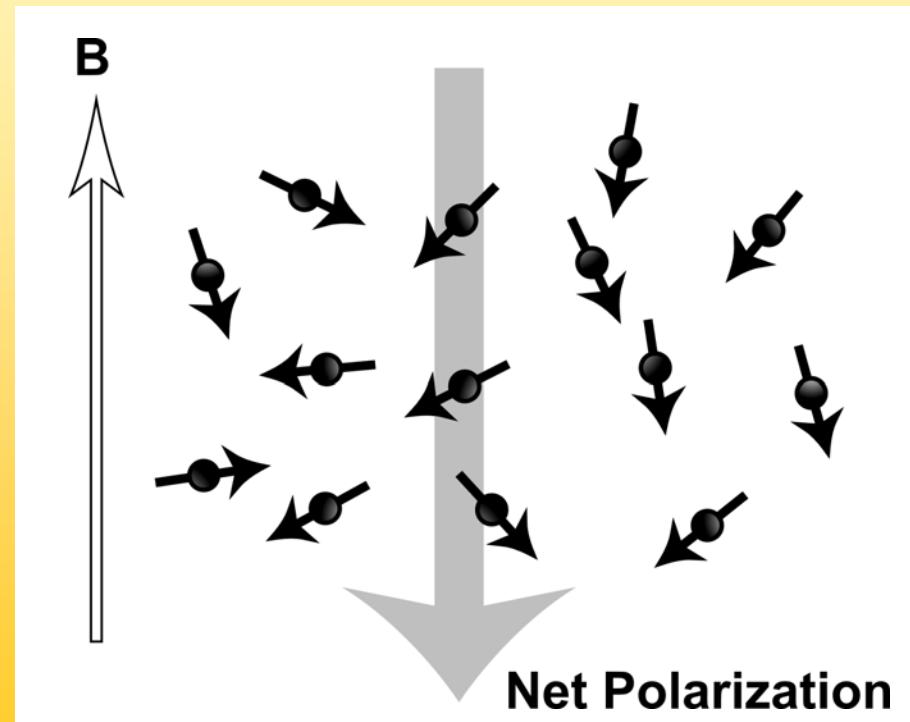
## What is a pulse

But: This is not the same as a simple saturation that leads to equal occupation of both energy levels, here we have a coherent movement of the spins.



## What is a pulse

If we irradiate longer we go beyond the  $90^\circ$  angle and reach  $180^\circ$  at some point



# The vector model

## The vector model

The vector model is a semi-classical description of NMR experiments and works well with isolated spins, i.e. spins without scalar coupling.

The mathematical formalism attached to it are the Bloch equations

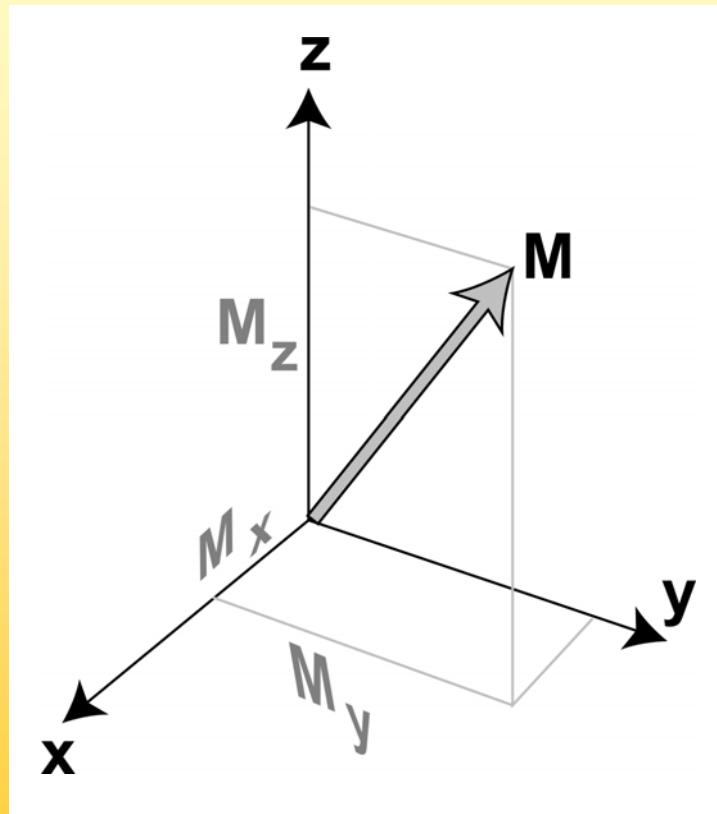
F. Bloch *Phys. Rev.* **70**, 460 - 474 (1946)

## The vector model

In case of scalar coupling it is only usefull within certain limits. Since many multidimensional experiments are based on the transfer of magnetization via scalar coupling it is suitable there.

It is, however, well suited for the description of simple 1D pulse sequences and relaxation phenomena.

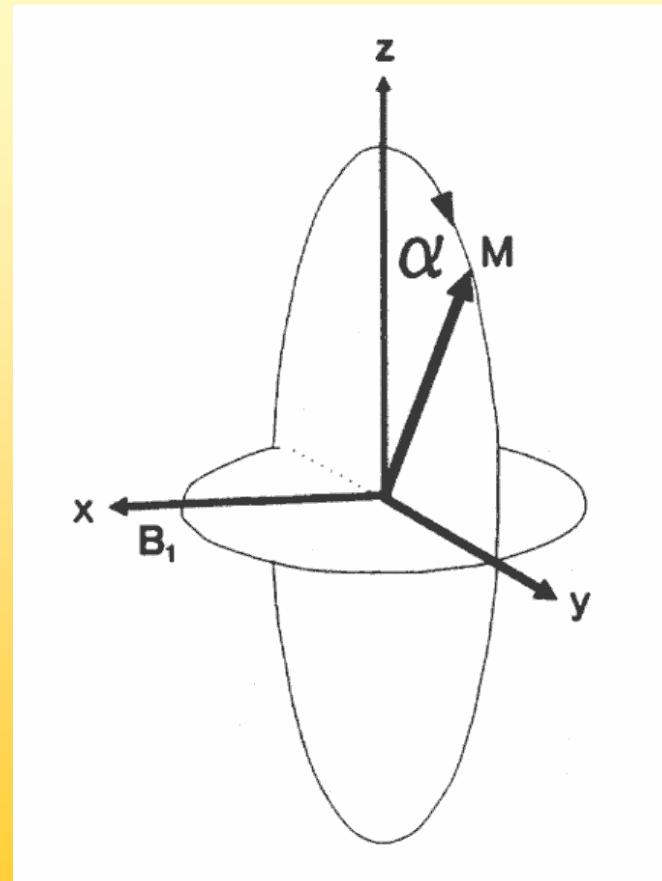
## The vector model



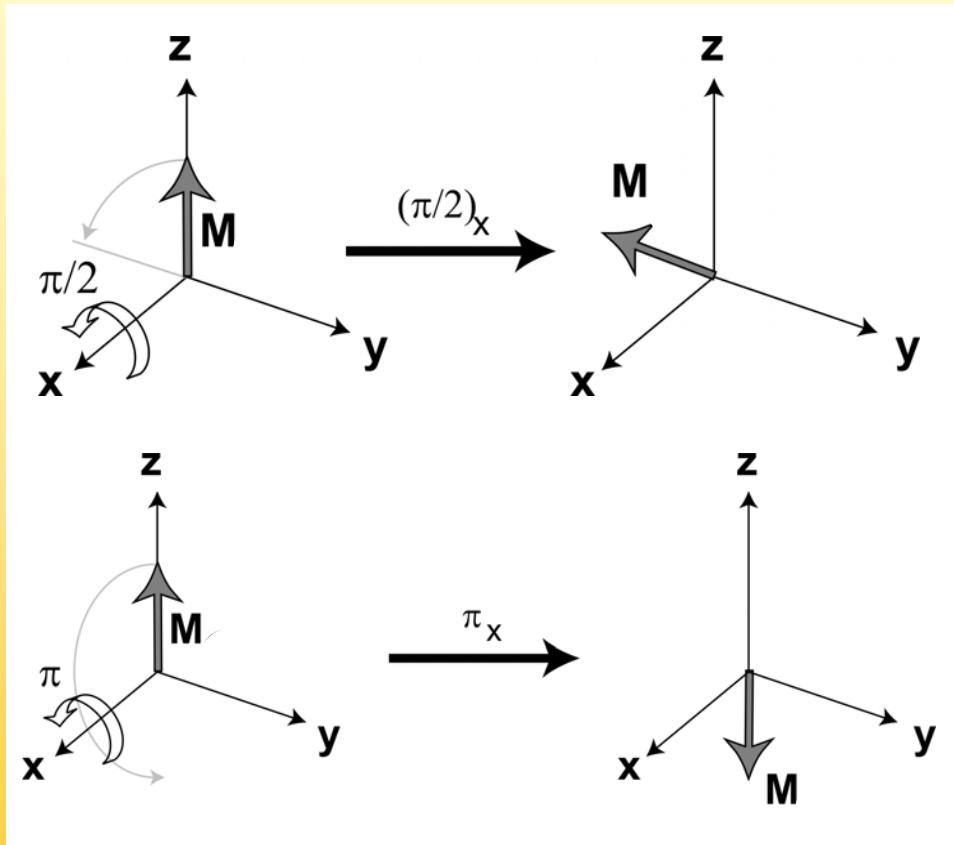
Magnetization is considered to be a vector that can be manipulated following the rules of vector manipulation using magnetic fields

## The vector model

The first kind of magnetic field are pulses



## The vector model

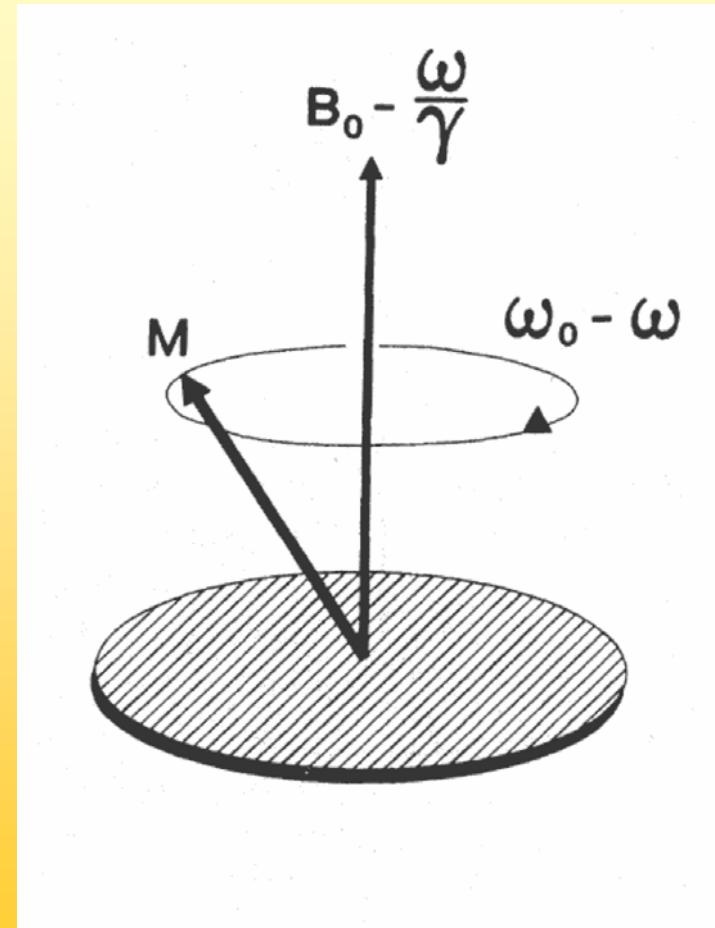


$90^\circ$  pulse from x:  
the vector turns  
around the x-axis  
to (-y)

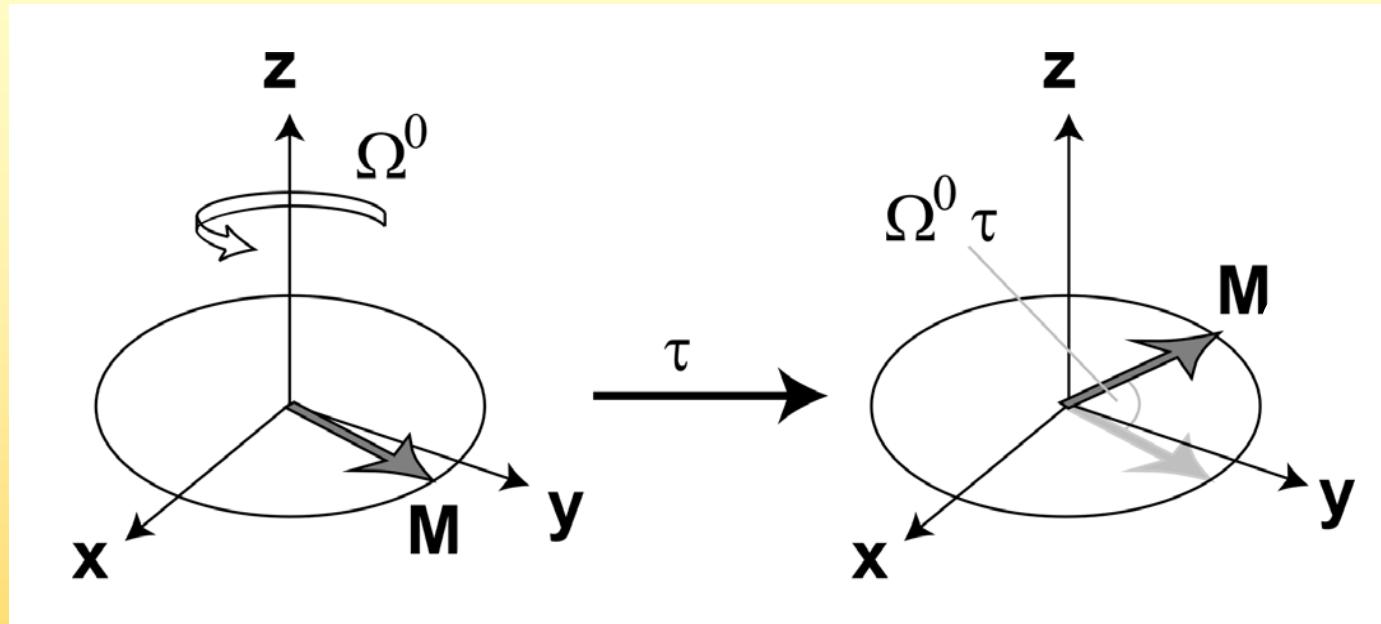
$180^\circ$  pulse from x:  
the vector turns  
around the x-axis  
to (-z)

## The vector model

The second kind of magnetic field is the main or  $B_0$ -field, that causes chemical shift and scalar coupling



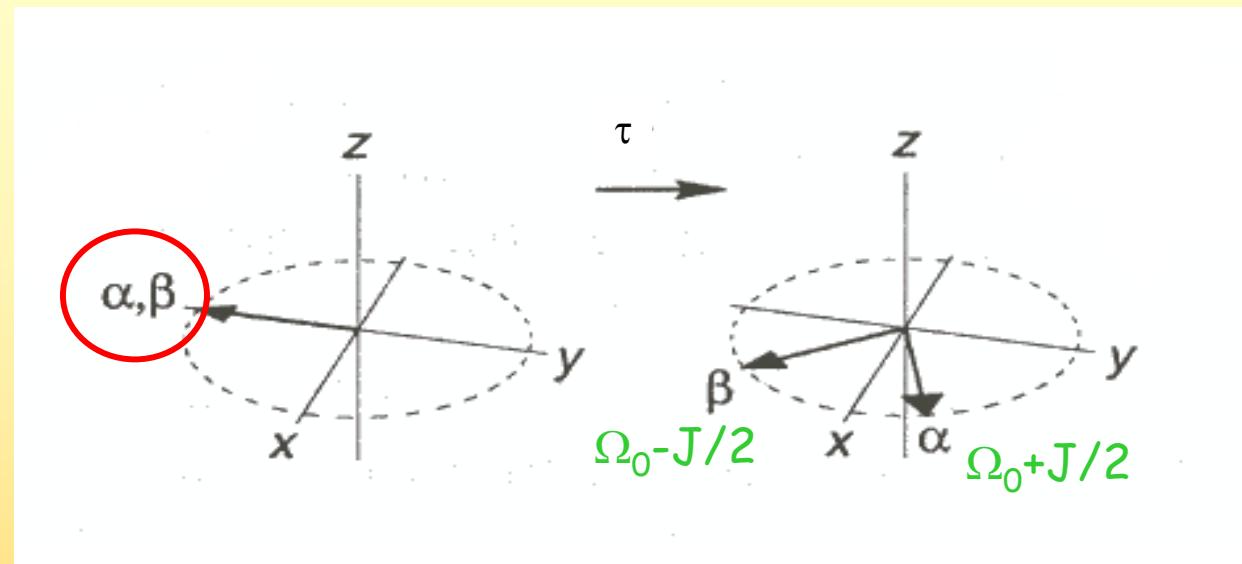
## The vector model



Chemical shift only acts on x,y-magnetization and causes a rotation around the z-axis with a frequency  $\Omega_0$  (i.e. the chemical shift)

## The vector model

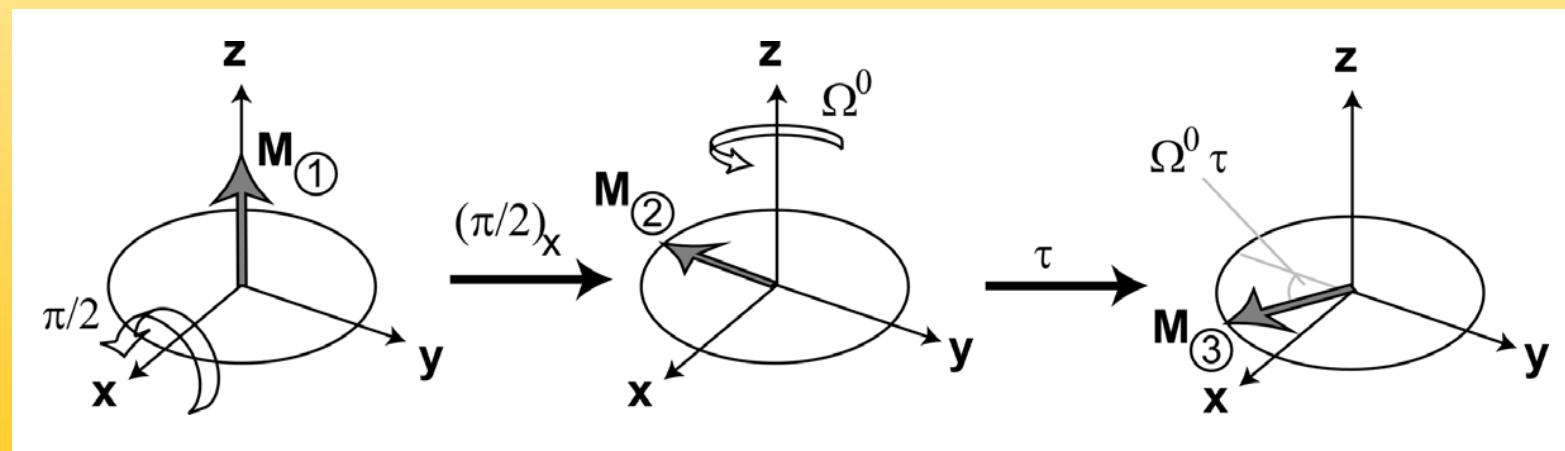
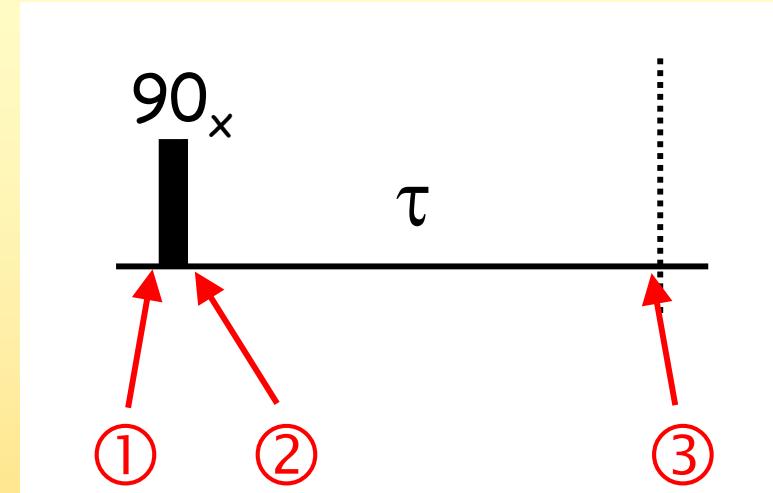
$\alpha, \beta$  characterises  
the spin state of  
the „other“ spin



Scalar coupling acts on  $x, y$ -magnetization as well and causes a rotation around the  $z$ -axis. The vector is split in two, one is moving  $J/2$  faster, the other slower than  $\Omega_0$

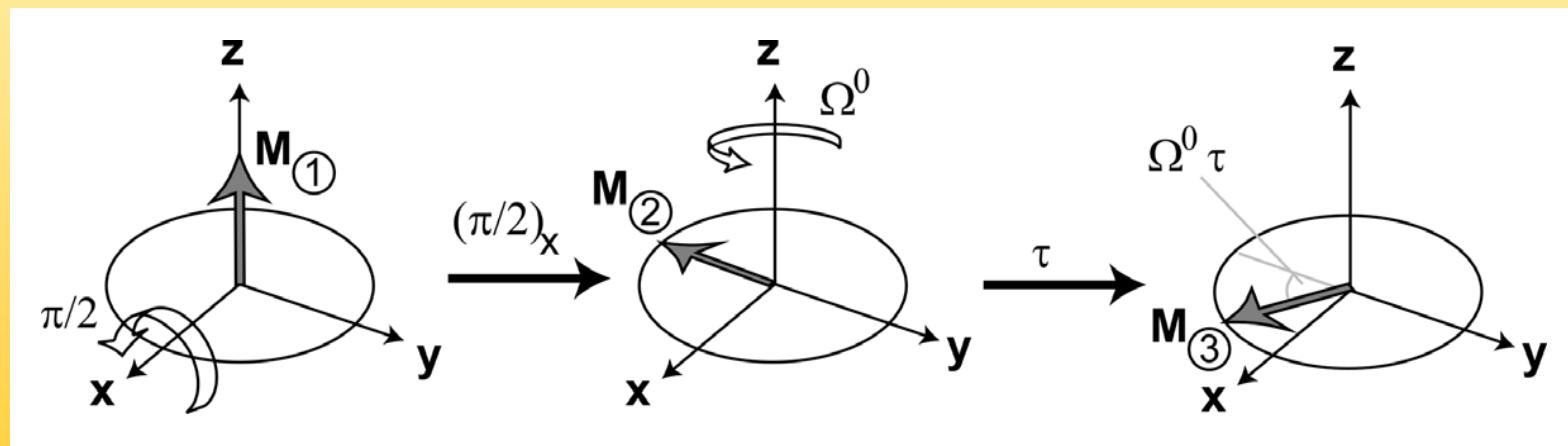
## The vector model

With these tools we can now start to analyze simple NMR sequences which are often building blocks of more complicated experiments

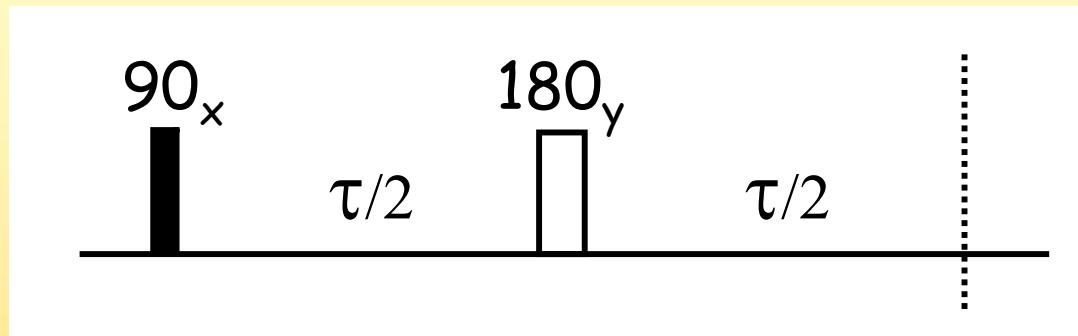


## The vector model

Spins with different chemical shifts reach different positions during the delay  $\tau$ . They will thus have different phases and no phase correction will be possible.

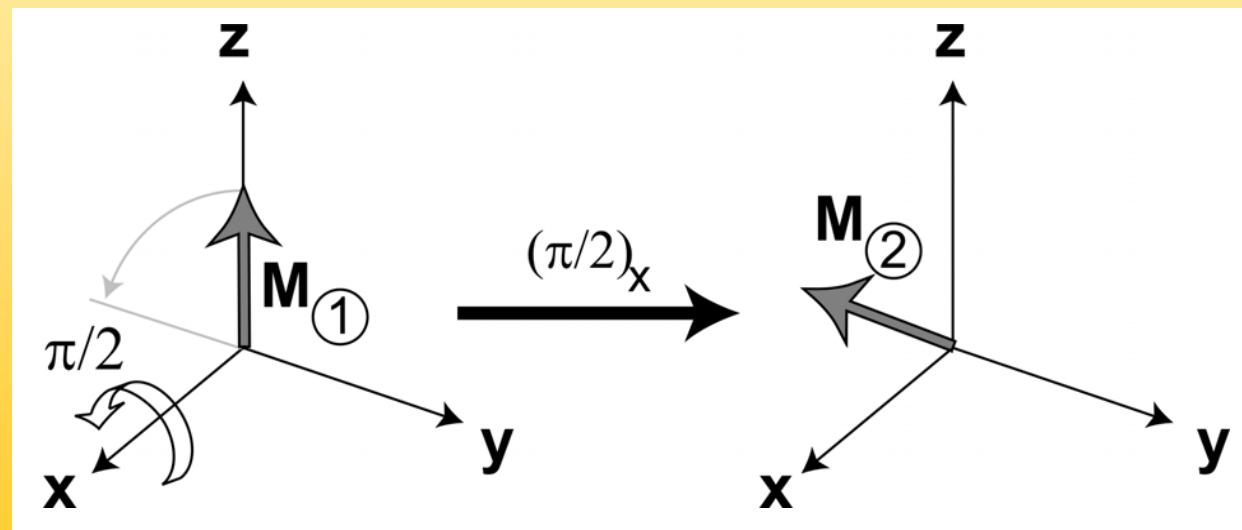
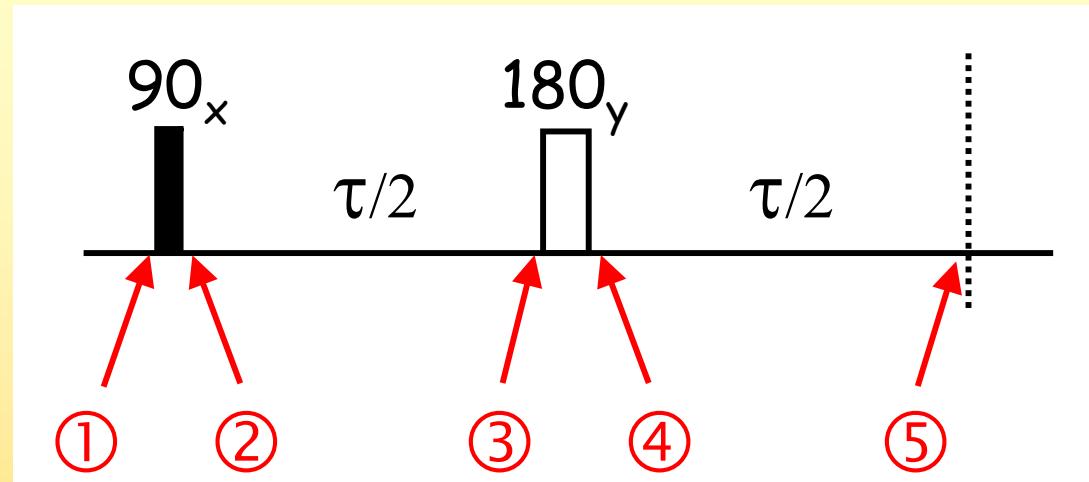


## The vector model

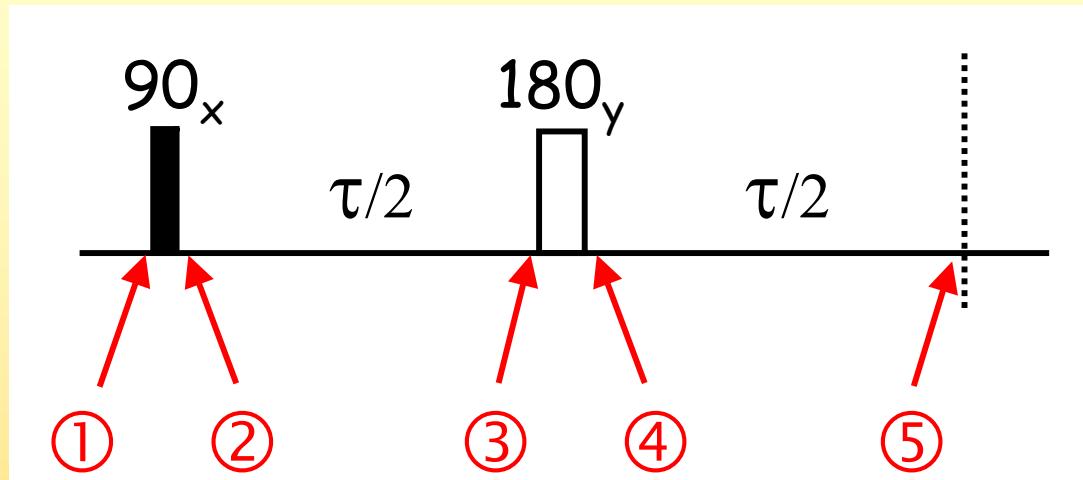


A simple sequence to prevent the evolution of chemical shift is the „spin echo“ that is also an important building block in many advanced experiments

## The vector model

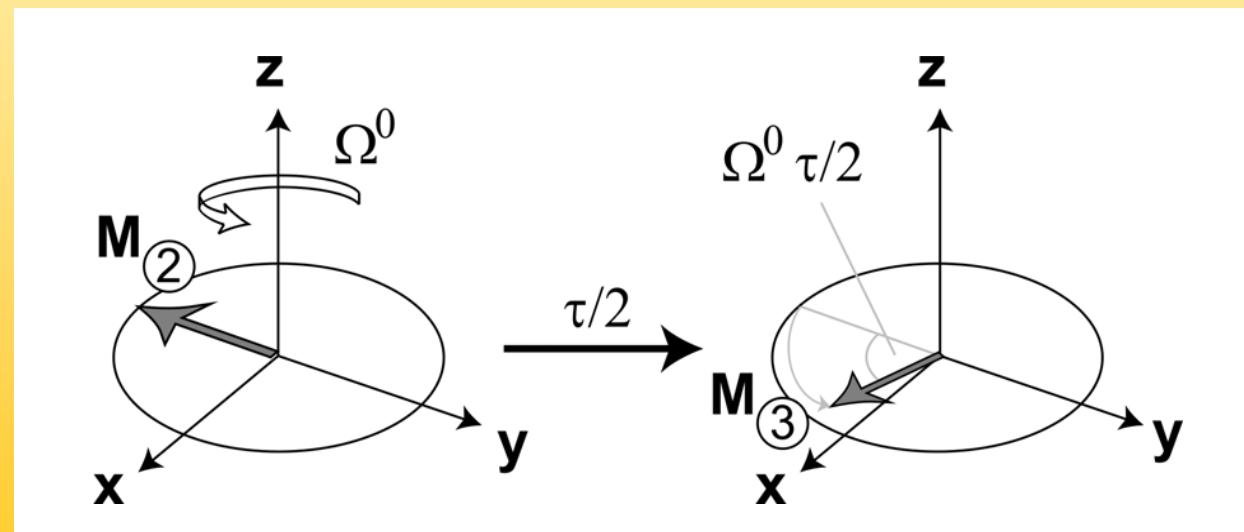
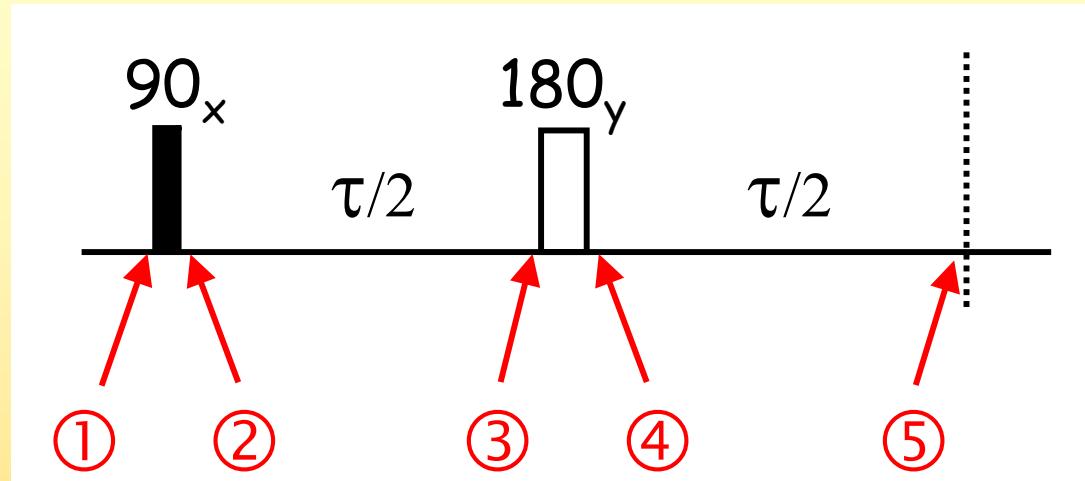


## The vector model

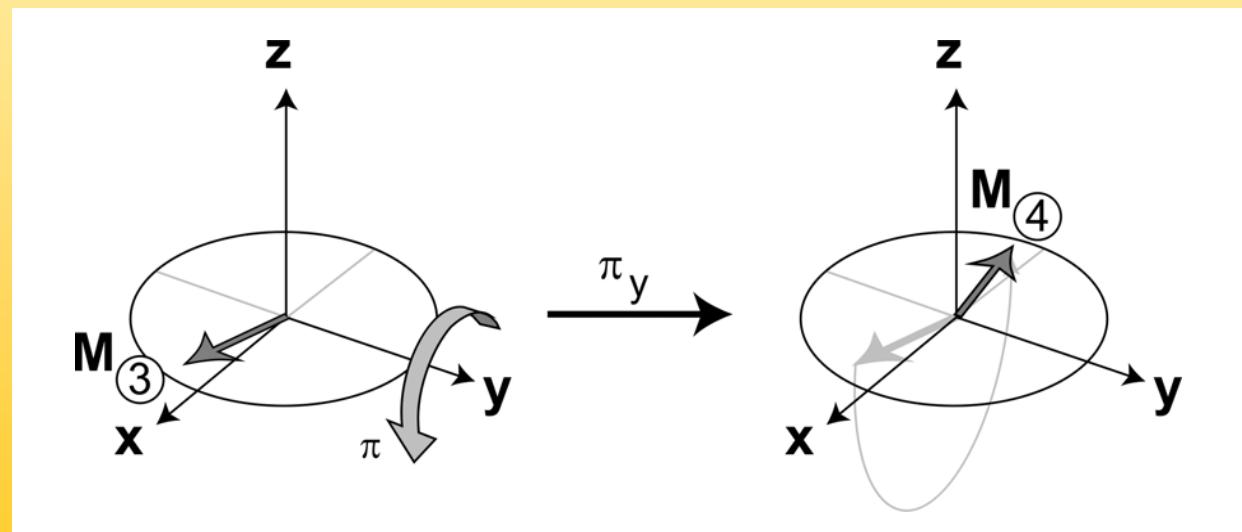
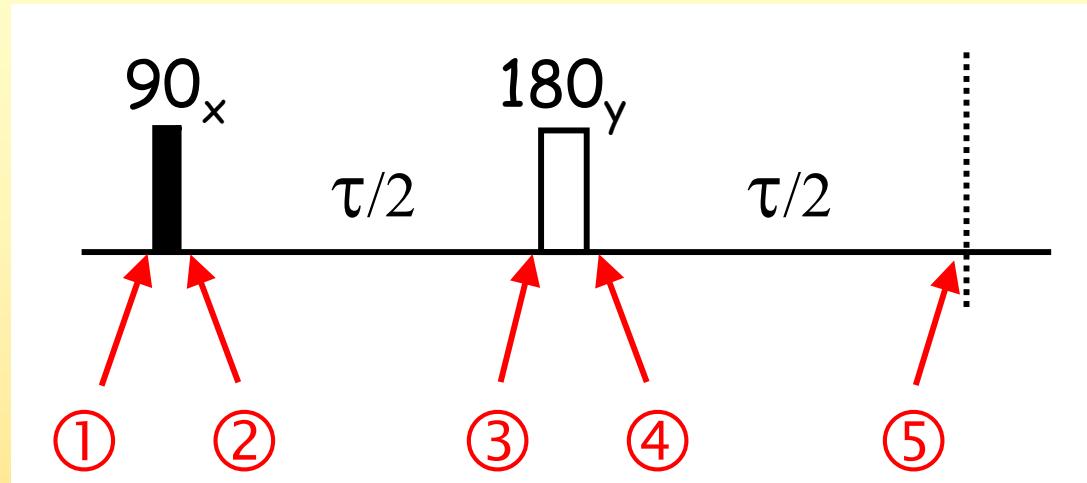


We will first only consider chemical shift and will treat scalar coupling separately

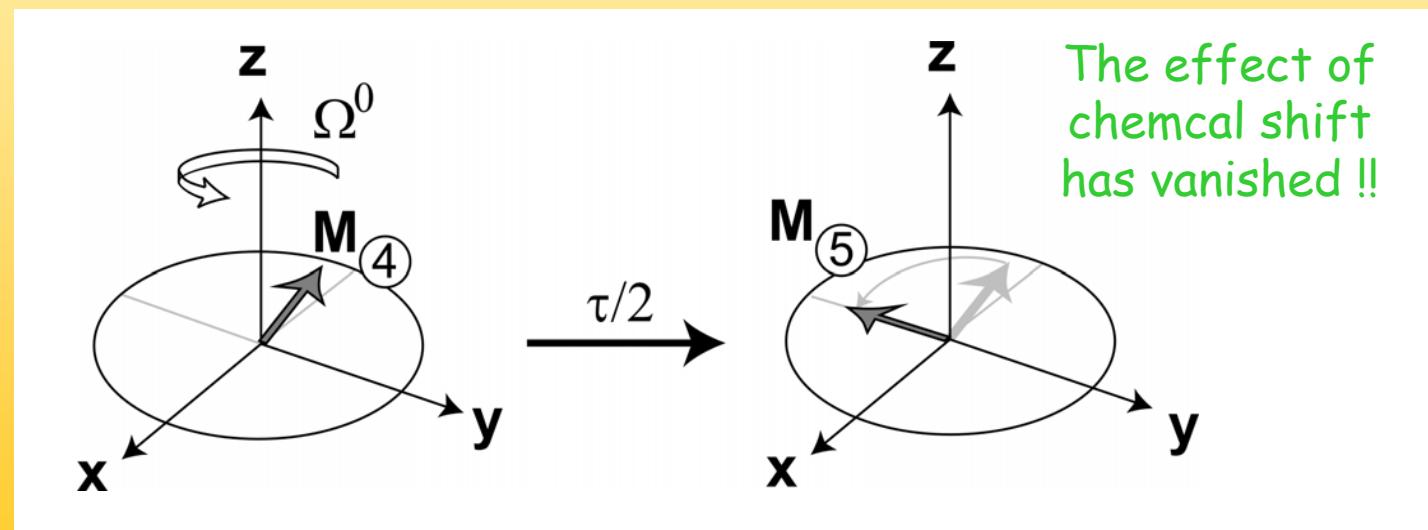
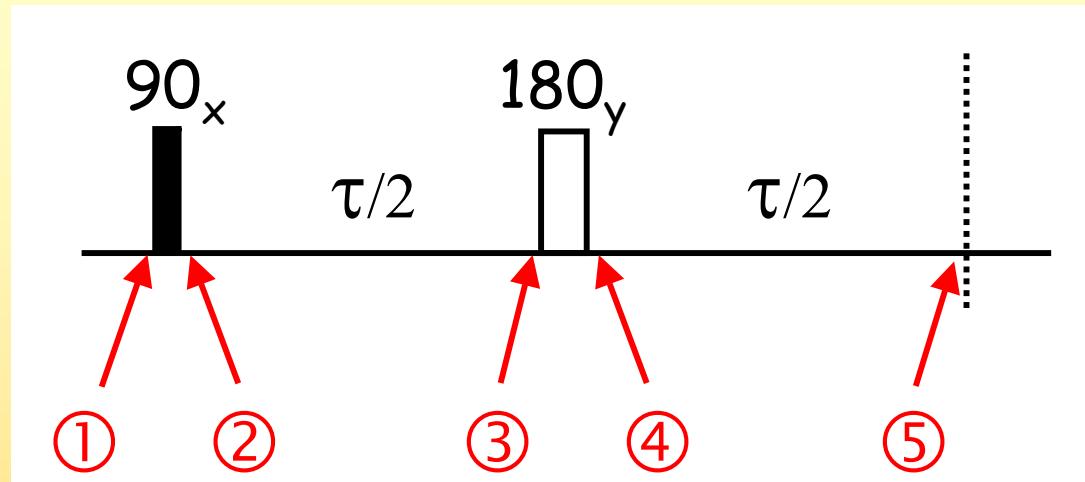
## The vector model



## The vector model

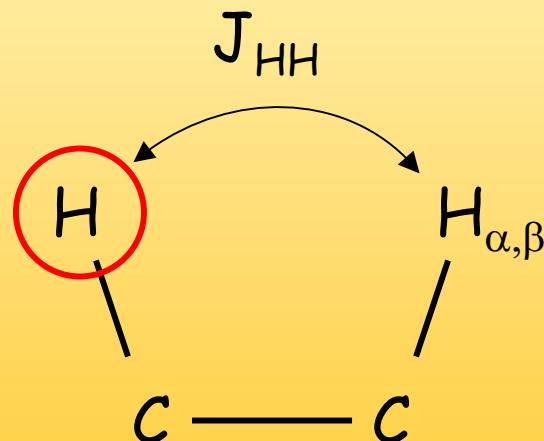


## The vector model

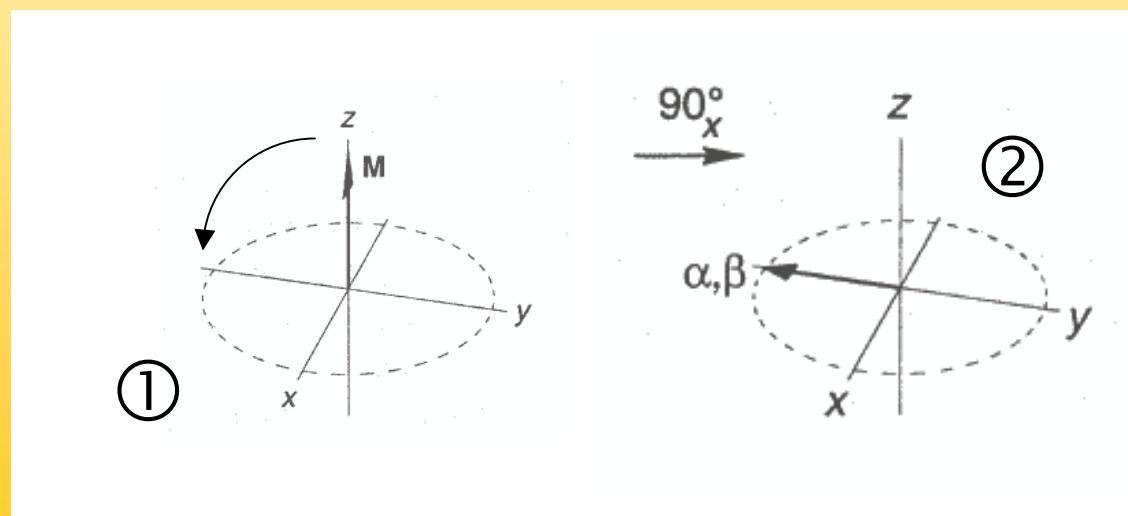
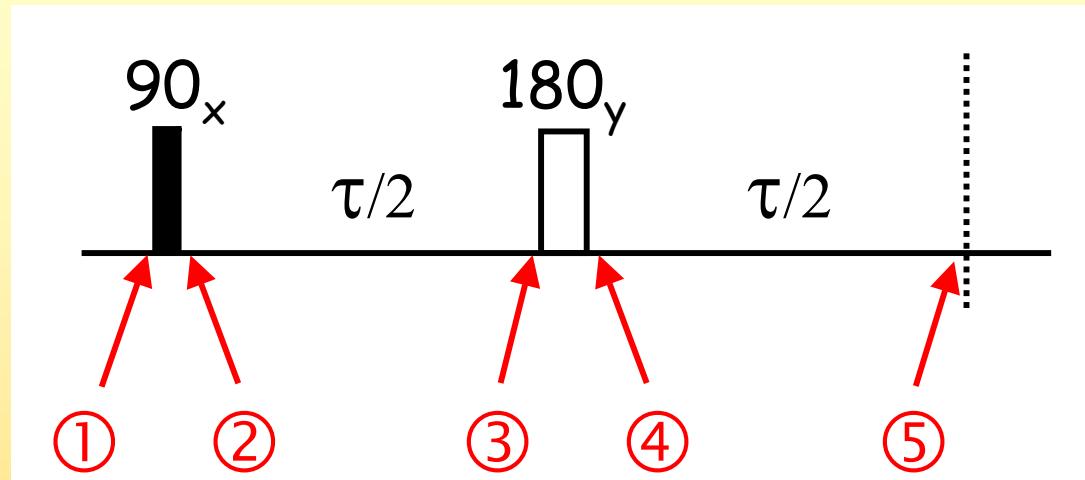


## The vector model

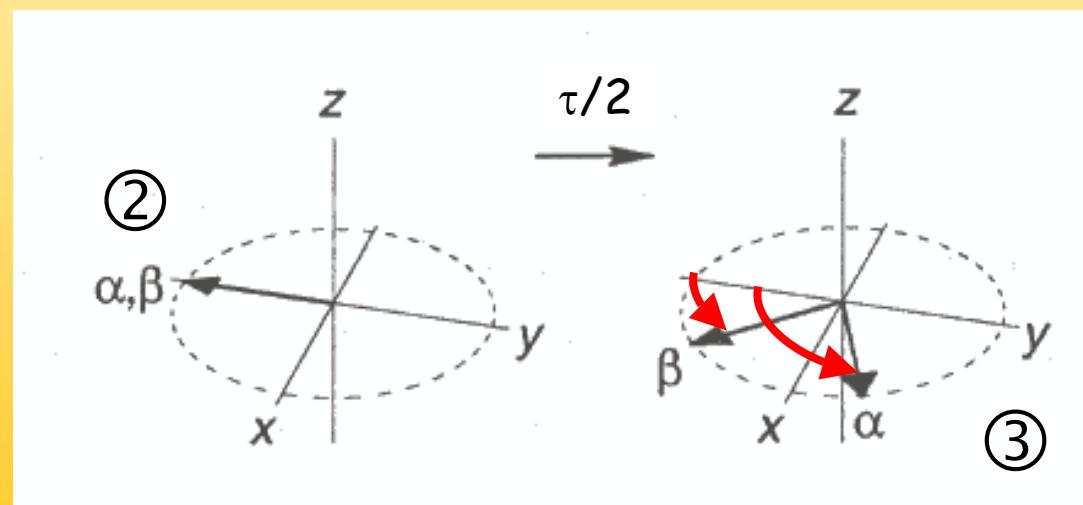
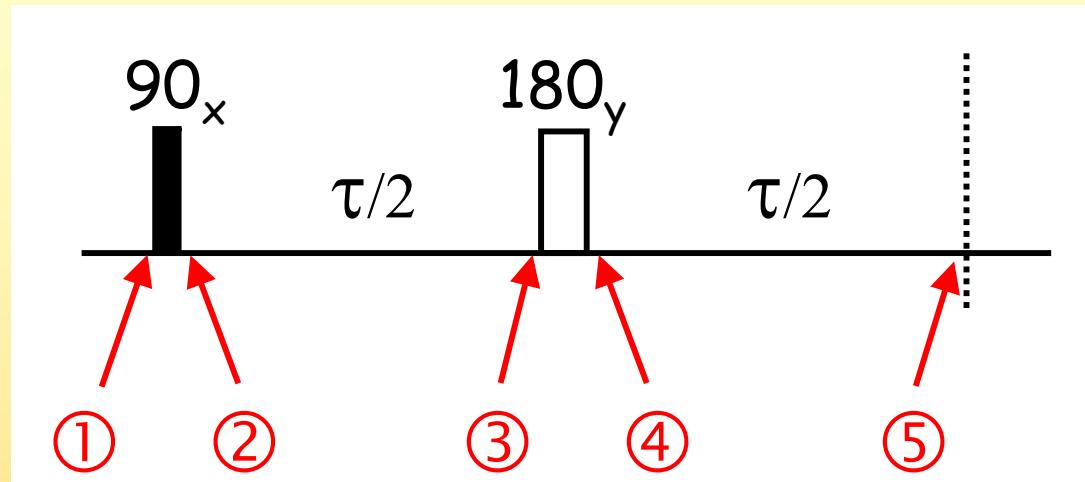
Now we consider homonuclear scalar coupling. A nucleus „sees“ the spin state of the other ( $\alpha$  oder  $\beta$ ) which results in two vectors of slightly different speed. The other spin experiences the  $180^\circ$  pulse as well



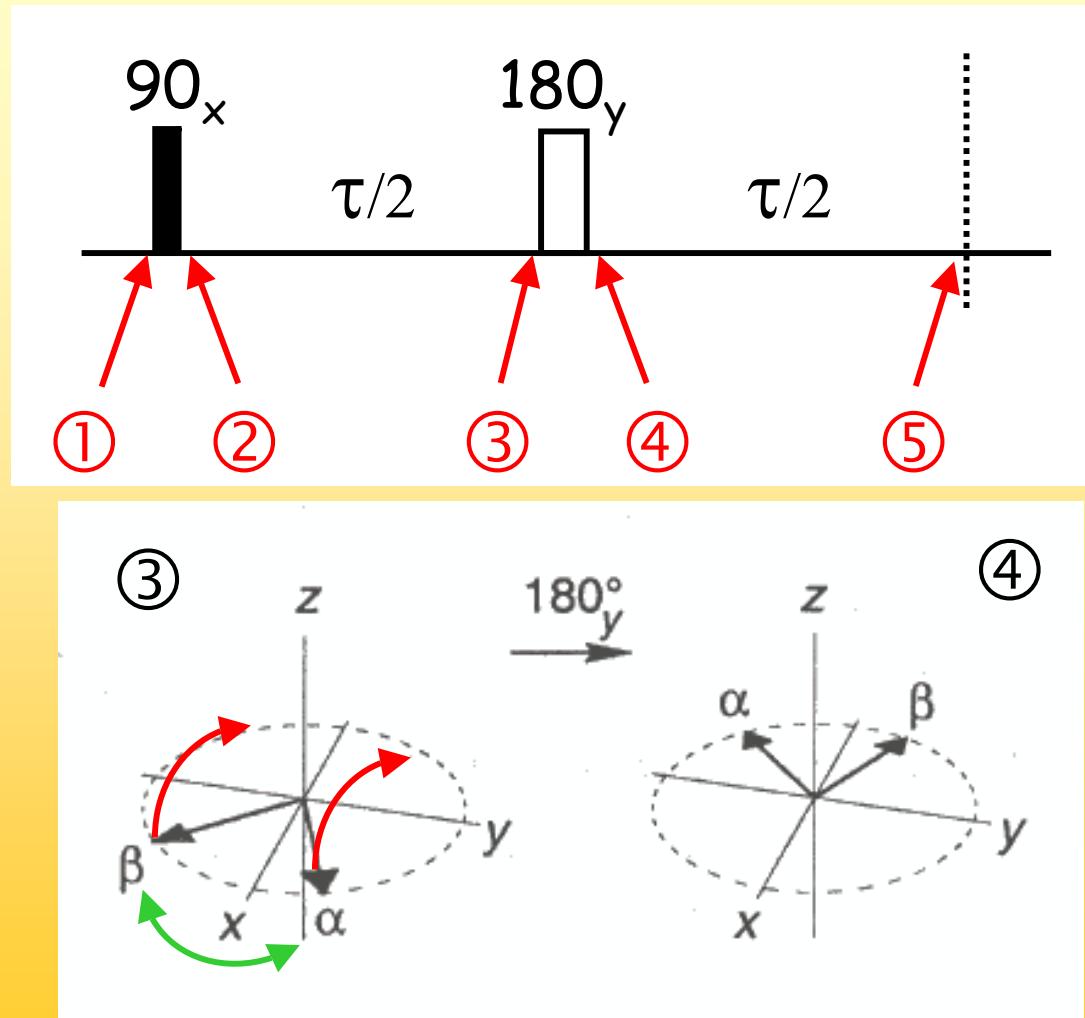
## The vector model



## The vector model

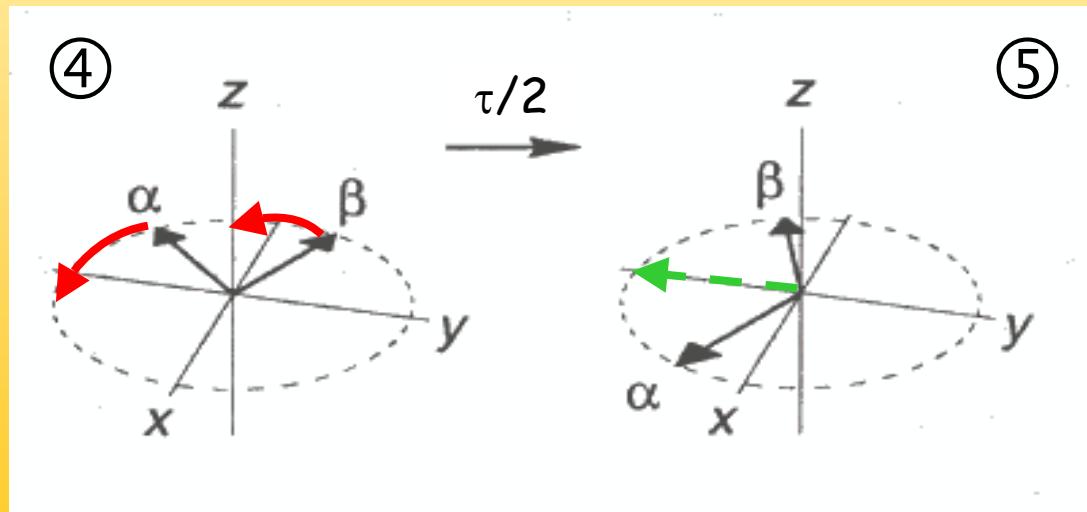
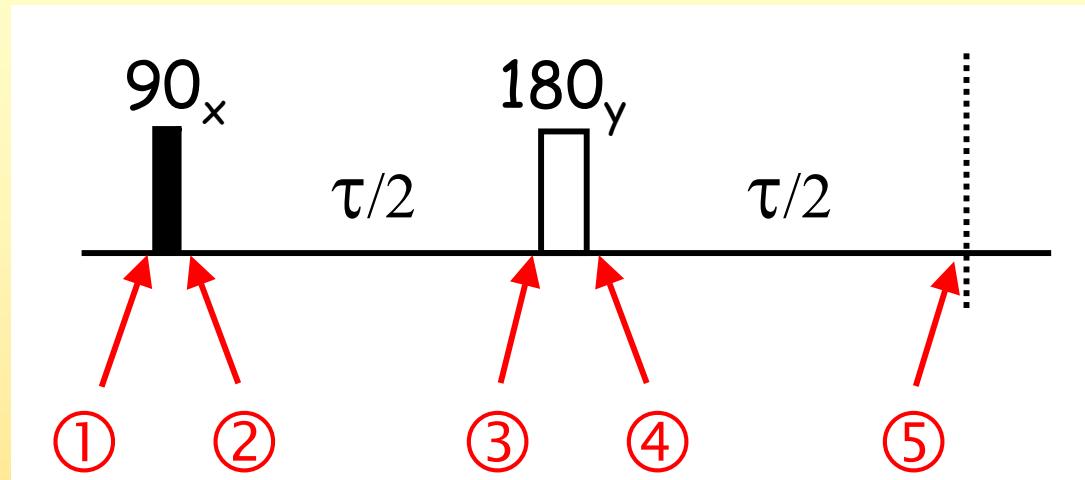


## The vector model



$\alpha, \beta$  are exchanged

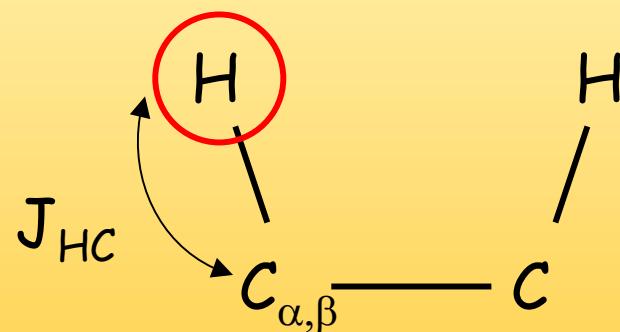
## The vector model



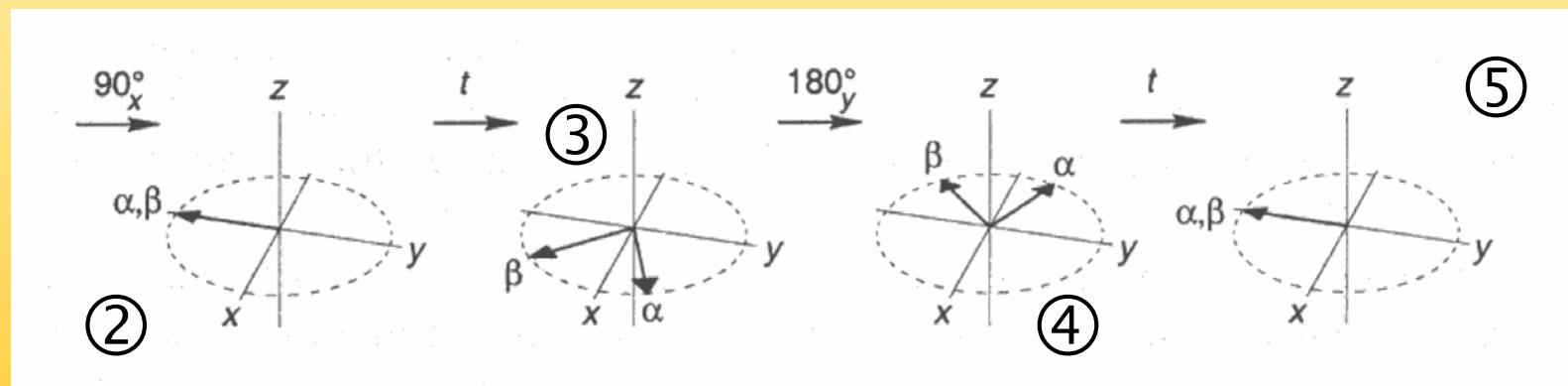
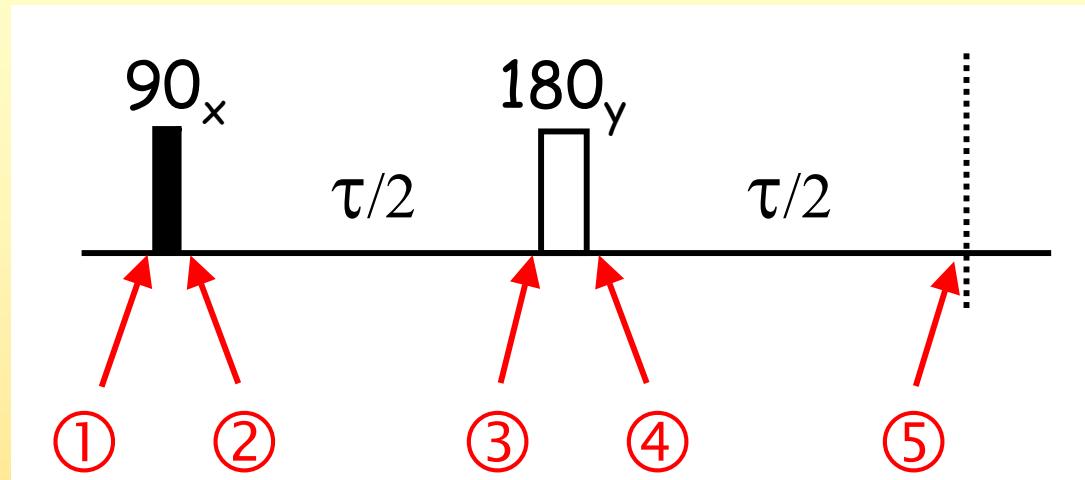
While the effect of chemical shift is still refocussed the coupling is not

## The vector model

In the case of heteronuclear scalar coupling the "other", the coupled spin is not hit by the  $180^\circ$  pulse

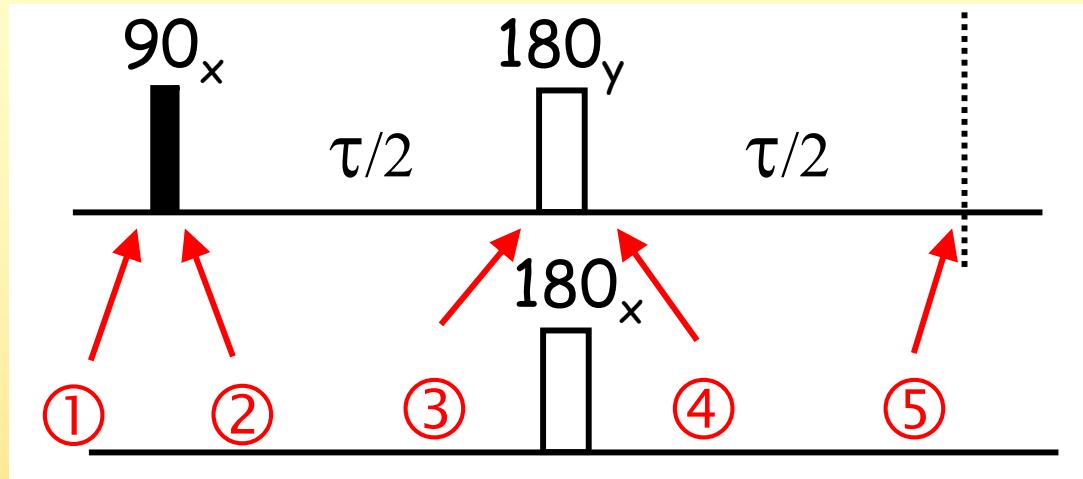


## The vector model



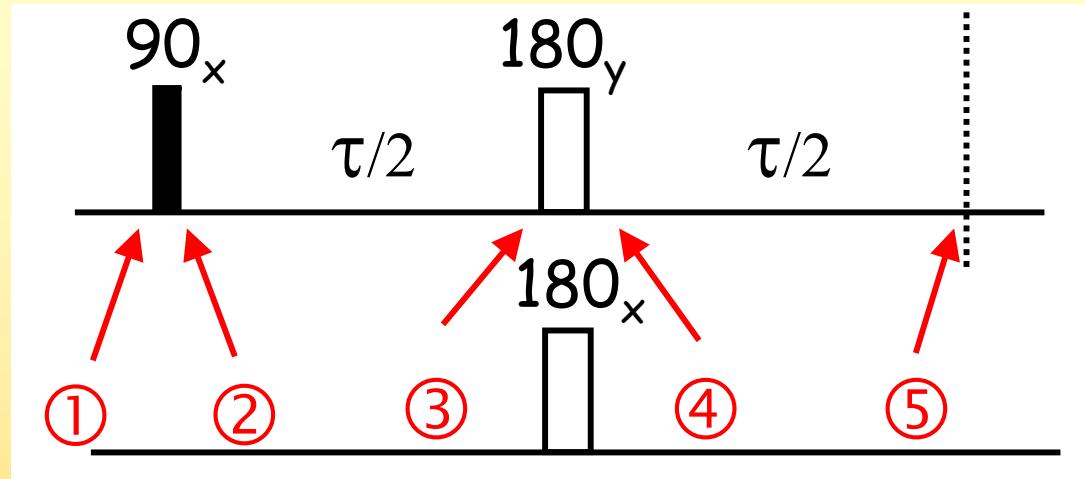
Now both the effect of chemical shift **AND** scalar coupling are refocussed !!

## The vector model

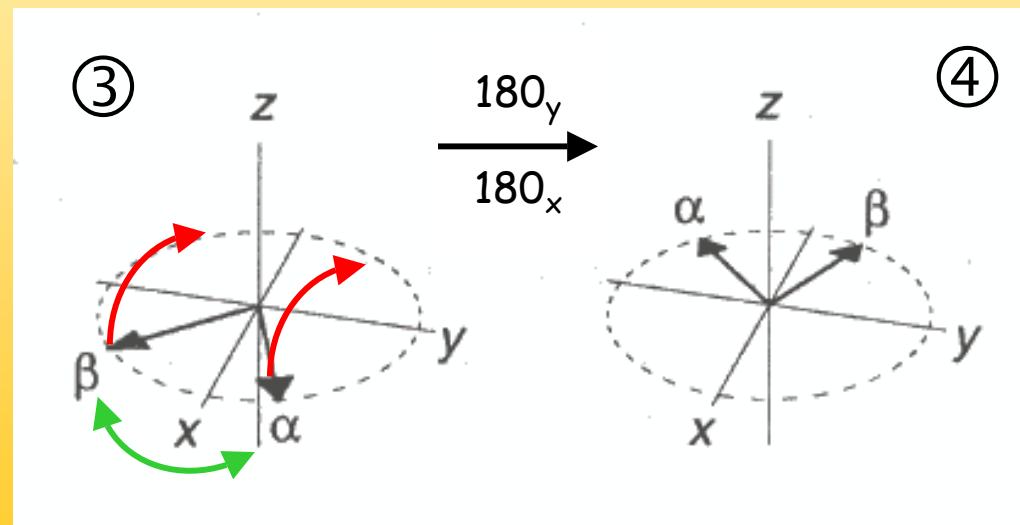


To affect the coupled spin we have to add a pulse. Now the the coupled spin is again hit by the pulse, the situation is comparable to the homonuclear case

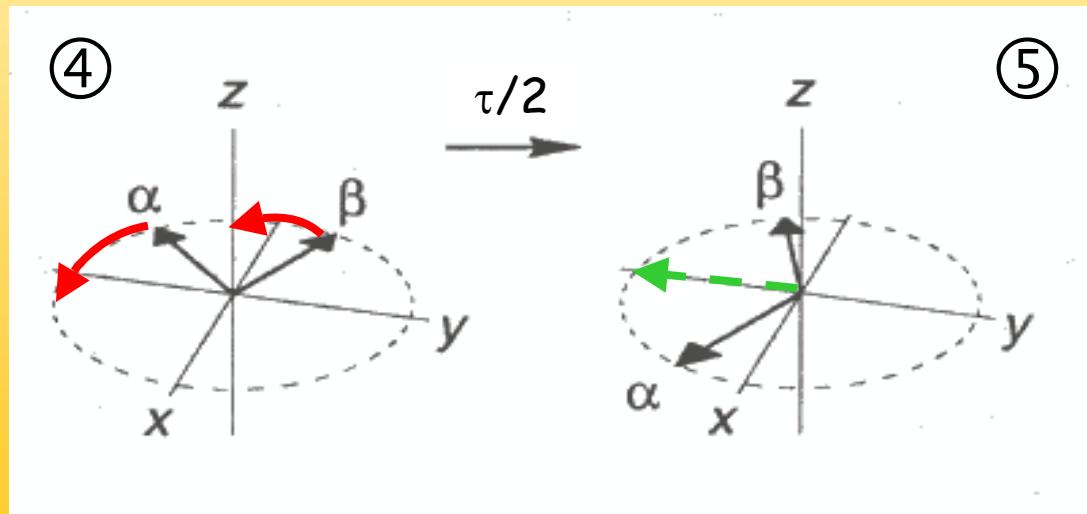
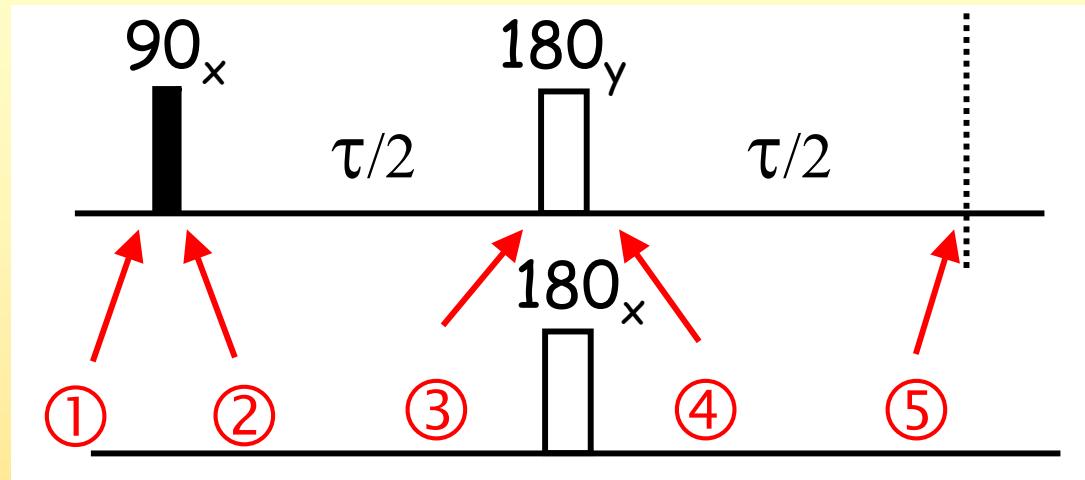
## The vector model



$\alpha, \beta$  are exchanged



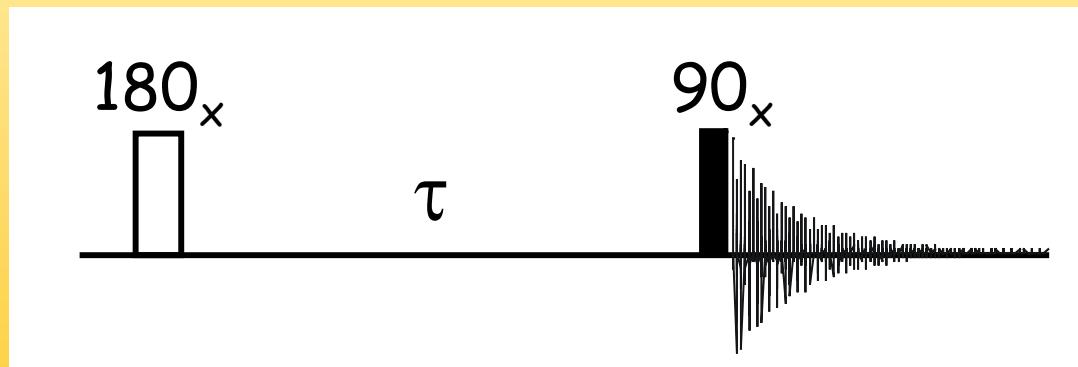
## The vector model



Again, the effect of chemical shift is refocussed but the coupling is not !

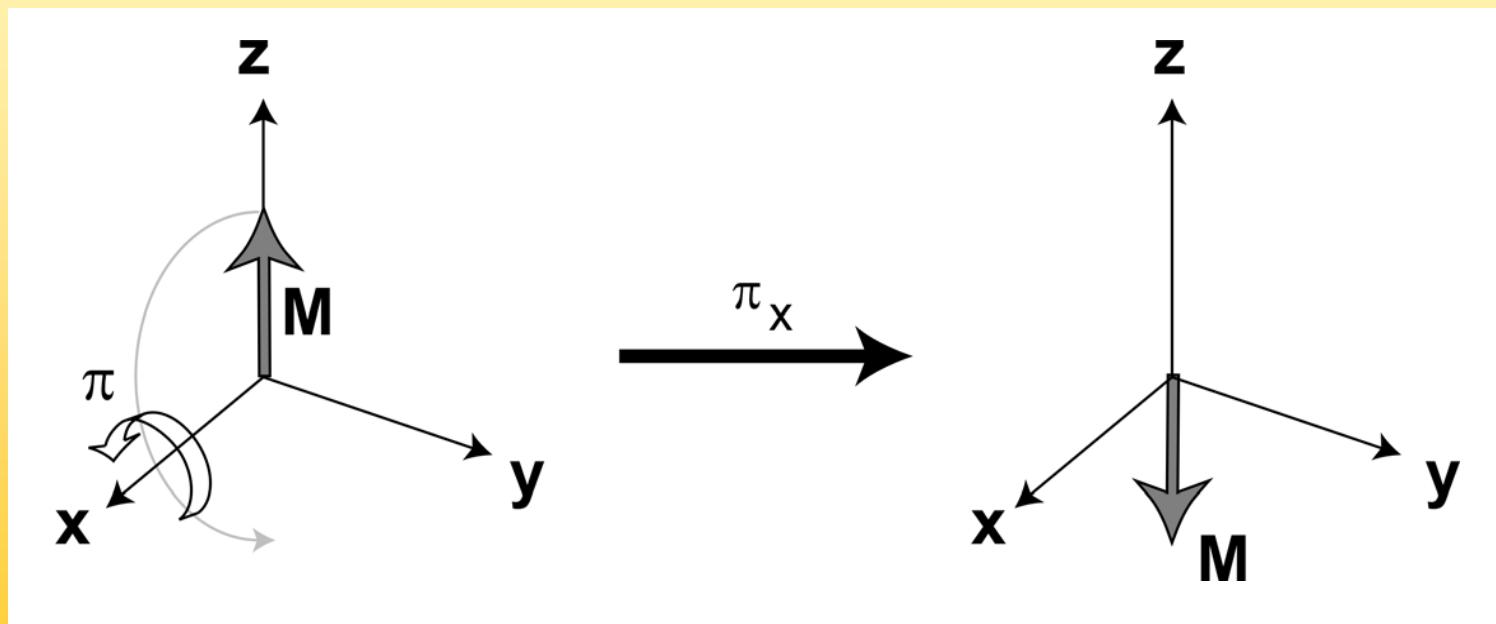
## The vector model

Using the vector model experiments for the determination of relaxation times can be explained. The inversion recovery experiment is used to determine longitudinal  $T_1$ -relaxation times



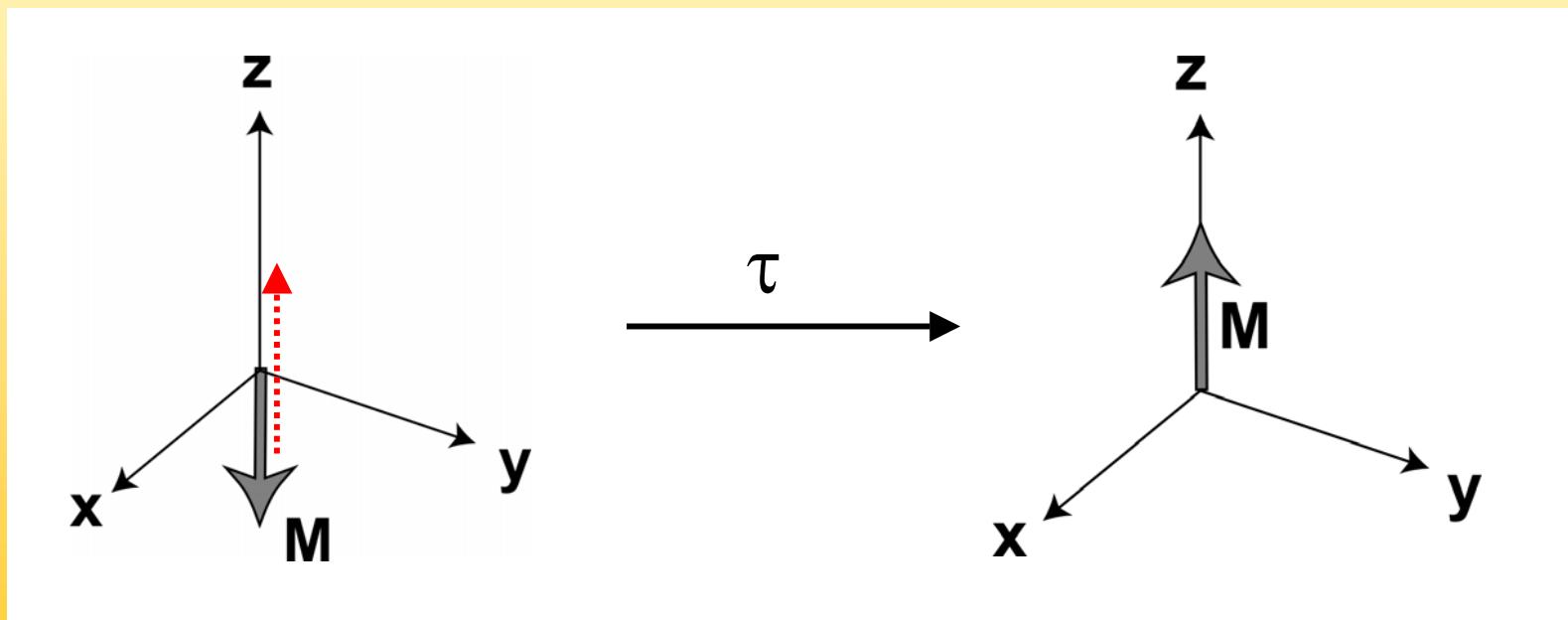
## The vector model

The effect of the  $180^\circ$  pulse is known, it rotates the magnetization to the  $(-z)$ -axis.



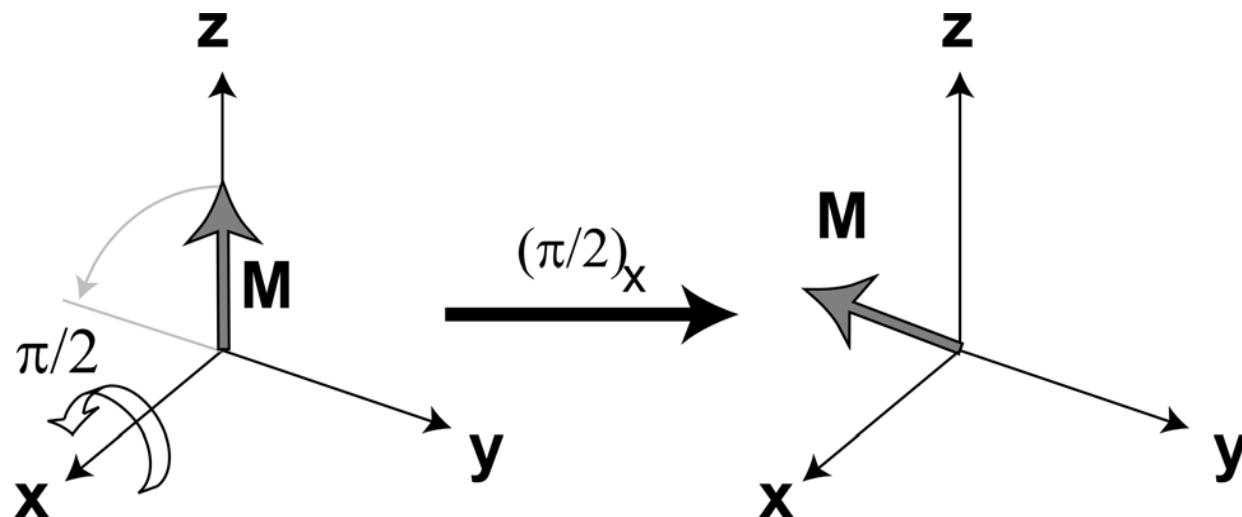
## The vector model

Then we wait for a certain amount of time ( $\tau$ ) while the magnetization returns to the (+z) direction



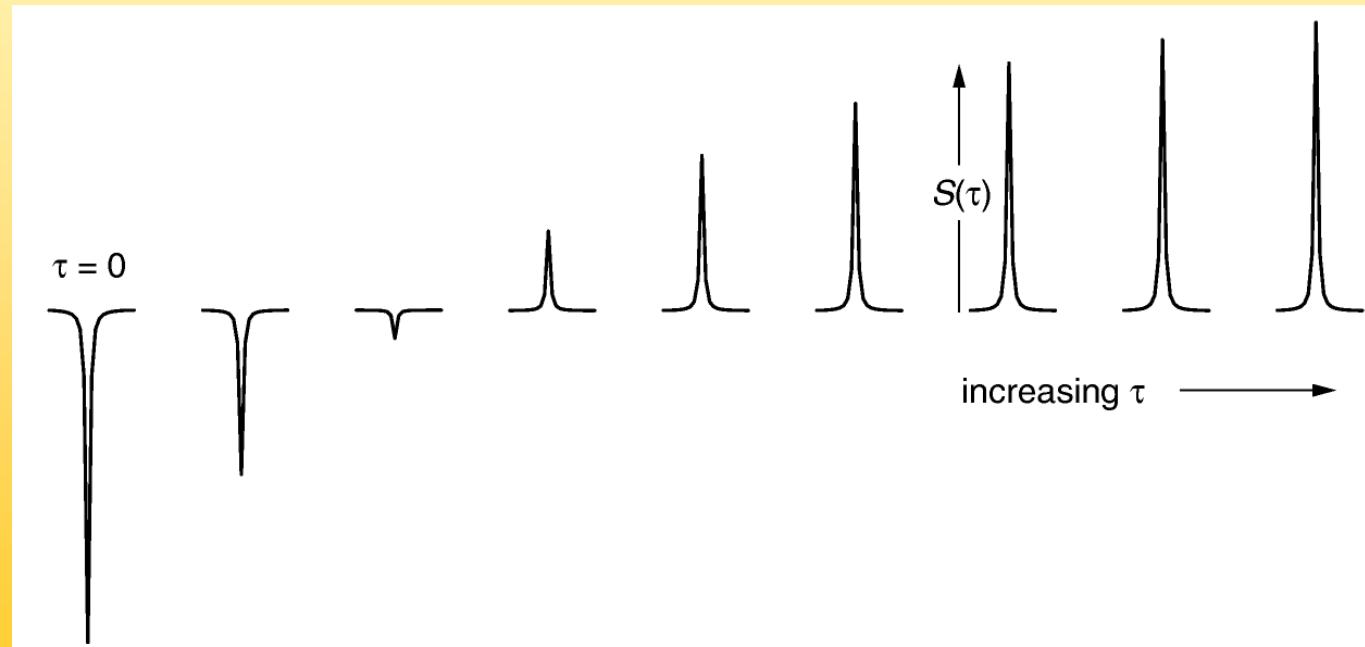
## The vector model

What magnetization is present after  $\tau$  is tested using a  $90^\circ$  pulse that converts the z-magnetization present into detectable magnetization



## The vector model

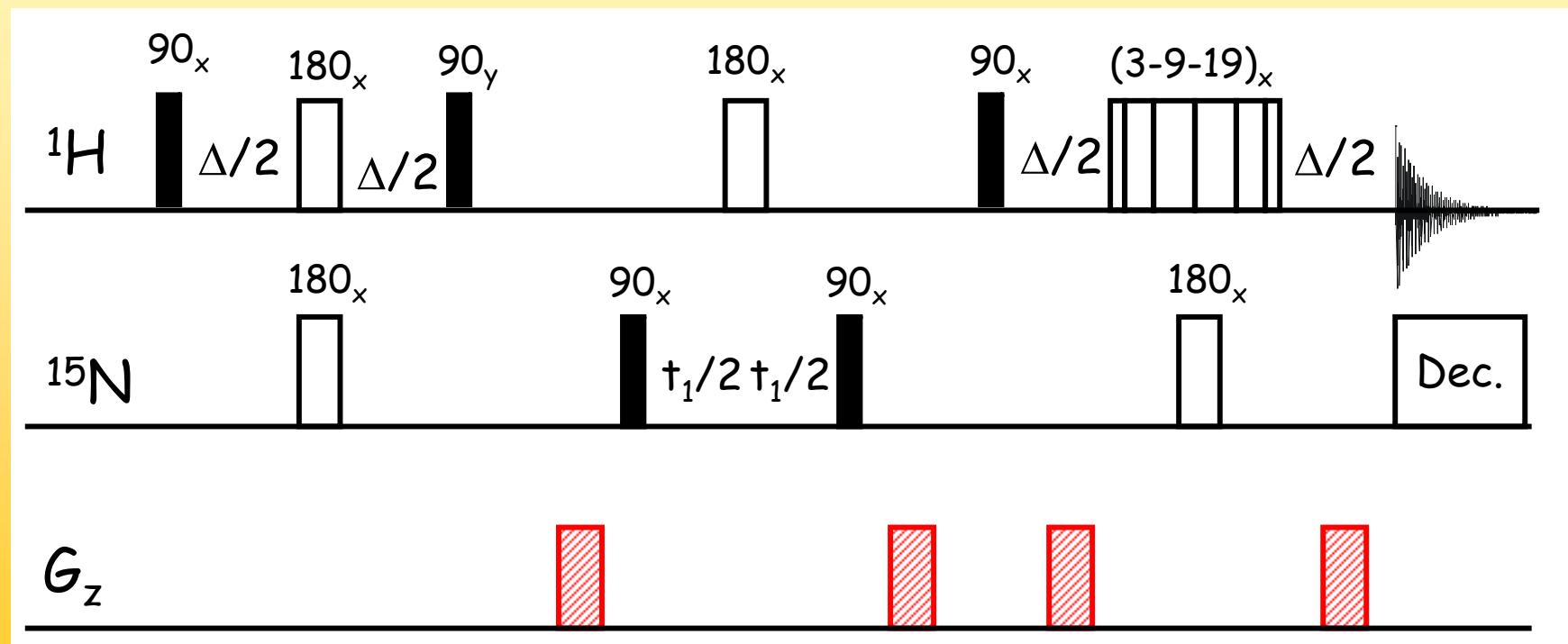
A series of experiments with different values for  $\tau$  is recorded and the relaxation time can be determined by fitting to a theoretical curve.



# Water flip back pulses

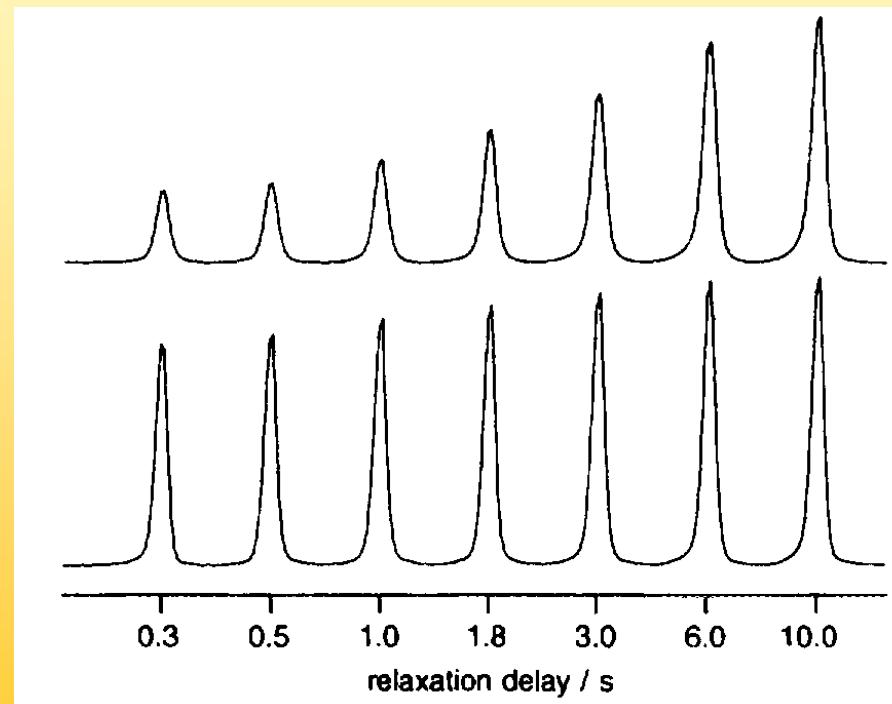
## Water flip back pulses

One of the most important experiments at least for proteins is the  $^{15}\text{N}$ -HSQC that correlates amide protons with the directly attached nitrogen



## Water flip back pulses

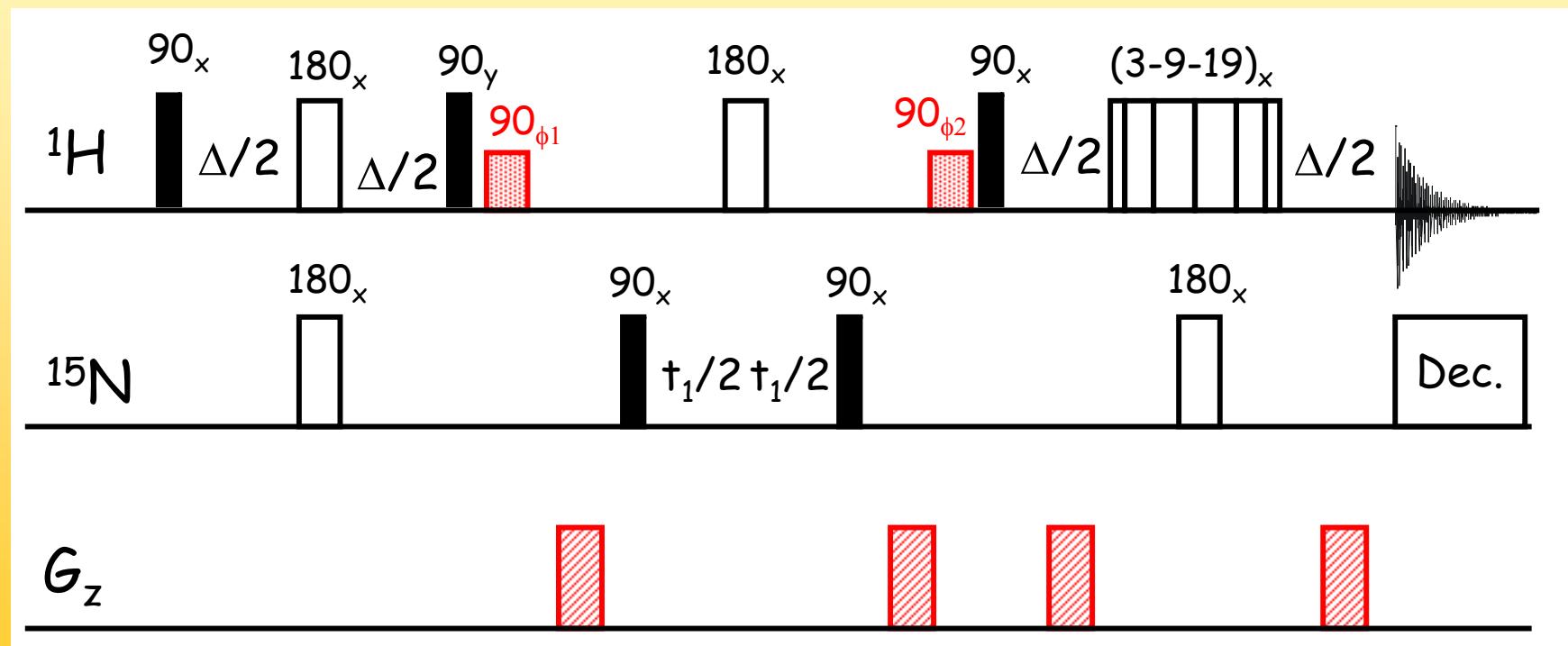
It was shown that the behaviour of the water, even though it is theoretically suppressed by the pulse sequence, has an influence on the signal intensity.



J. Stonehouse et al. *JMR A* 107, 178-184 (1994)

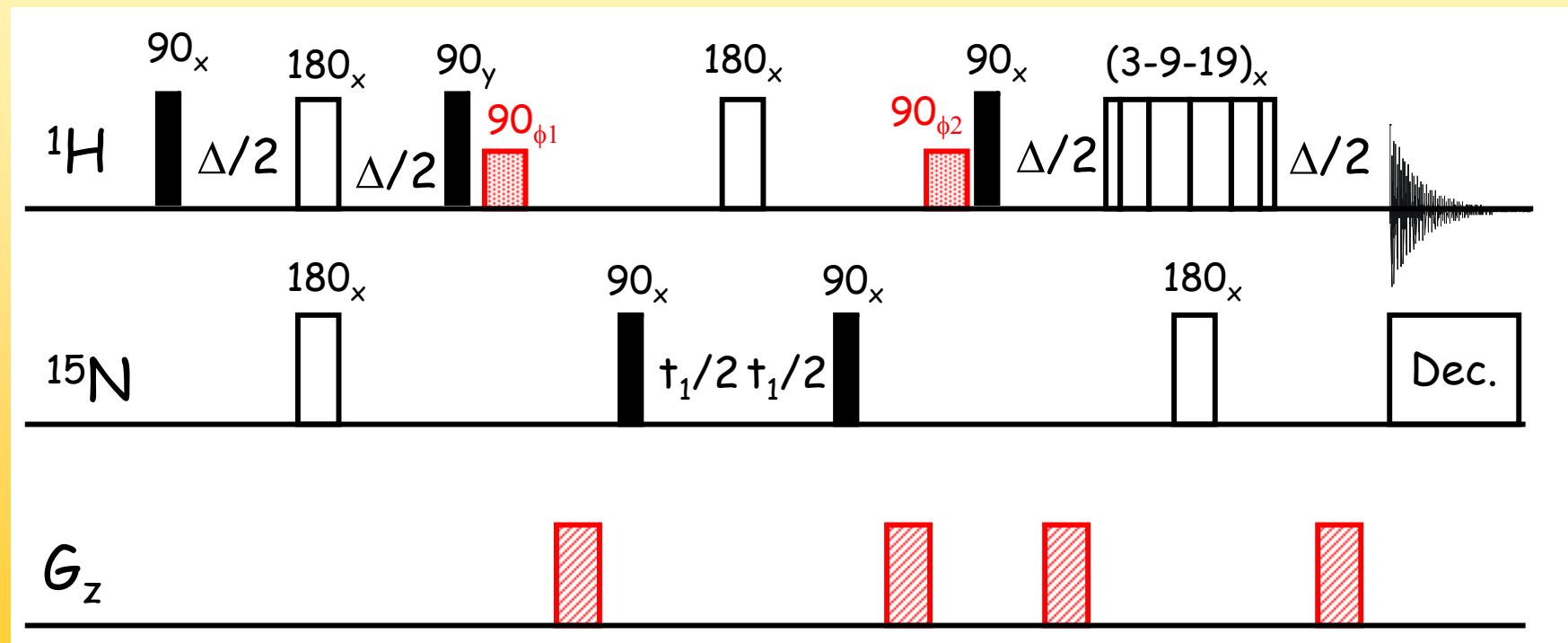
## Water flip back pulses

Therefore, additional pulses were implemented to control the water: water-flip-back-pulses to keep the water in the (+z)- or (-z)-direction all the time

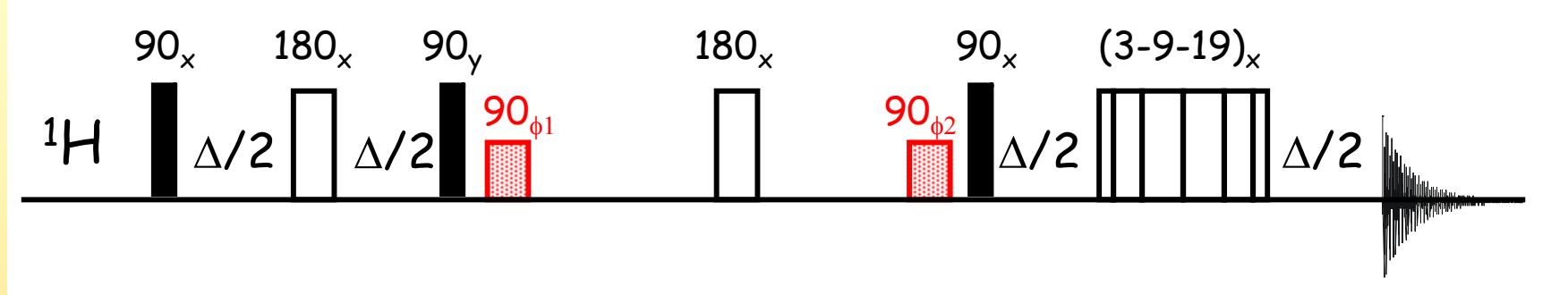


## Water flip back pulses

Using the vector model we can now follow the movement of the water and find out what we have to choose for  $\phi_1$  and  $\phi_2$  to achieve our goal

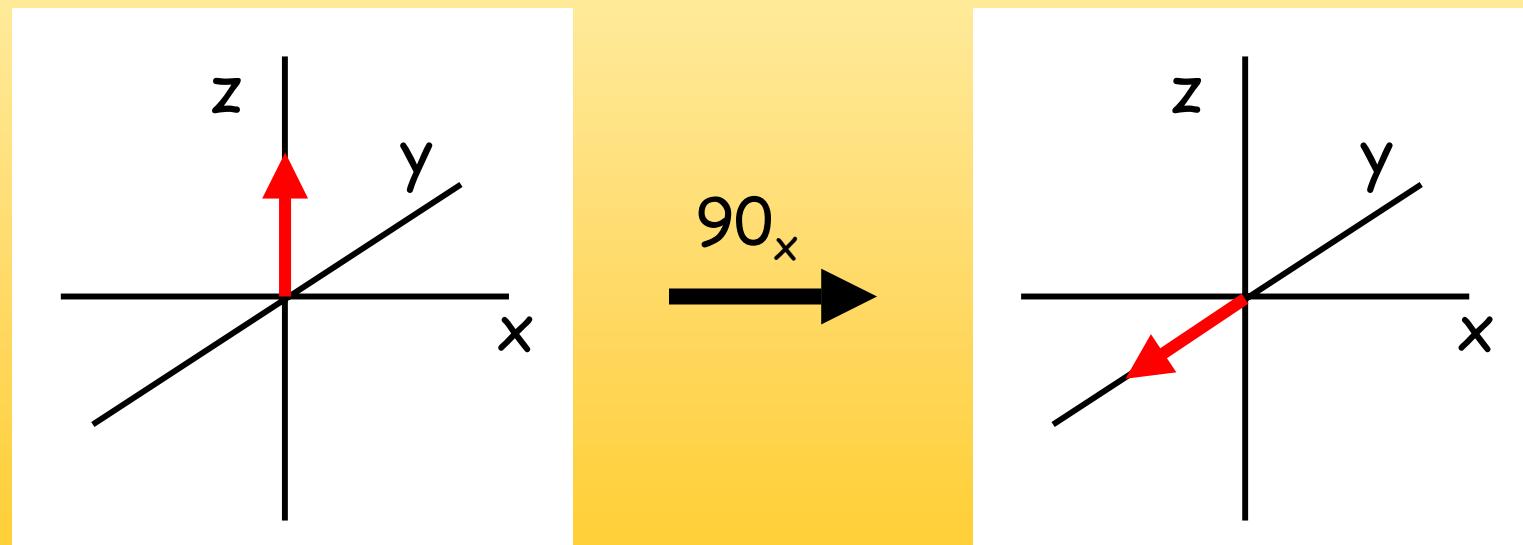
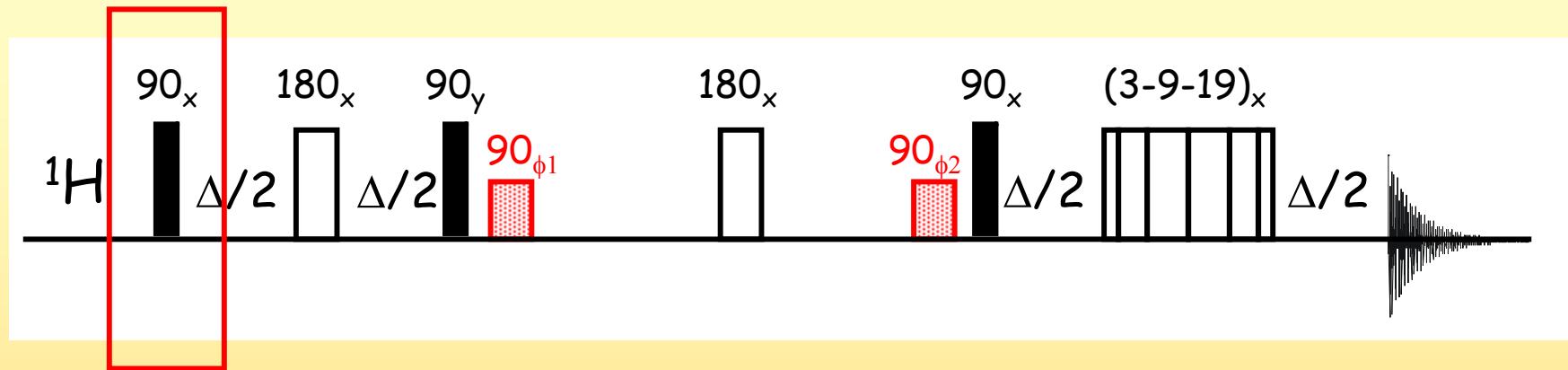


## Water flip back pulses

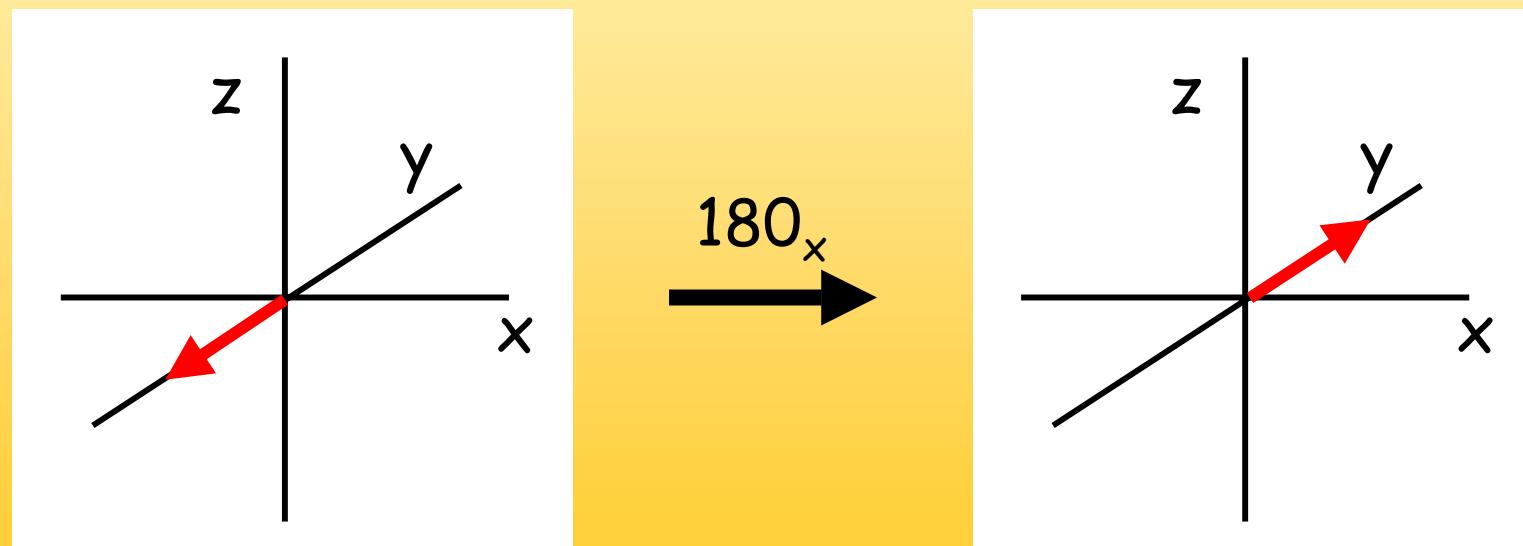
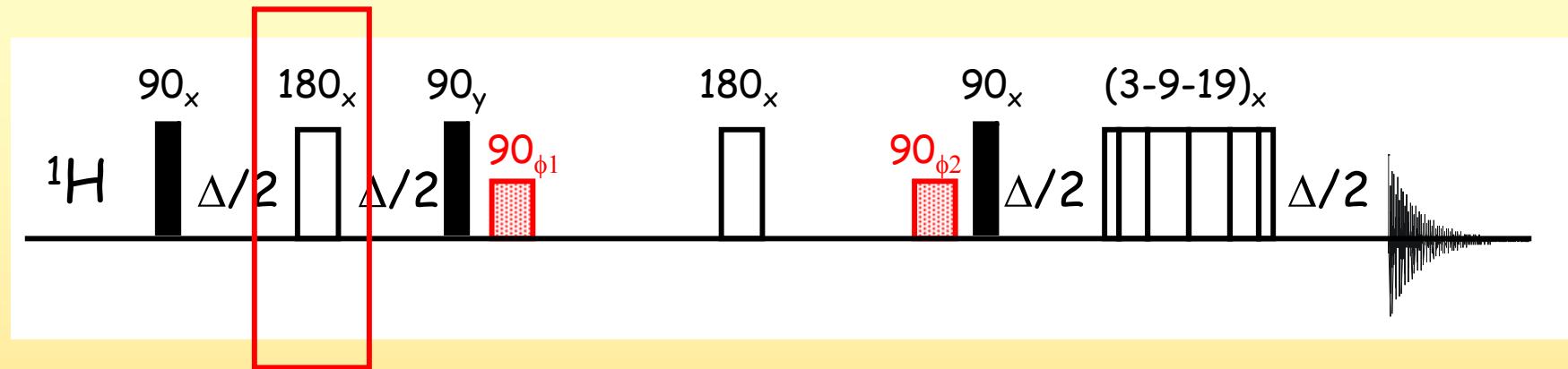


When considering the water resonance we need only look at the proton channel. And since we are sitting on resonance, we do not have to take chemical shift into account but can concentrate on the pulses.

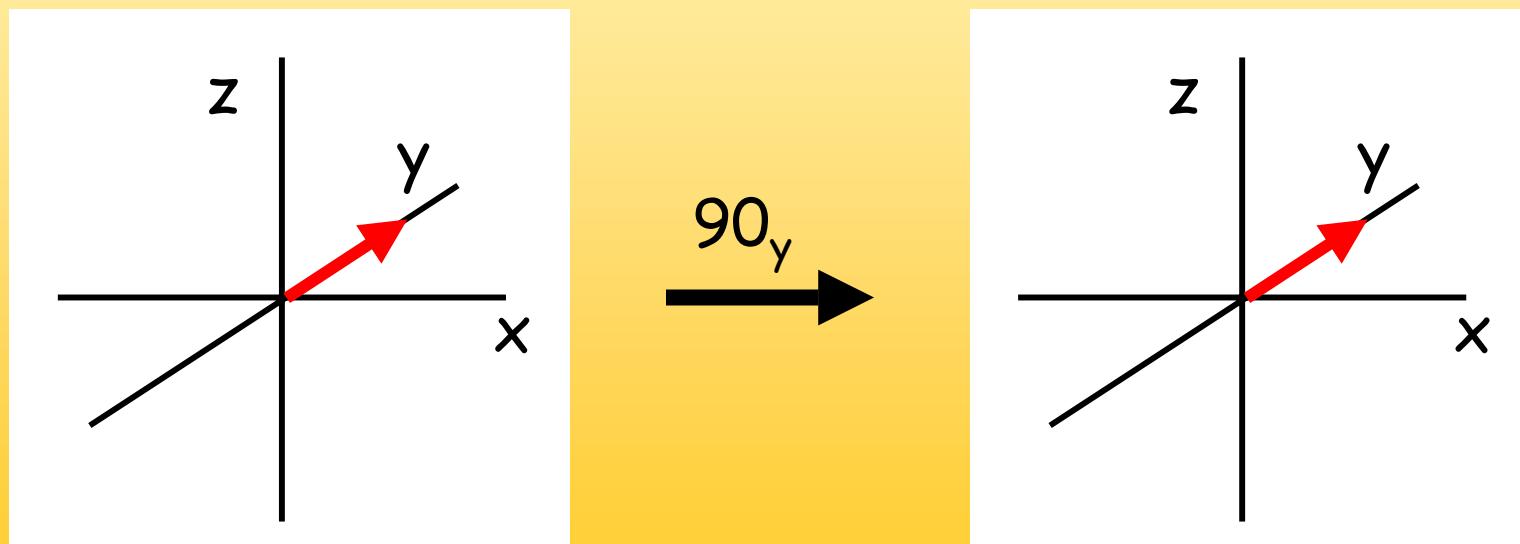
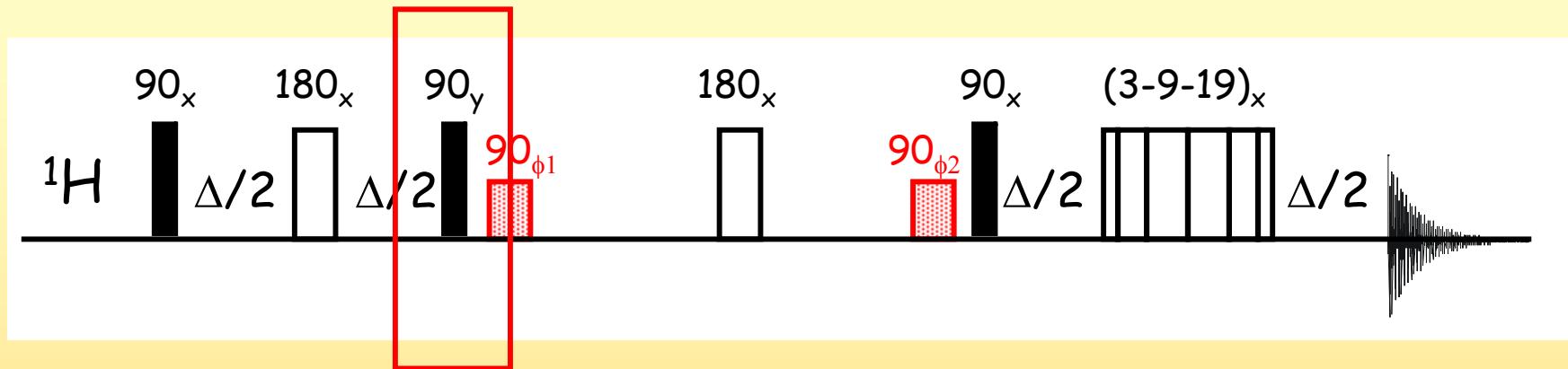
## Water flip back pulses



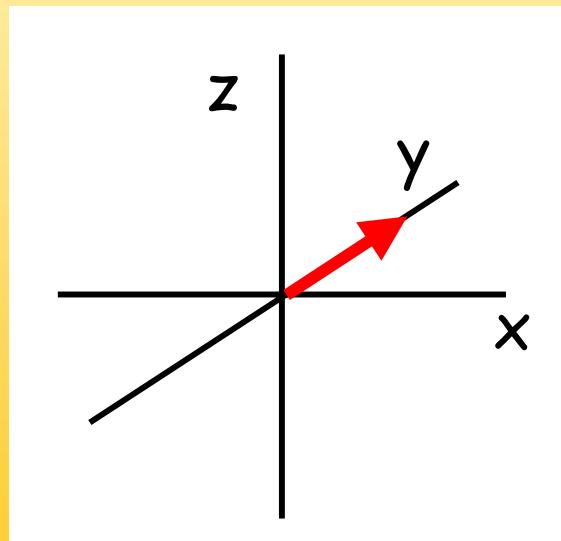
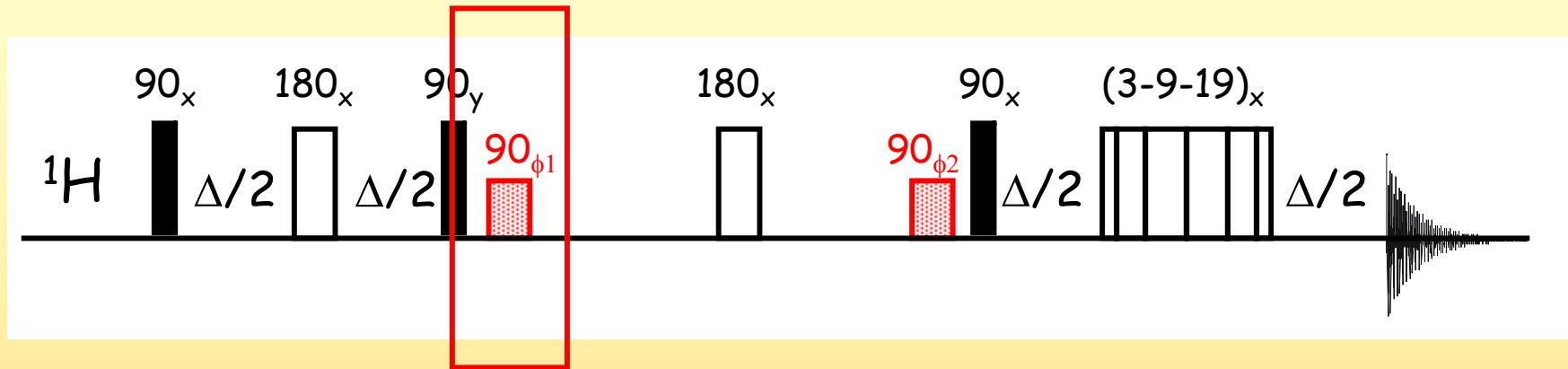
## Water flip back pulses



## Water flip back pulses

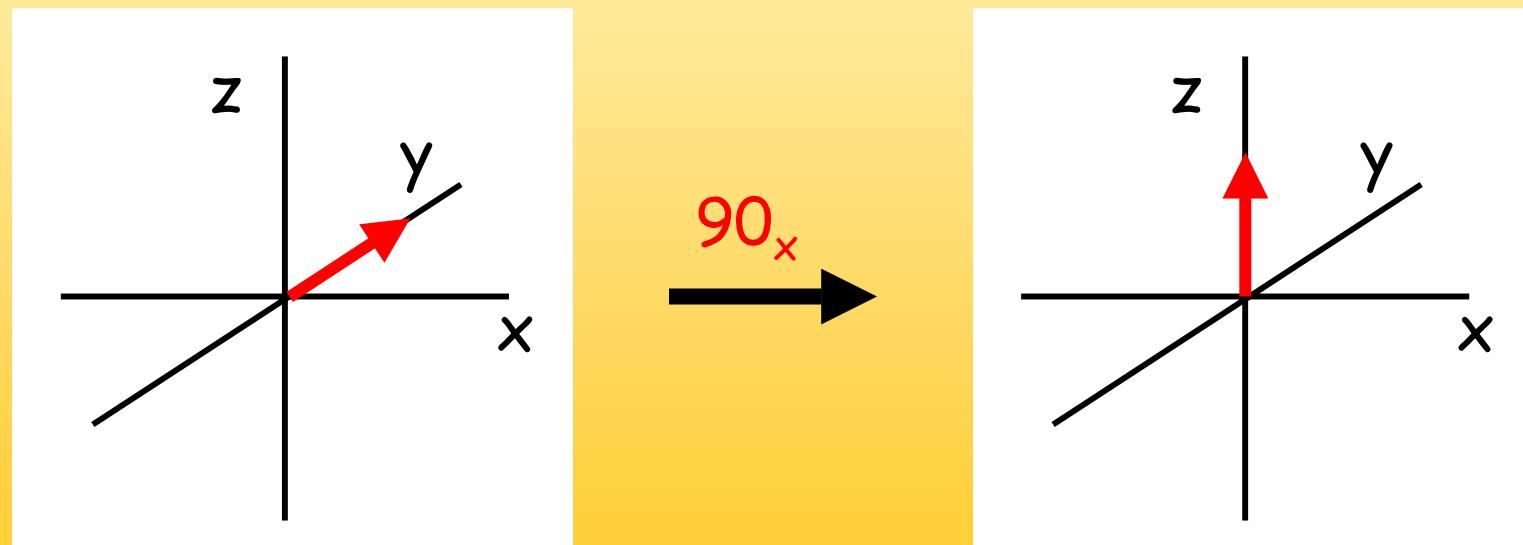
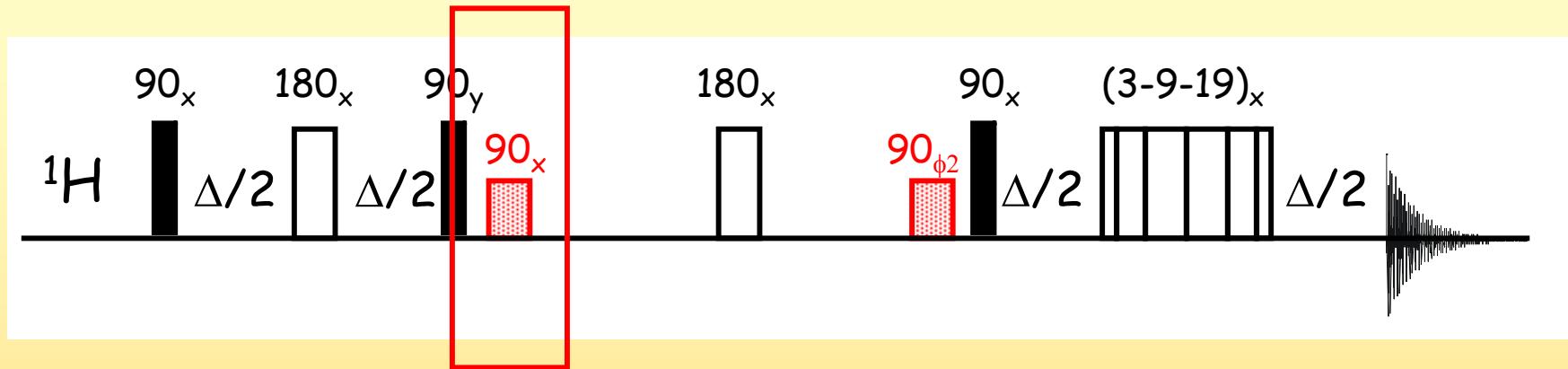


## Water flip back pulses

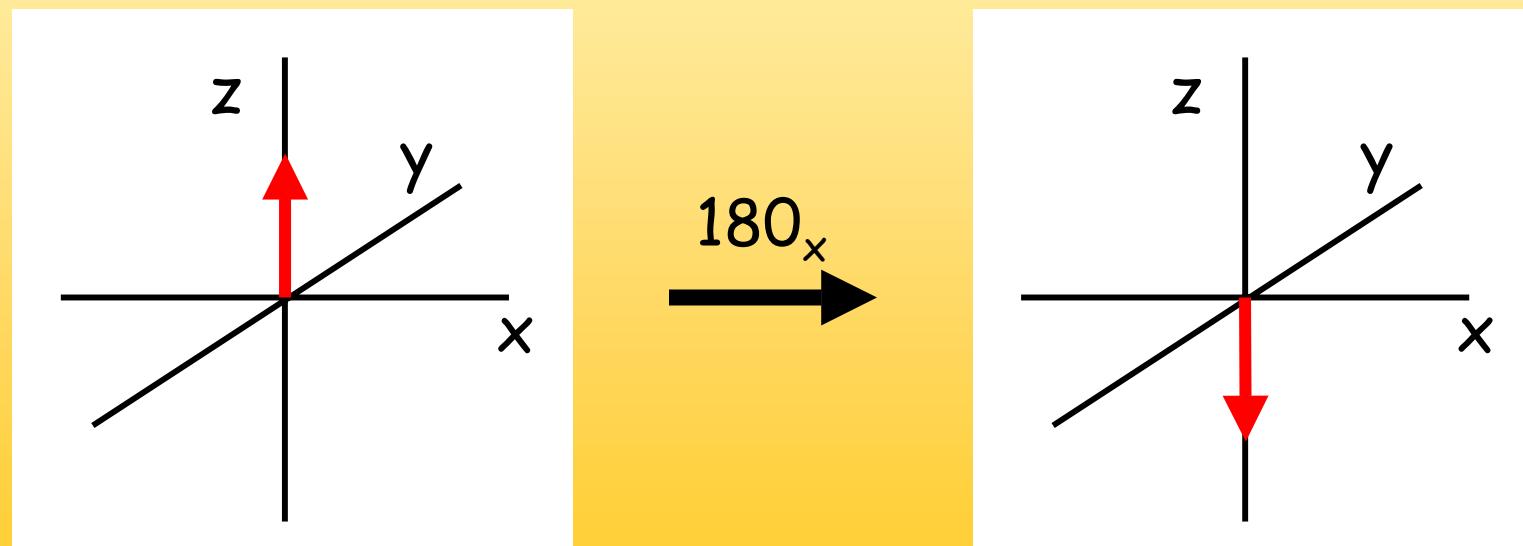
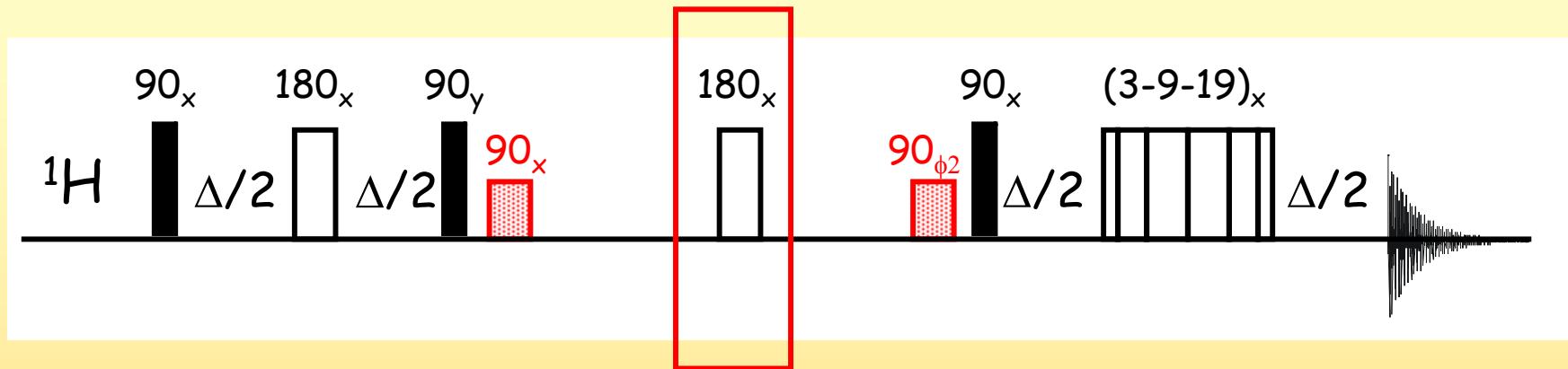


If we now want to get the water back to the z-axis before the gradient after the 90<sub>φ1</sub> pulse we see:  
 $\phi 1 = x$

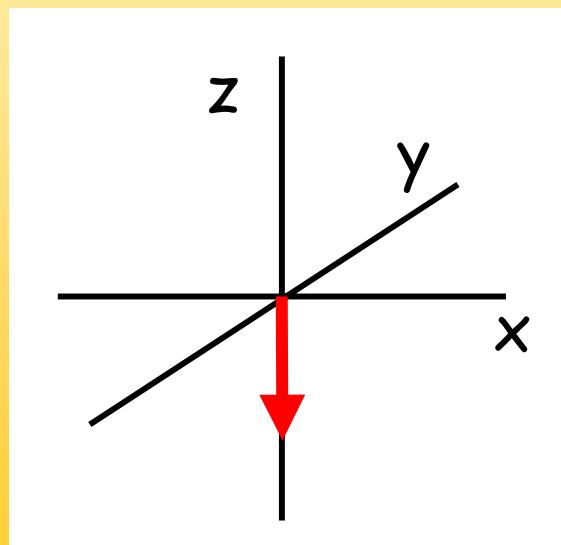
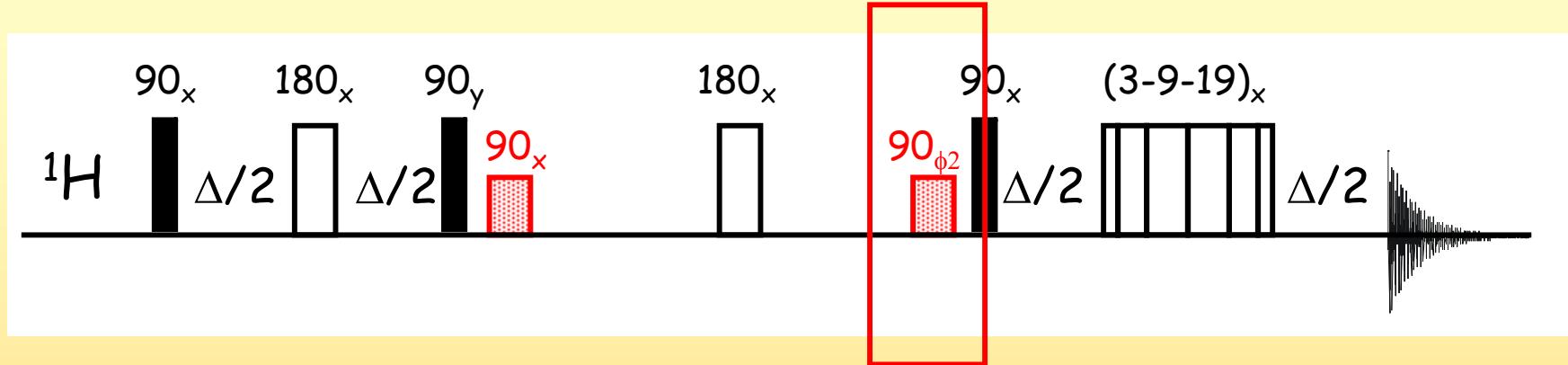
## Water flip back pulses



## Water flip back pulses



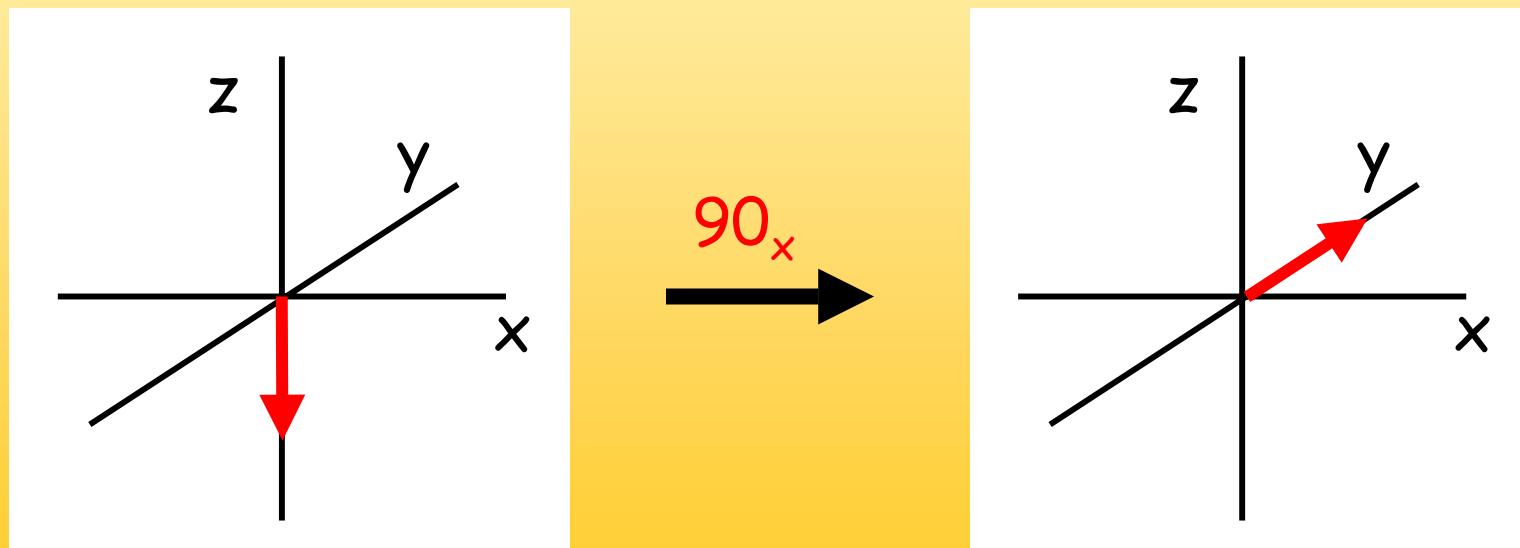
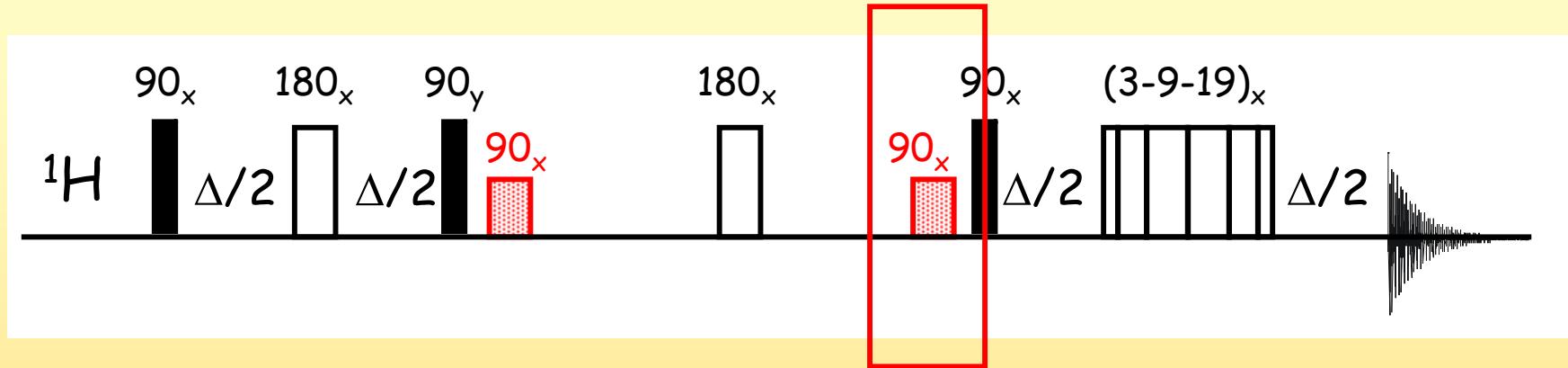
## Water flip back pulses



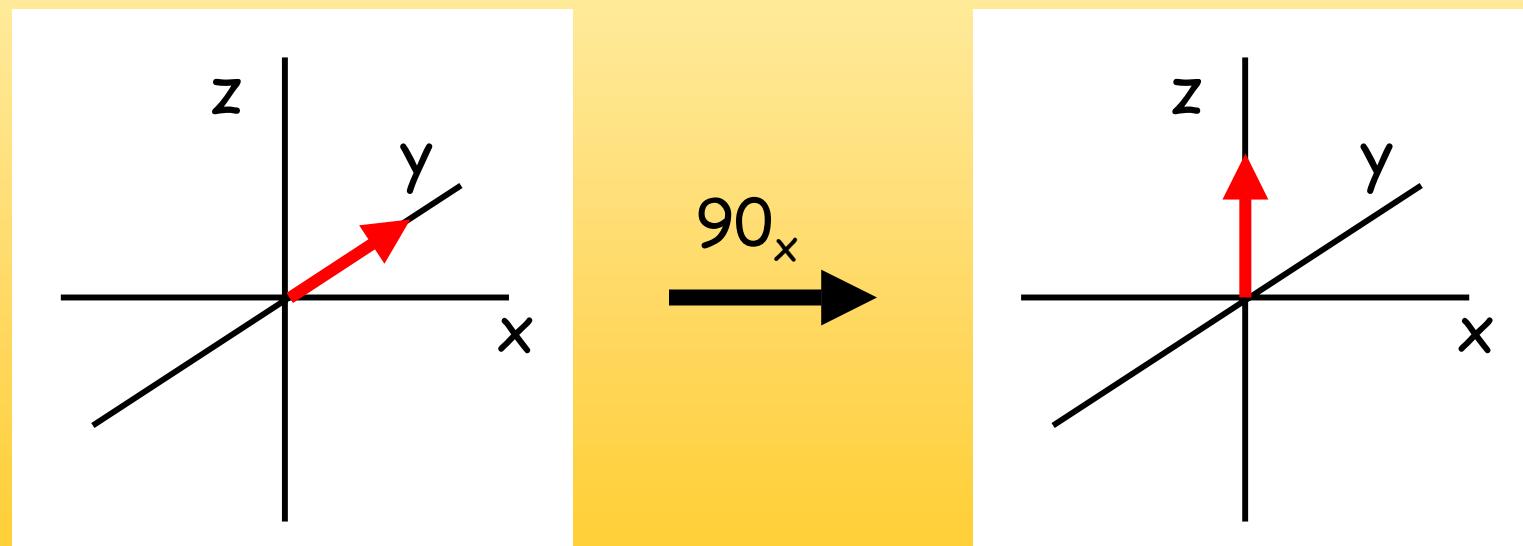
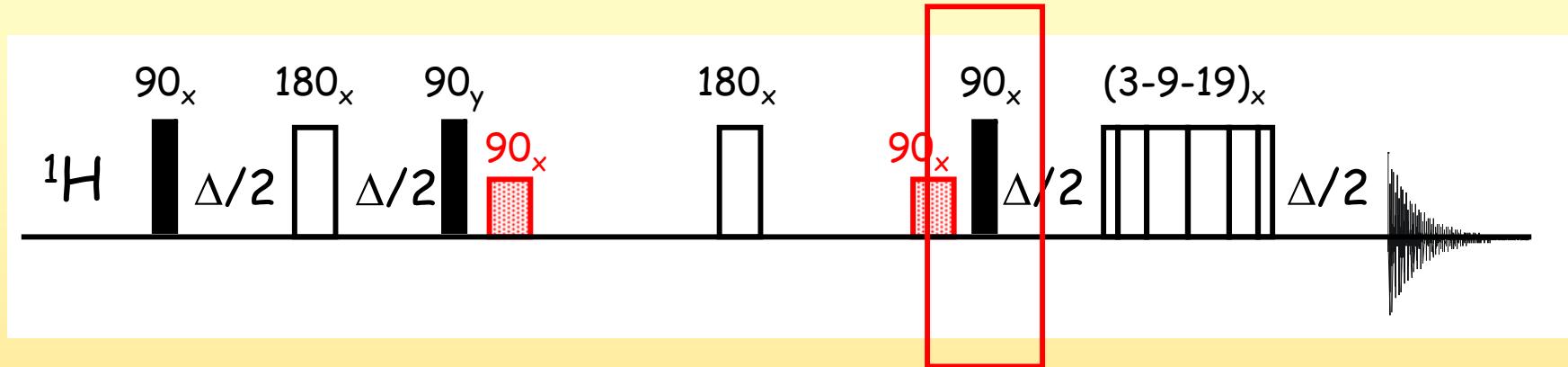
The  $(3-9-19)_x$  does nothing to the water, so the two following pulses have to turn the water to  $+z$ :

$$\phi 2 = x$$

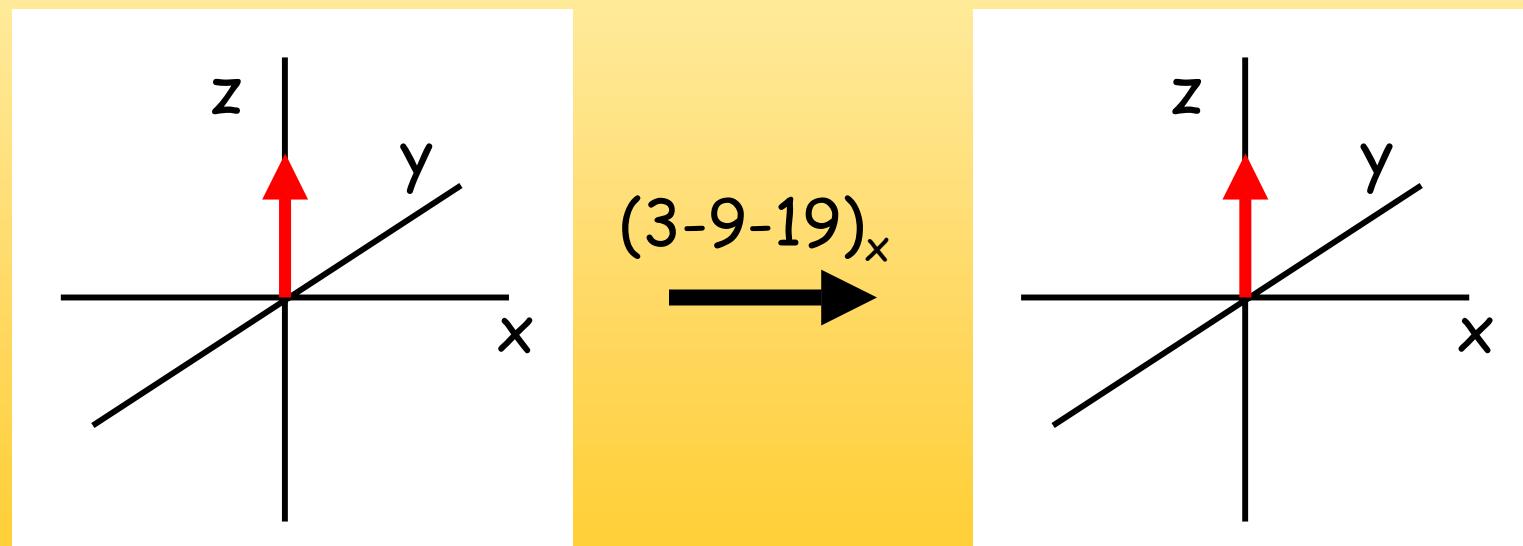
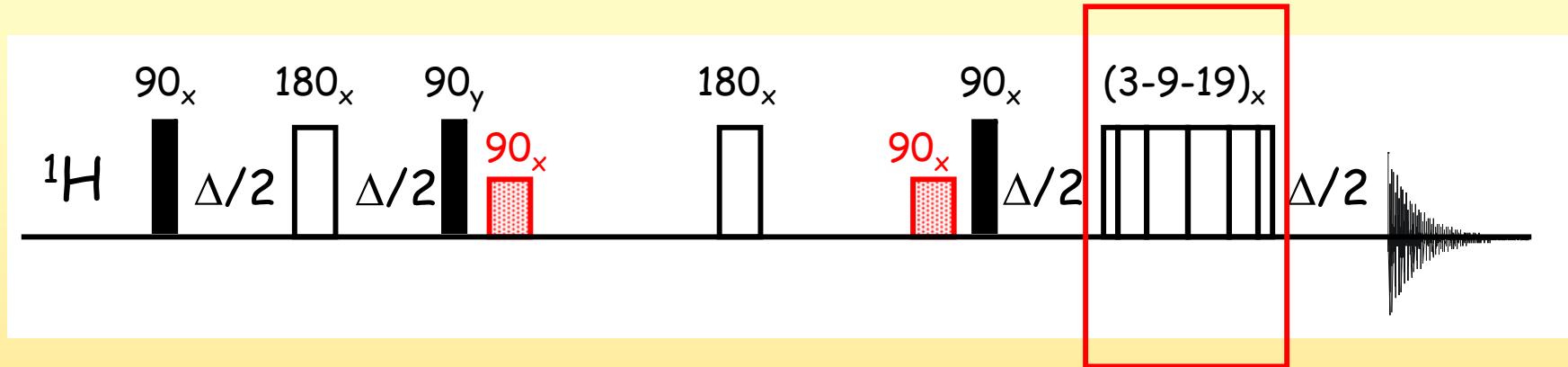
## Water flip back pulses



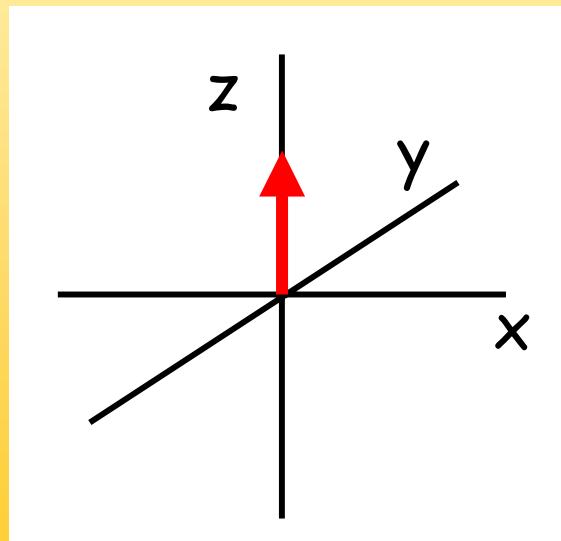
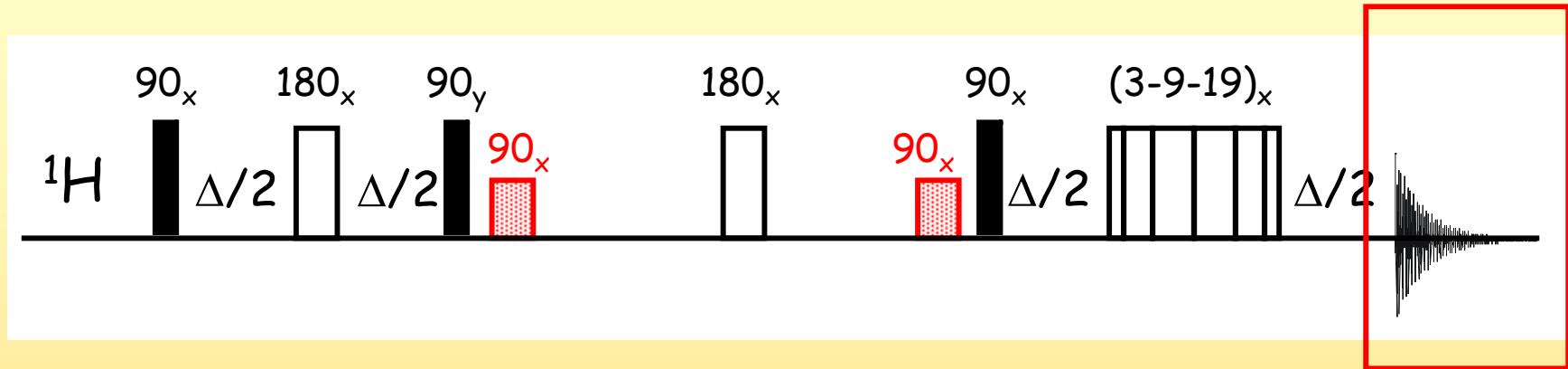
## Water flip back pulses



## Water flip back pulses



## Water flip back pulses



At the beginning of the acquisition we have achieved our goal, water points to the +z direction !

# That's it

[www.fmp-berlin.de/schmieder/teaching/selenko\\_seminars.htm](http://www.fmp-berlin.de/schmieder/teaching/selenko_seminars.htm)



NMR of organic compounds and small biomolecules II

Peter Schmieder  
AG Solution NMR